

**Obrazové Transformácie**  
Cvičenia z Počítačového Videnia

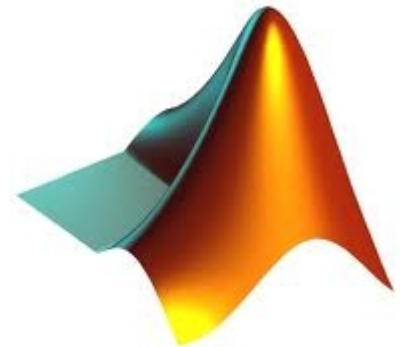
**Zuzana Haladová**  
**Júlia Kučerová**

# Obrazové transformácie

Zovšeobecnená Houghova transformácia

Rýchla Fourierova transformácia

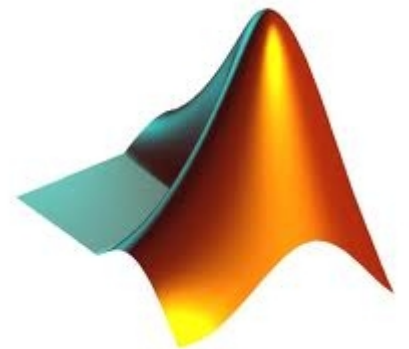
Diskrétna kosínusová transformácia



# Hough

Houghova transformácia- ak chceme detekovať oblasti zo známym tvarom hranice

- Vieme detekovať priamky aj krivky, ak je známe ich analytické vyjadrenie
- Metóda je robustná aj pre zašumené objekty



# Hough

Houghova transformácia pre priamky

- Priamku vieme vyjadriť

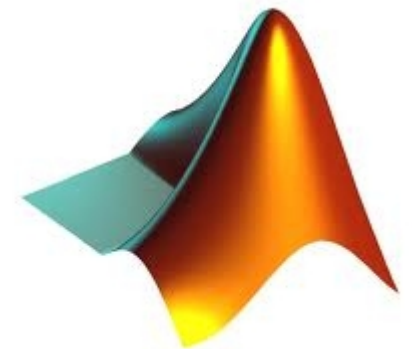
$$y = mx + b$$

- Houghova trans. reprezentuje priamku pomocou  $b$ ,  $m$  resp.  $r$ ,  $\theta$  pričom

-  $r$  je najmenšia vzdialenosť od počiatku k priamke



$\theta$  je uhol medzi  $x$  a priamkou



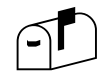
# Hough

Vyjadrenie priamky pomocou  $r$  a  $\theta$  je:

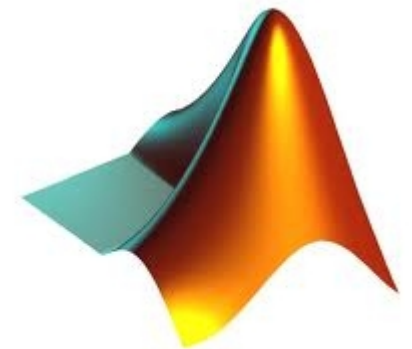


HT pracuje na bin. obrázku

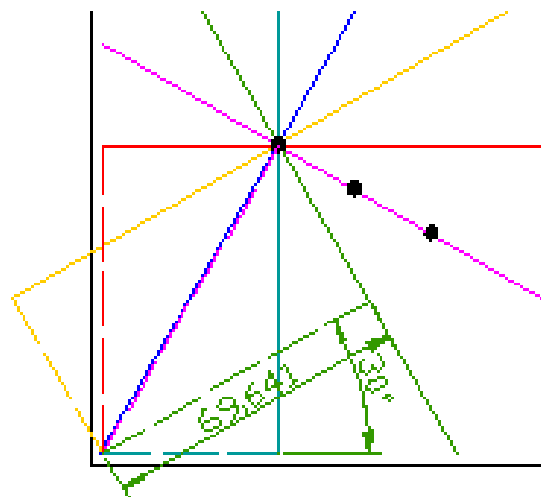
nasledovne  $y = \left(-\frac{\cos \Theta}{\sin \Theta}\right)x + \left(\frac{r}{\sin \Theta}\right)$



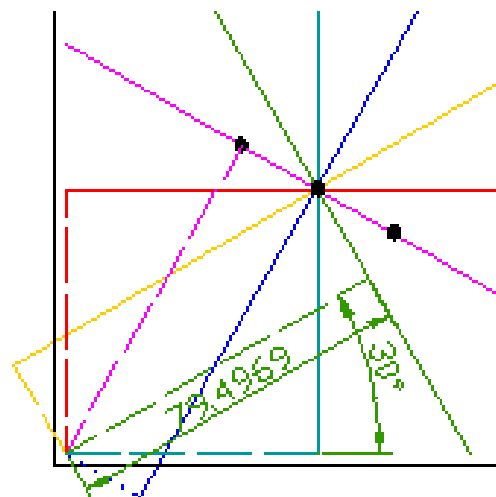
Pre každý bod obrázku a pre každú priamku ním prechádzajúcu vypočíta  $r$  a  $\theta$  tejto priamky.



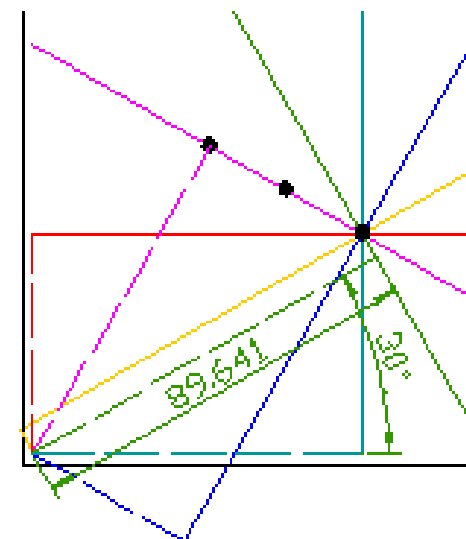
# Hough



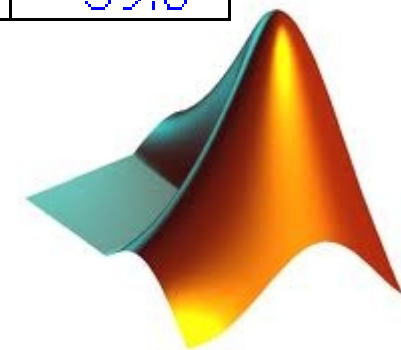
| Angle | Dist. |
|-------|-------|
| 0     | 40    |
| 30    | 69.6  |
| 60    | 81.2  |
| 90    | 70    |
| 120   | 40.6  |
| 150   | 0.4   |



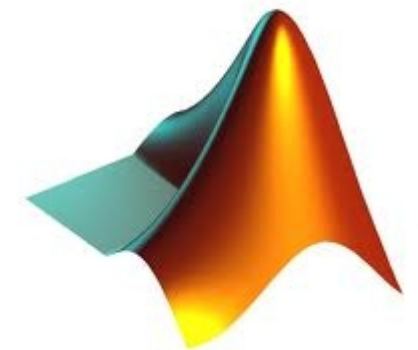
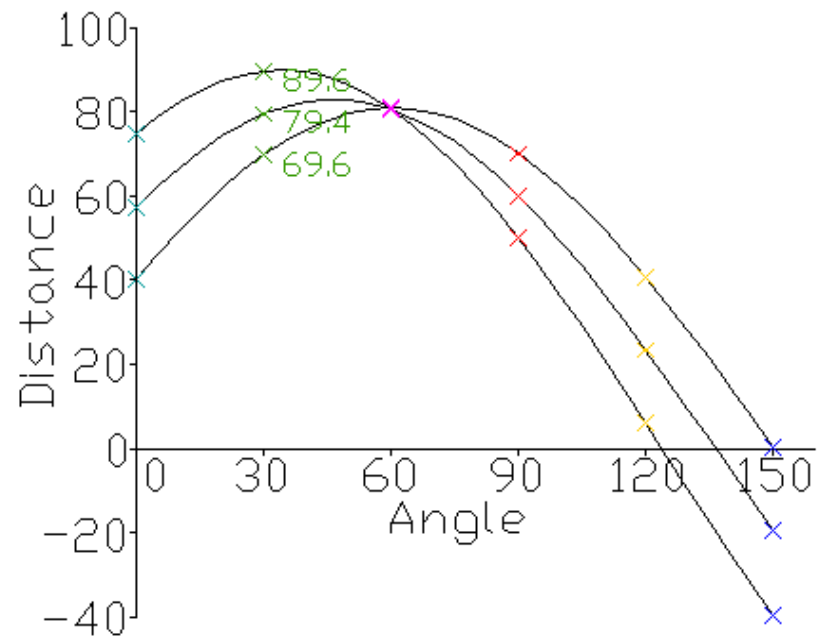
| Angle | Dist. |
|-------|-------|
| 0     | 57.1  |
| 30    | 79.5  |
| 60    | 80.5  |
| 90    | 60    |
| 120   | 23.4  |
| 150   | -19.5 |



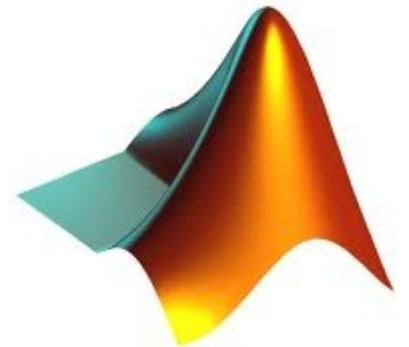
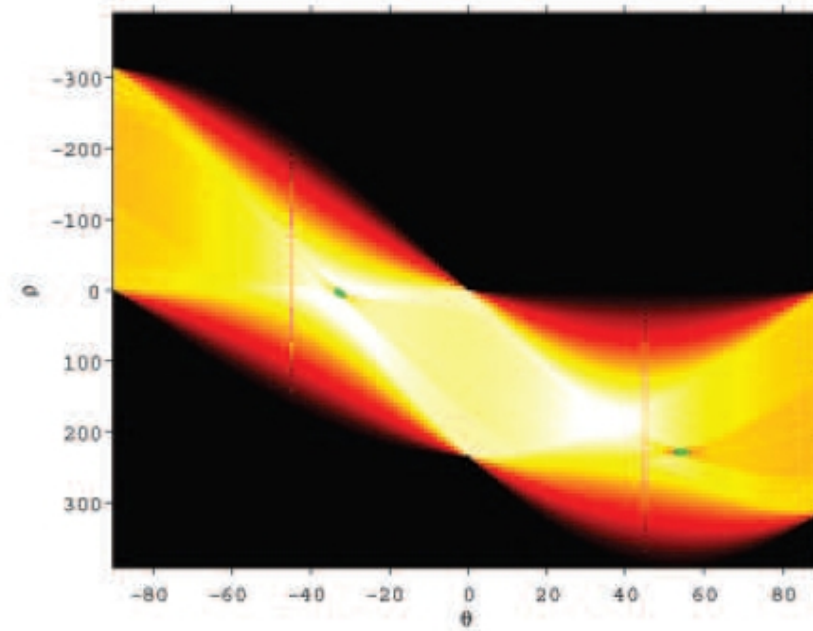
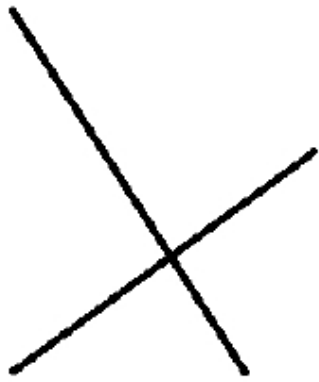
| Angle | Dist. |
|-------|-------|
| 0     | 74.6  |
| 30    | 89.6  |
| 60    | 80.6  |
| 90    | 50    |
| 120   | 6.0   |
| 150   | -39.6 |



# Hough



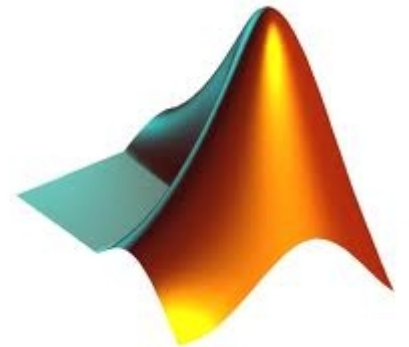
# Hough



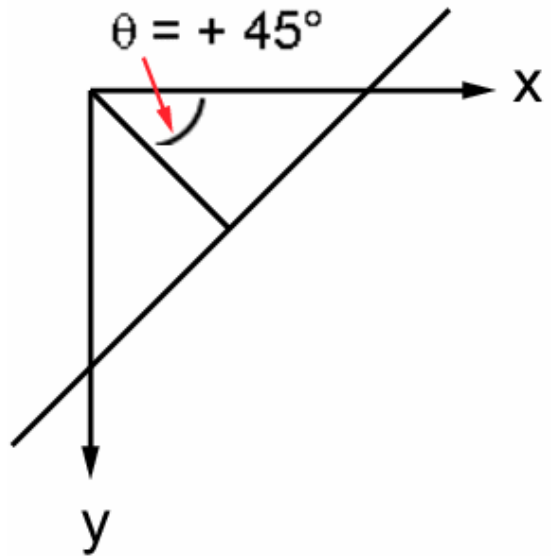
# Hough

V MATLAB (Image Processing Toolbox)

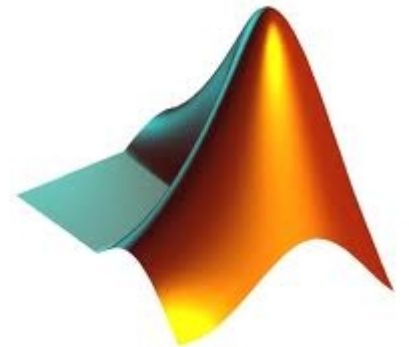
```
I=imread('1.jpg'); IG =rgb2gray(I);  
IE=edge(IG,'Canny');  
[H,T,R]=hough(IE);  
imshow(imadjust(mat2gray(H)), 'XData',T, 'YData',  
R); colormap(hot);
```



# Hough



$$\rho = x \cdot \cos(\theta) + y \cdot \sin(\theta)$$



# Hough

$[H, T, R] = \text{hough}(IE);$



H – matica Houghovej transformácie



T je pole hodnôt  $\theta$  a R je pole r nad ktorými je vyjadrená H



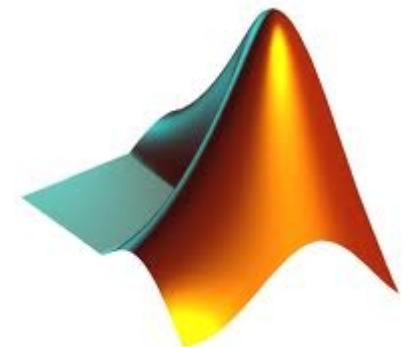
Riadky a stĺpce H zodpovedajú r a  $\theta$



hodnota na pozícii (1,2) zodpovedá počtu

bodov ležiacich na priamke z 1. r a

2.  $\theta$  z polí R a T



# Hough

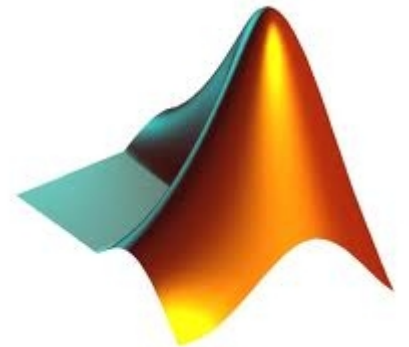
`[H,T,R]=hough(IE);`

- `peaks = houghpeaks(H, numpeaks)`

- `peaks` je pole  $Q \times 2$  kde  $Q$

`<0,numpeaks>`

a obsahuje  $x,y$  hodnoty pre `peaks` v `H`



# Hough

`lines = houghlines(BW, theta, rho, peaks)`

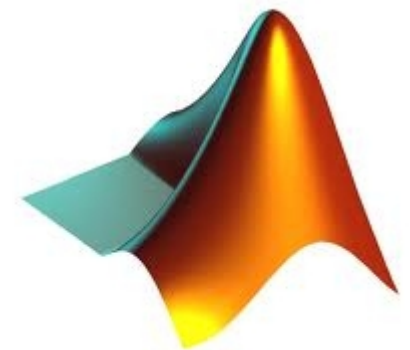
 `lines` je štruktúrované pole ktoré pre každú nájdenú úsečku obsahuje:

 `point1` x,y hodnoty konca úsečky

 `point2` x,y hodnoty konca úsečky

 `theta` uhol v stupňoch (z matice H)

 `rho` hodnota(z matice H)



# Hough

```
lines = houghlines(IE, theta, rho, peaks)
```

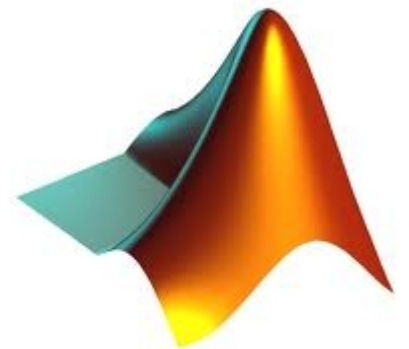
```
- figure, imshow(IE), hold on
```

```
📁 for k = 1:length(lines)
```

```
📁 xy = [lines(k).point1; lines(k).point2];
```

```
📁 plot(xy(:,1),xy(:,2),'Color','green');
```

```
📁 end
```

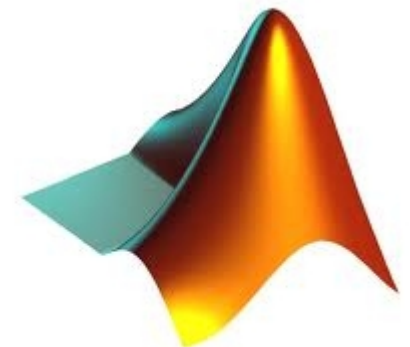
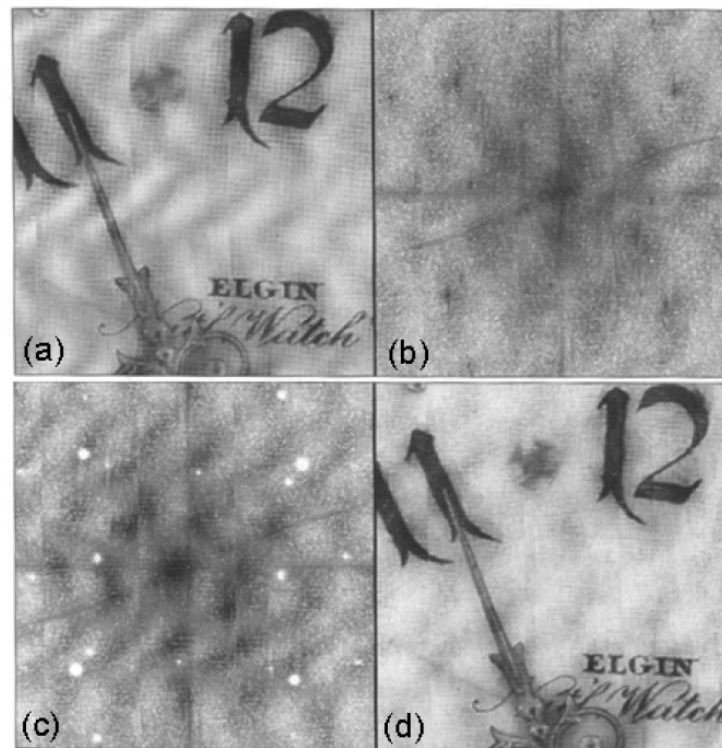


# FFT

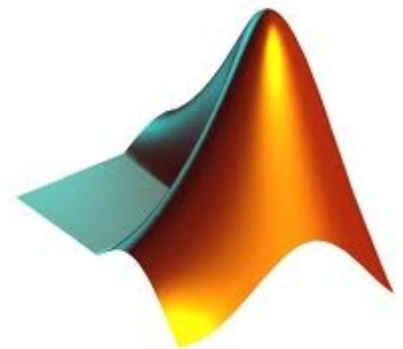
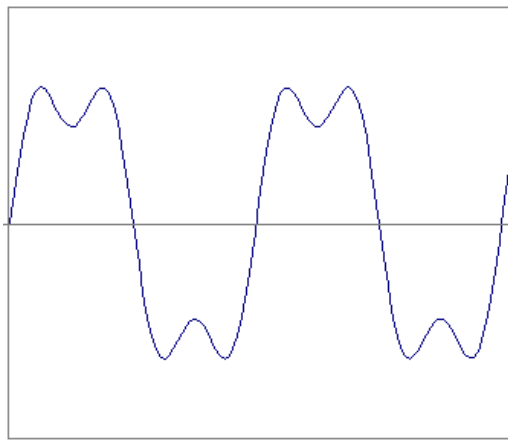
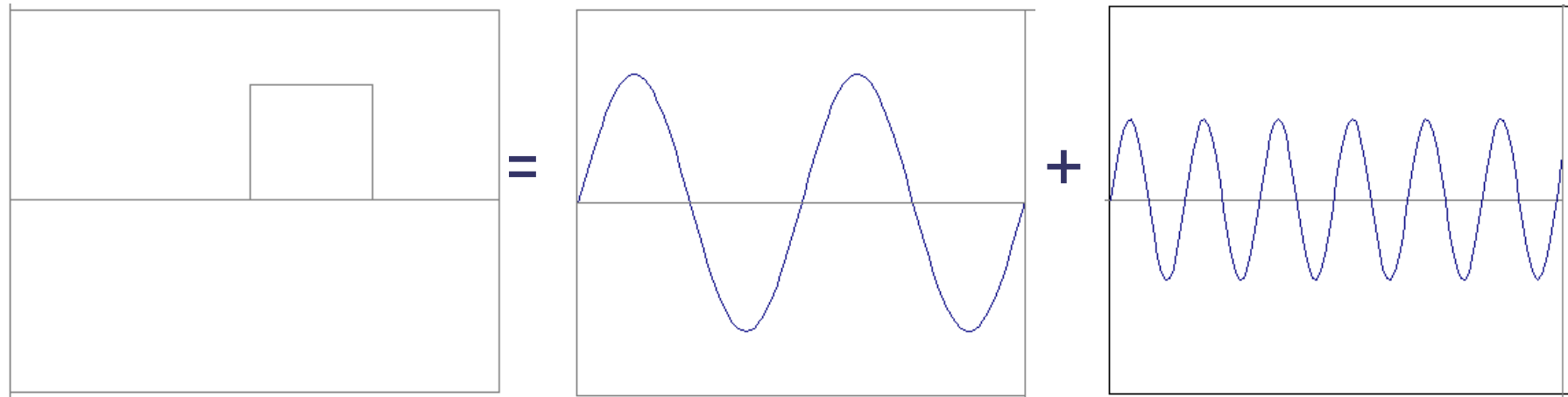
Akákoľvek funkcia  $f(x)$  môže byť vyjadrená ako vážený súčet sínusov a kosínusov

Využitie:

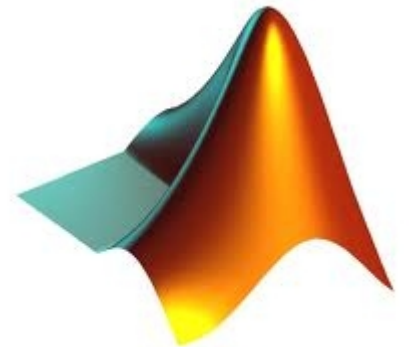
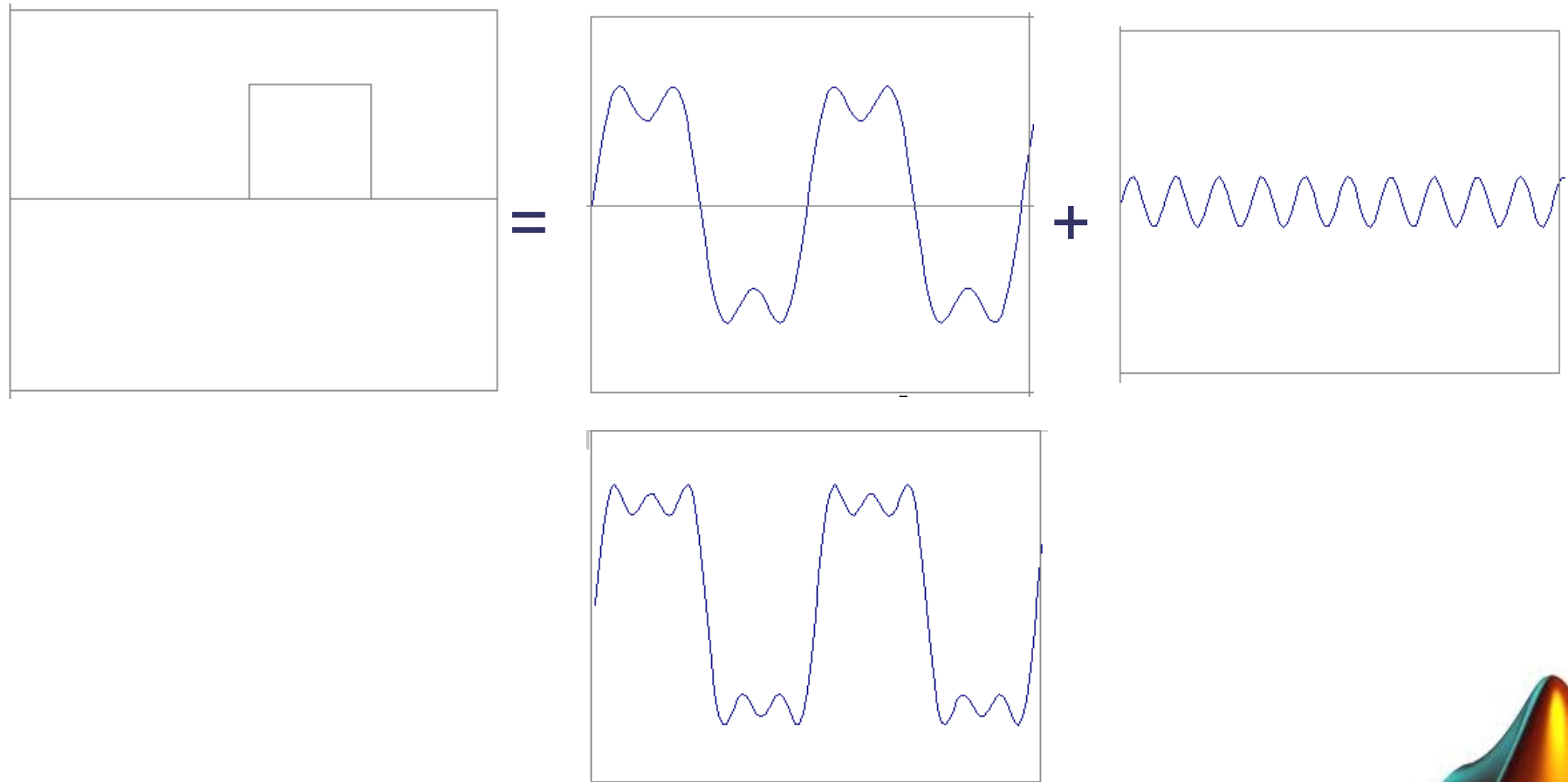
- lowpass filter
- highpass filter
- odstraňovanie artefaktov z obrazu



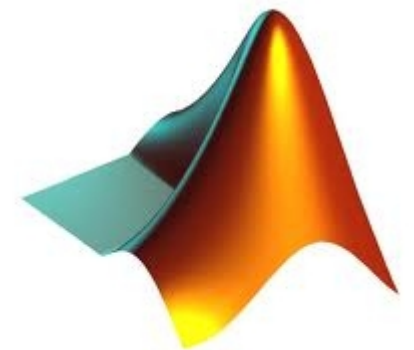
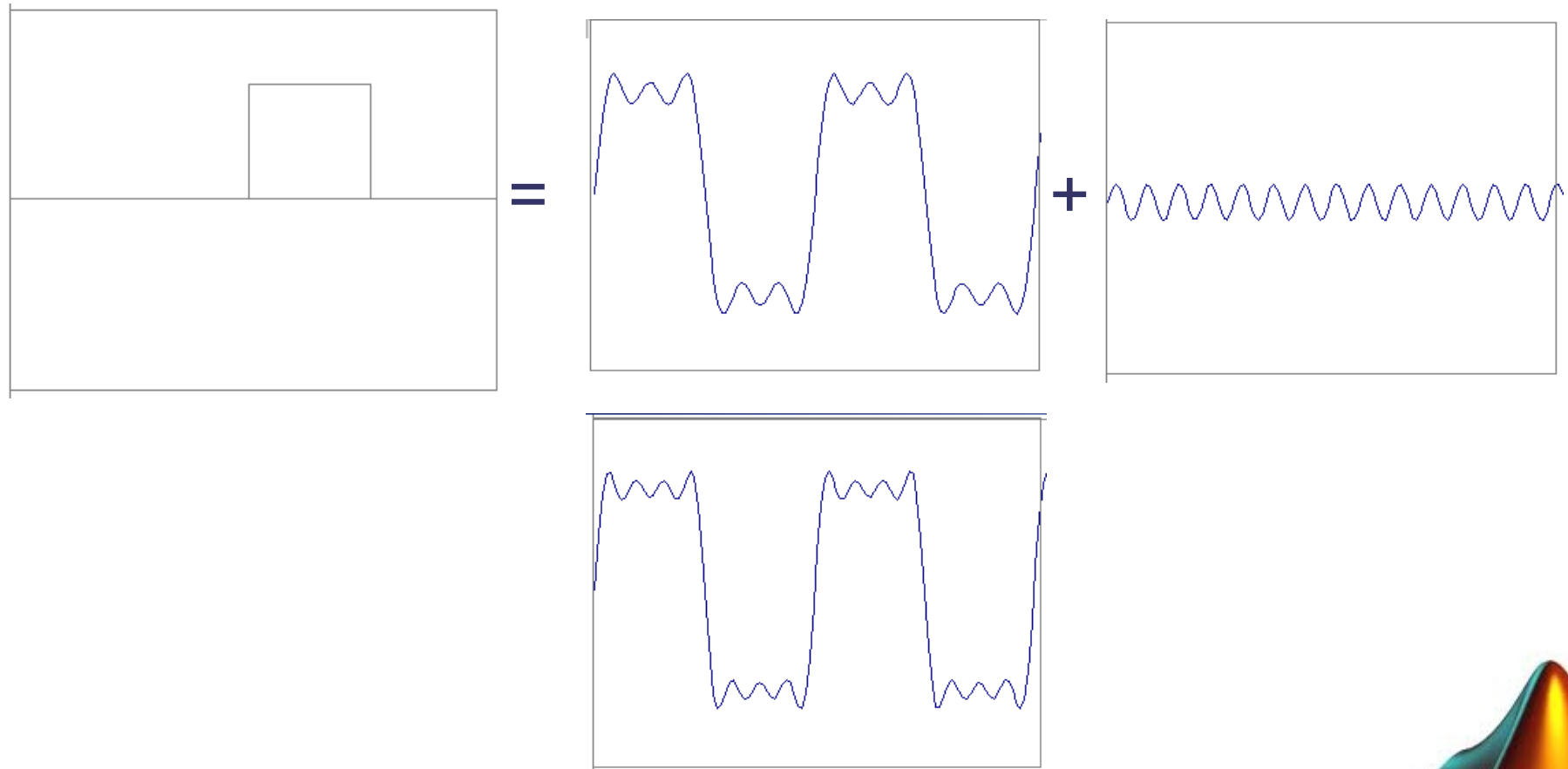
# FFT



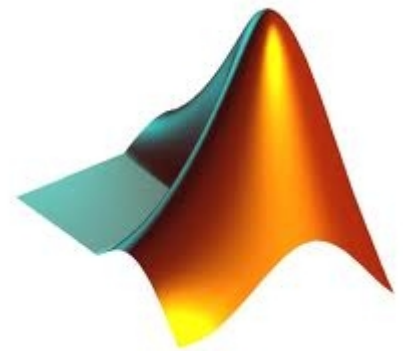
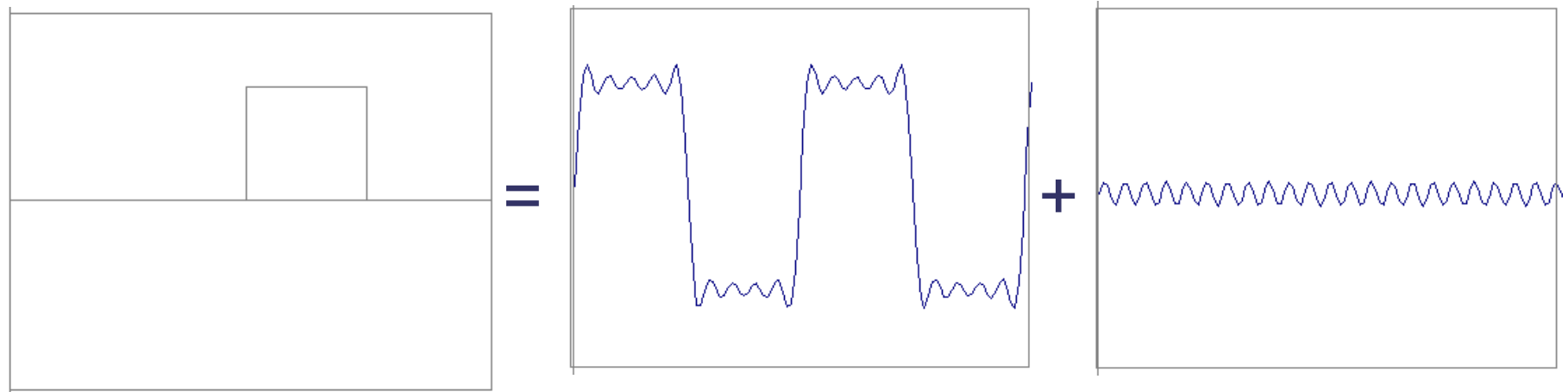
# FFT



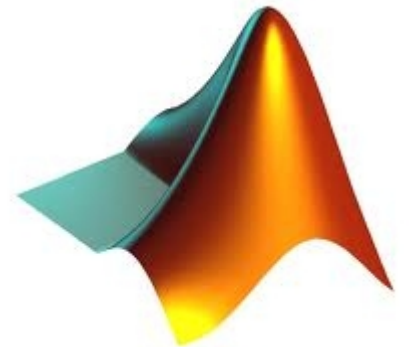
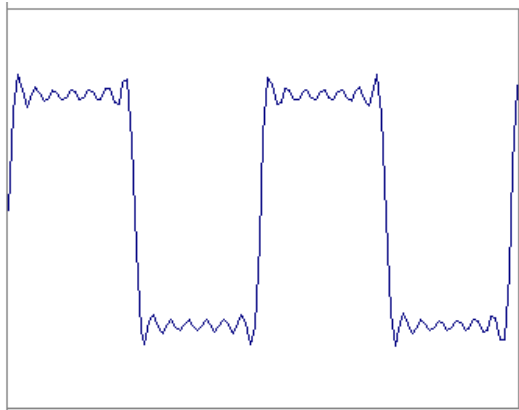
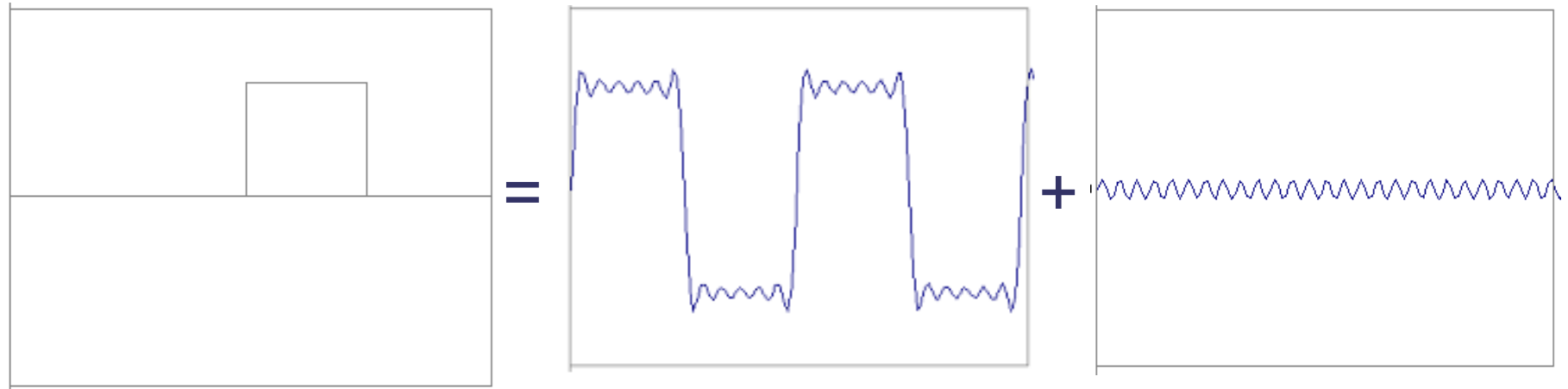
# FFT



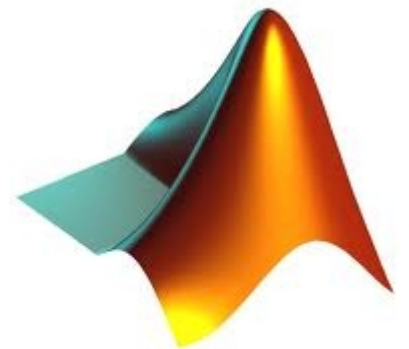
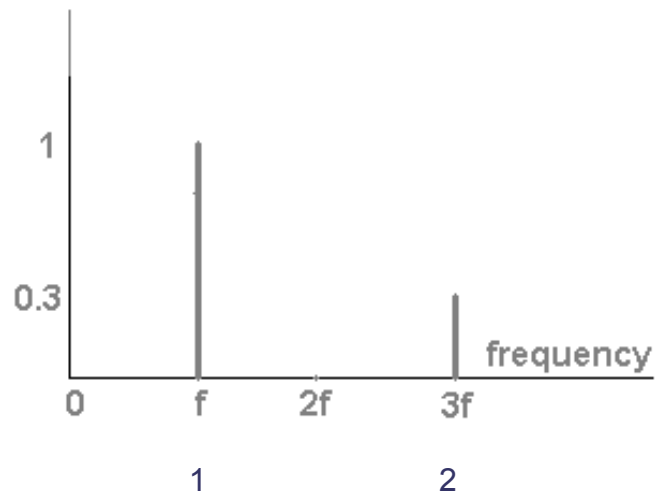
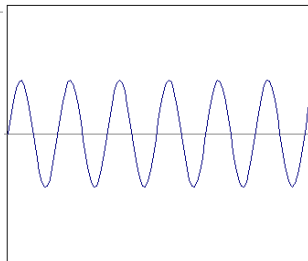
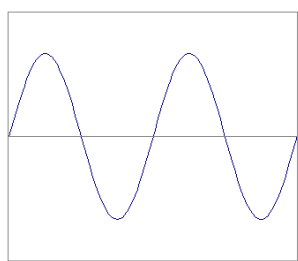
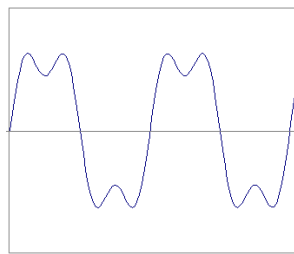
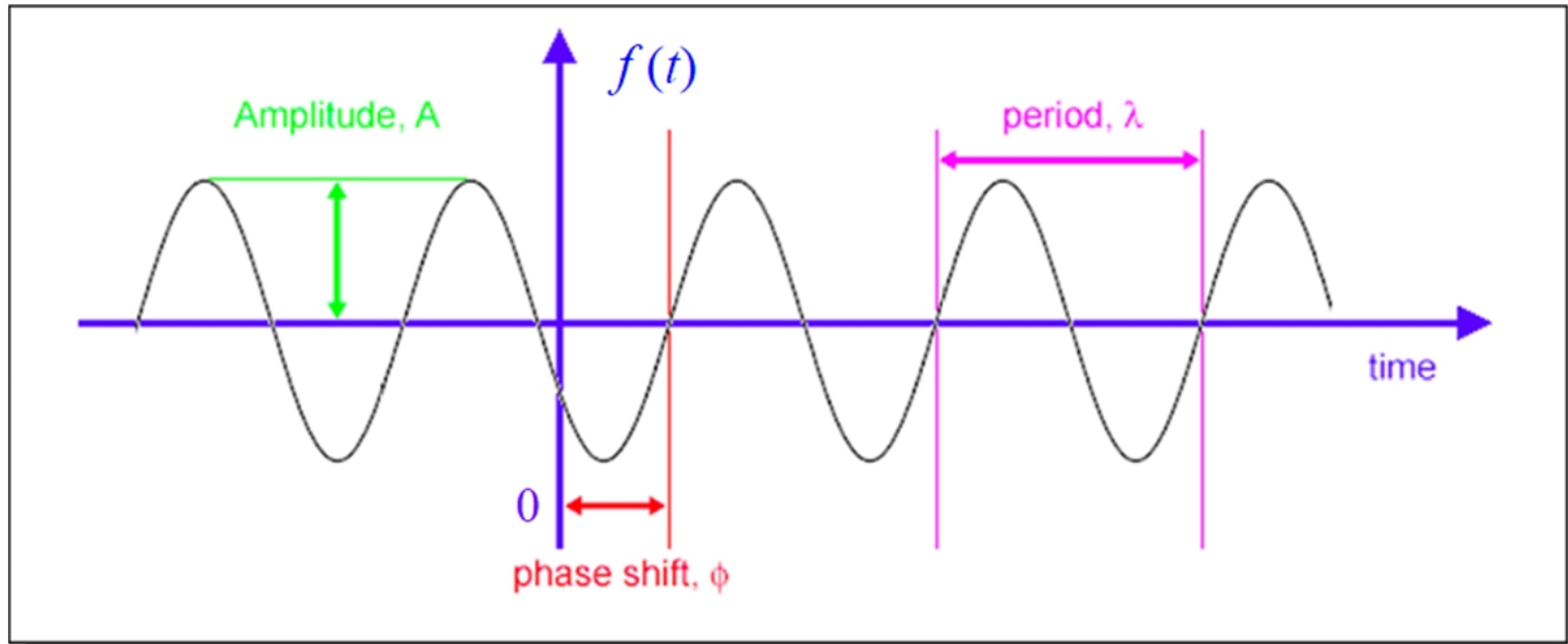
# FFT



# FFT



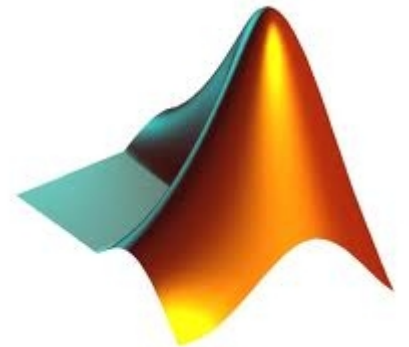
# FFT



# FFT – Skladanie signálu

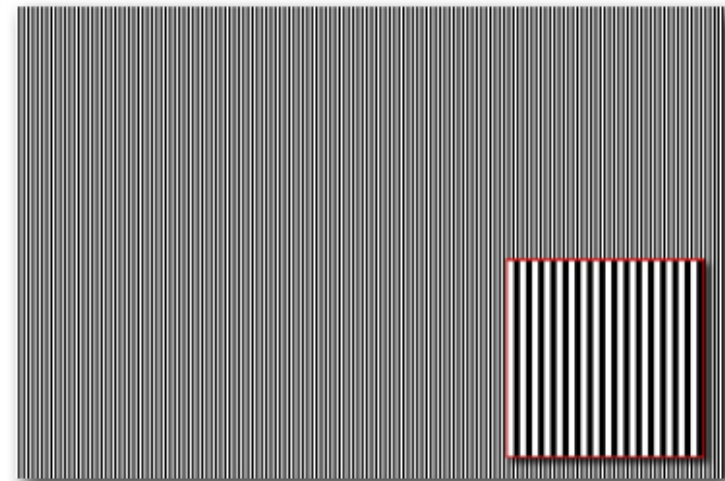
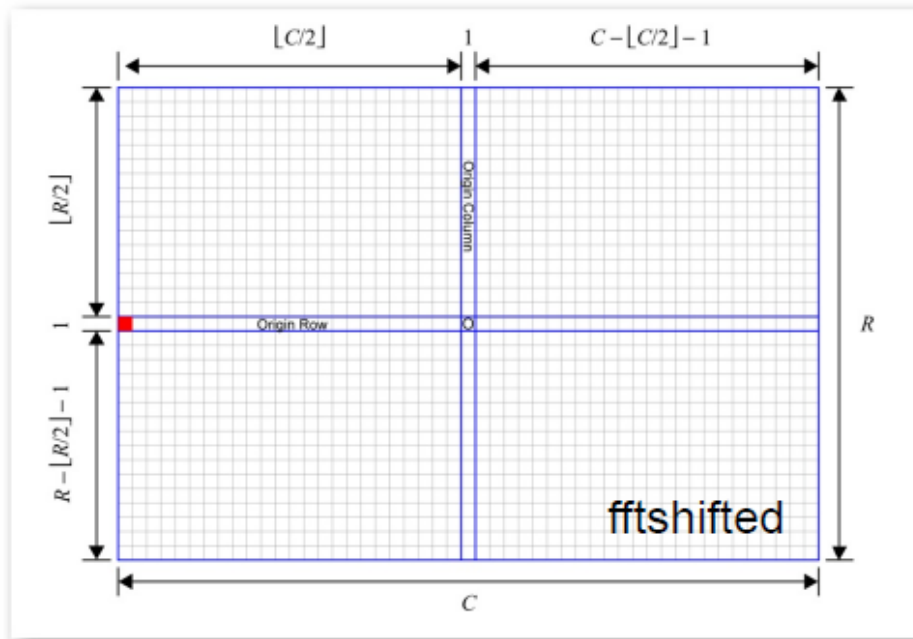
## MATLAB

```
Fs = 1000;           % Sampling frequency
T = 1/Fs;           % Sample time
L = 1000;           % Length of signal
t = (0:L-1)*T;      % Time vector
y1 = 0.9*sin(2*pi*10*t);
y2 = 0.3*sin(2*pi*30*t);
y3 = y1 + y2;
figure, plot(Fs*t(1:200),y1(1:200));
figure, plot(Fs*t(1:200),y2(1:200));
figure, plot(Fs*t(1:200),y3(1:200));
```

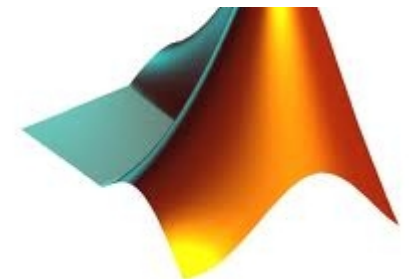


# FFT

"horizontal" is the wavefront direction.

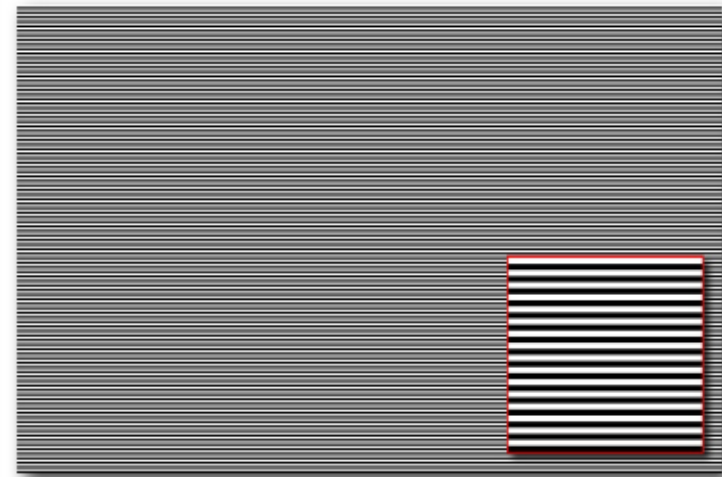
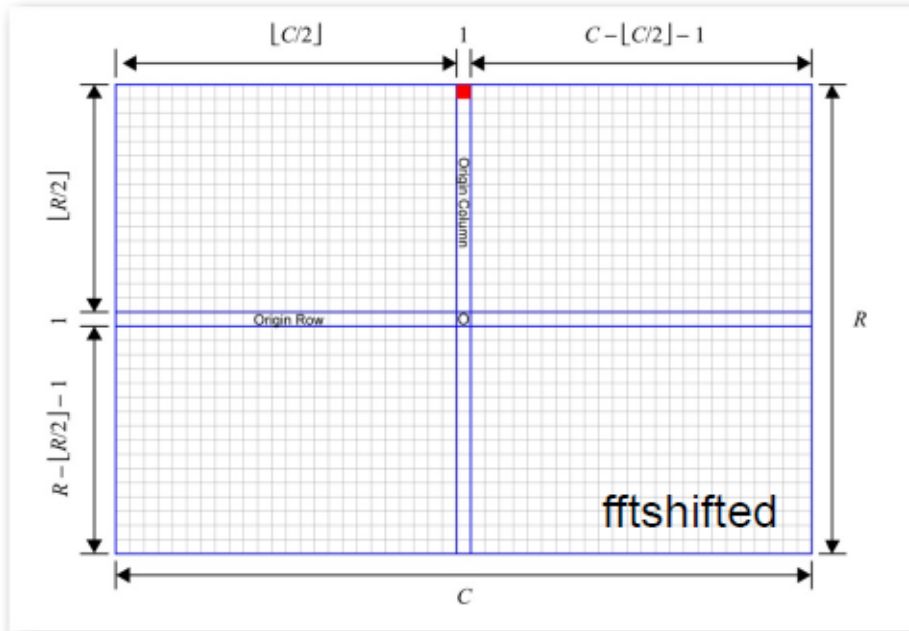


highest-possible-frequency horizontal sinusoid ( $C$  is even)

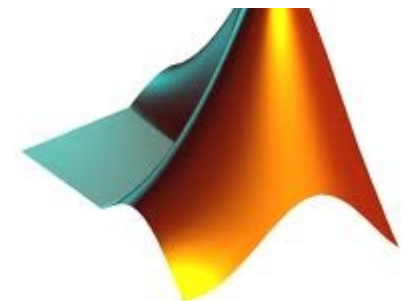


# FFT

"vertical" is the wavefront direction.

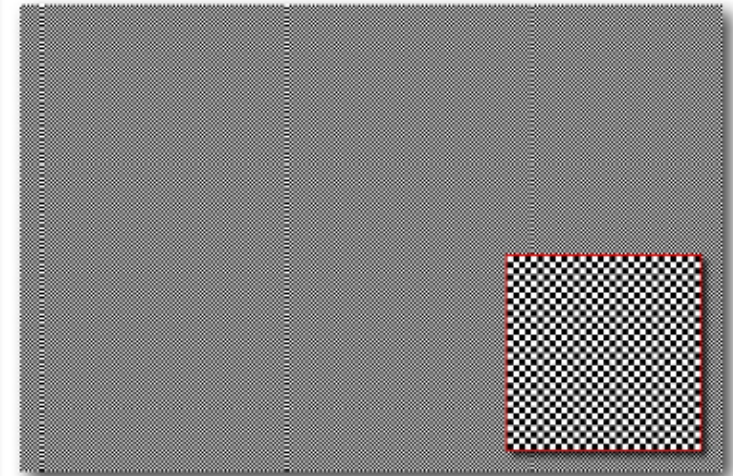
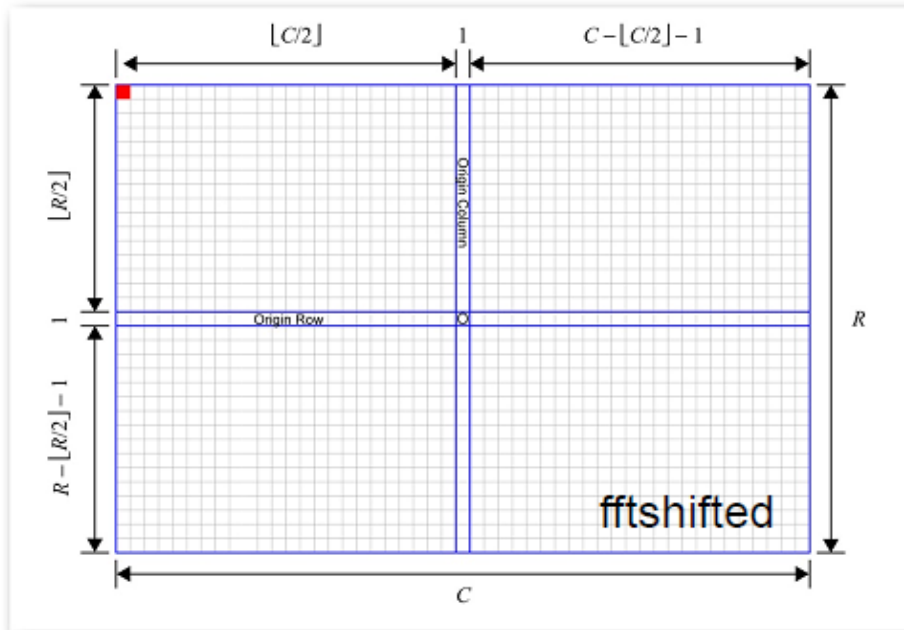


highest-possible-frequency vertical sinusoid ( $R$  is even)

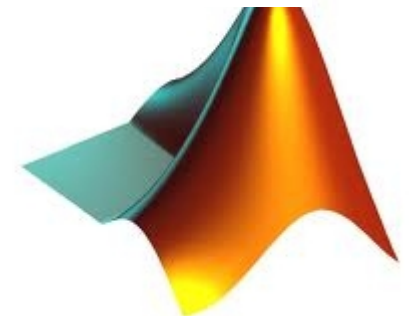


# FFT

a checker-board pattern.

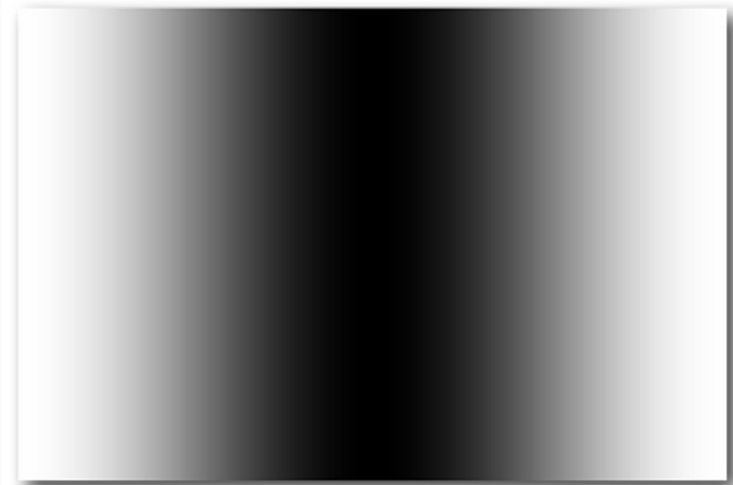
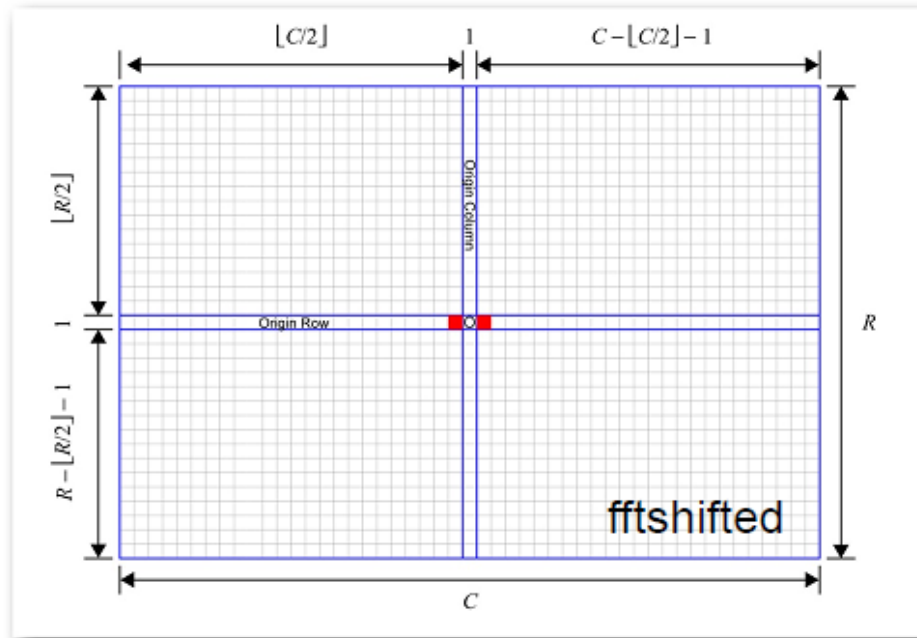


highest-possible-freq horizontal+vertical sinusoid ( $R$  &  $C$  even)

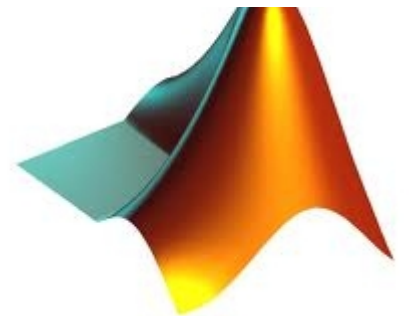


# FFT

"horizontal" is the wavefront direction.

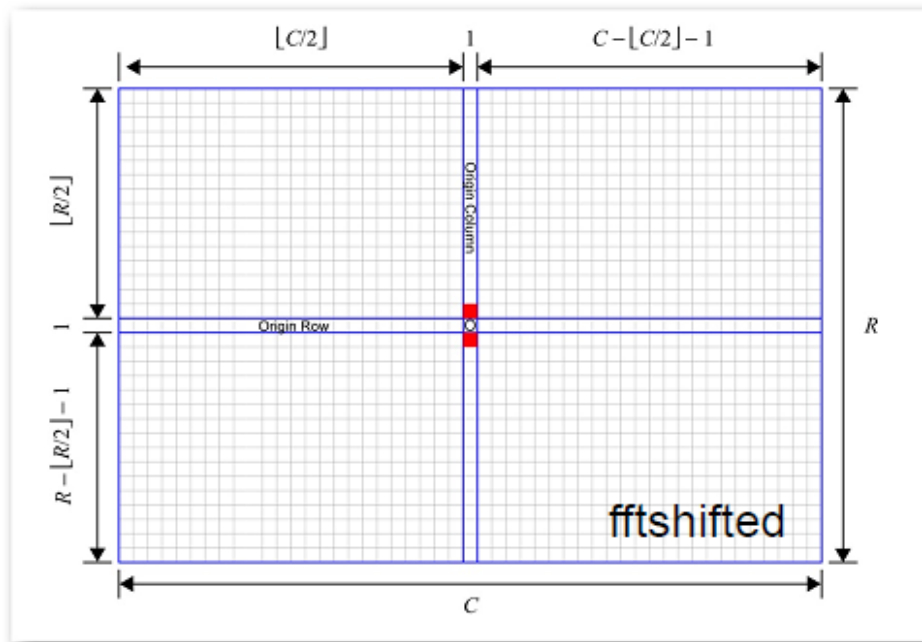


lowest-possible-frequency horizontal sinusoid

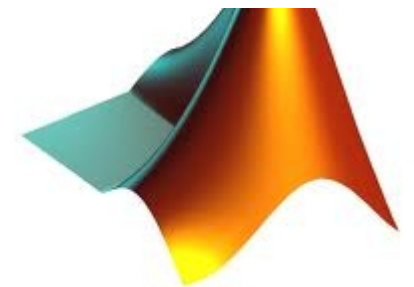


# FFT

"vertical" is the wavefront direction.

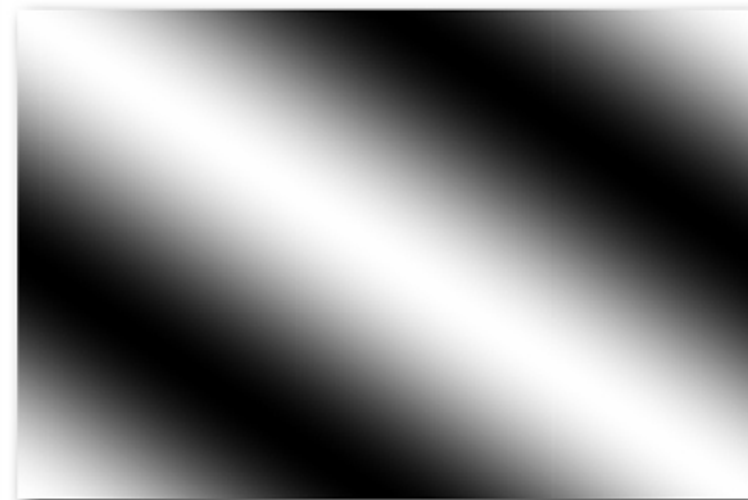
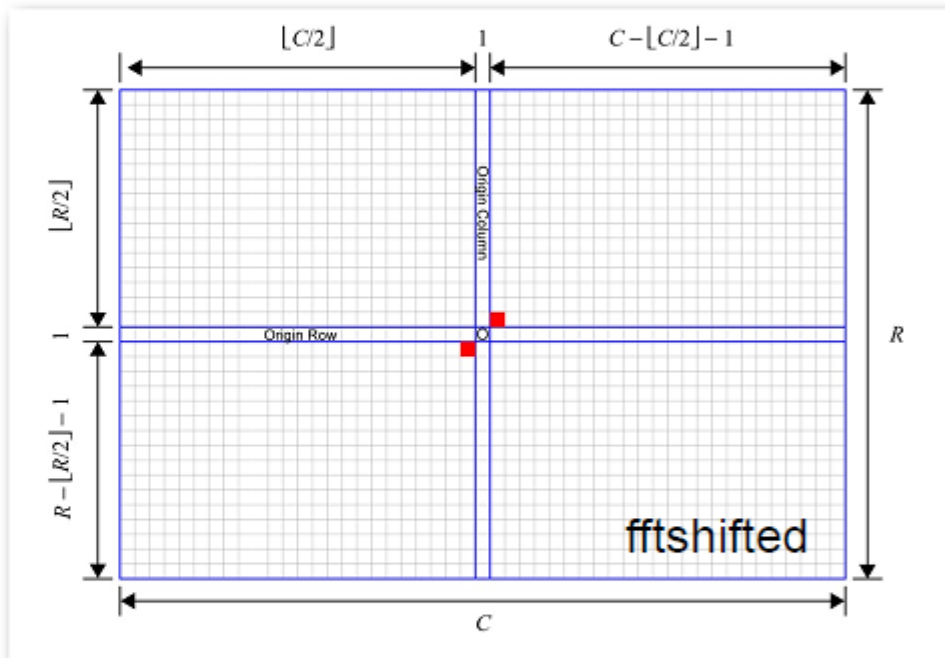


lowest-possible-frequency vertical sinusoid

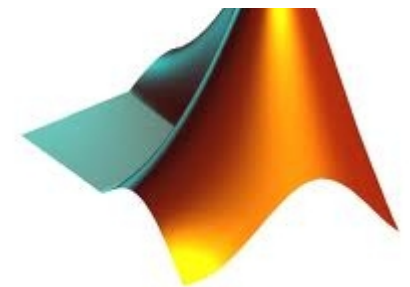


# FFT

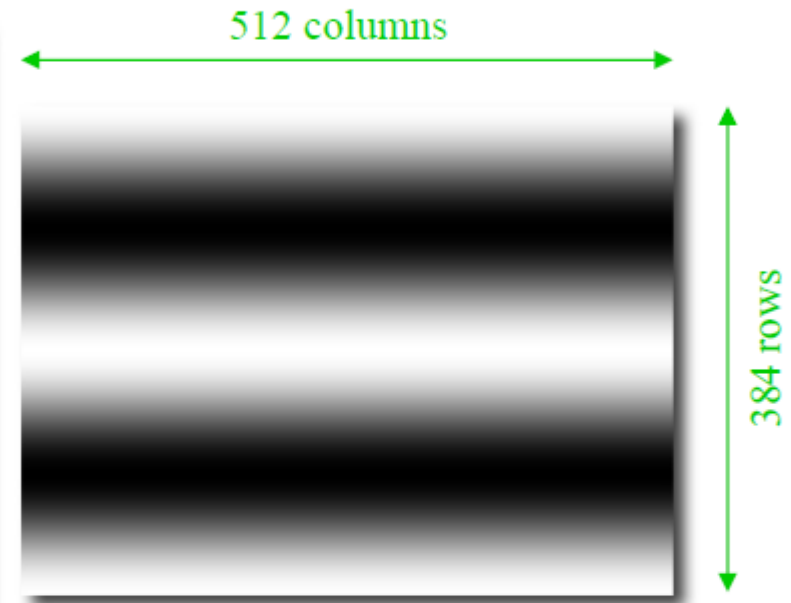
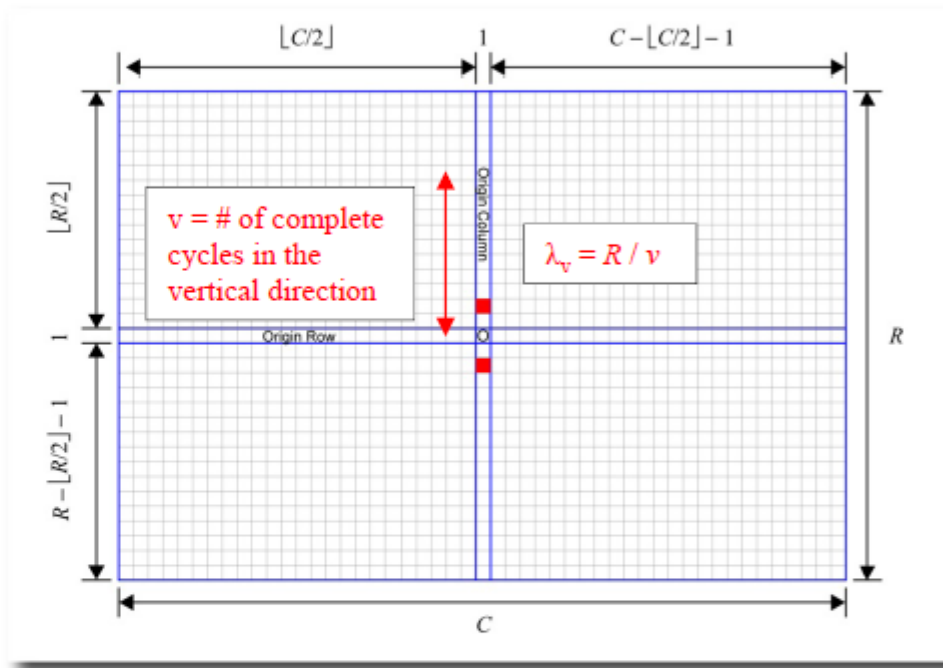
"negative diagonal" is the wavefront direction.



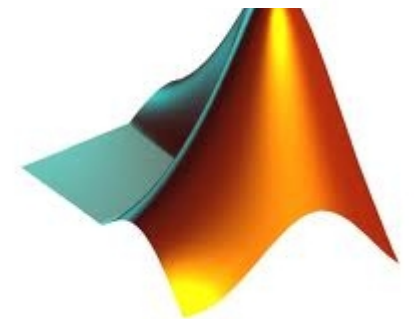
lowest-possible-frequency negative diagonal sinusoid



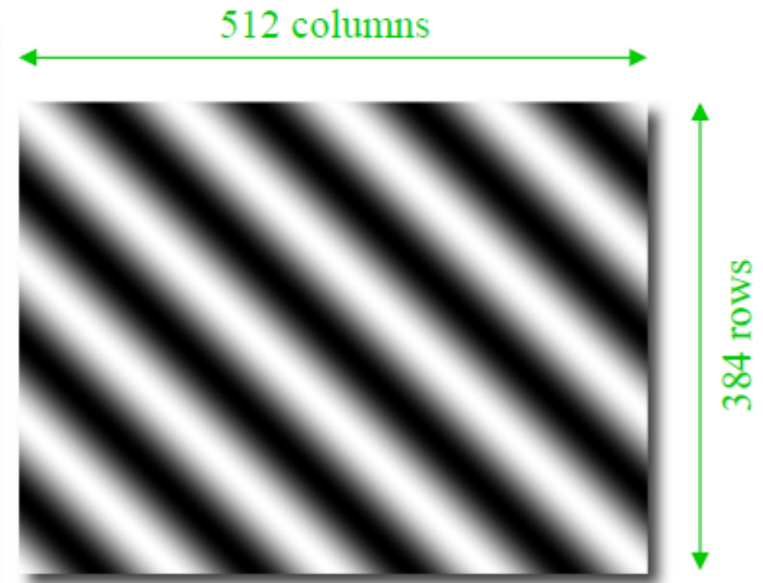
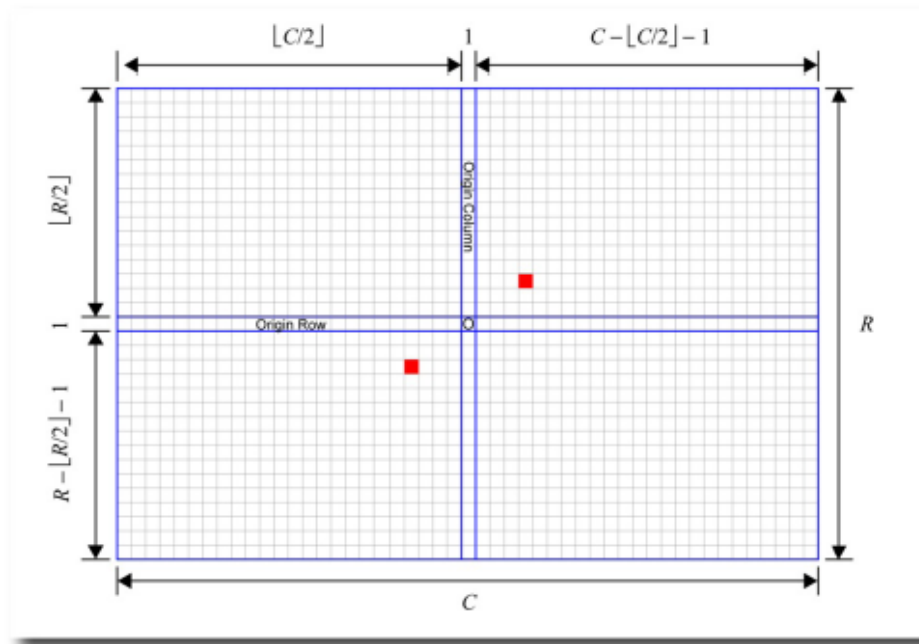
# FFT



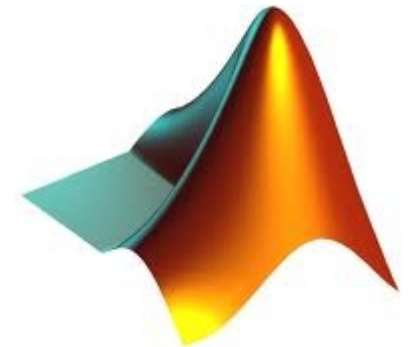
frequencies:  $(u, v) = (0, 2)$ ; wavelength:  $\lambda_v = 192$



# FFT



frequencies:  $(u, v) = (4, 3)$ ; wavelengths:  $(\lambda_u, \lambda_v) = (128, 128)$



# FFT

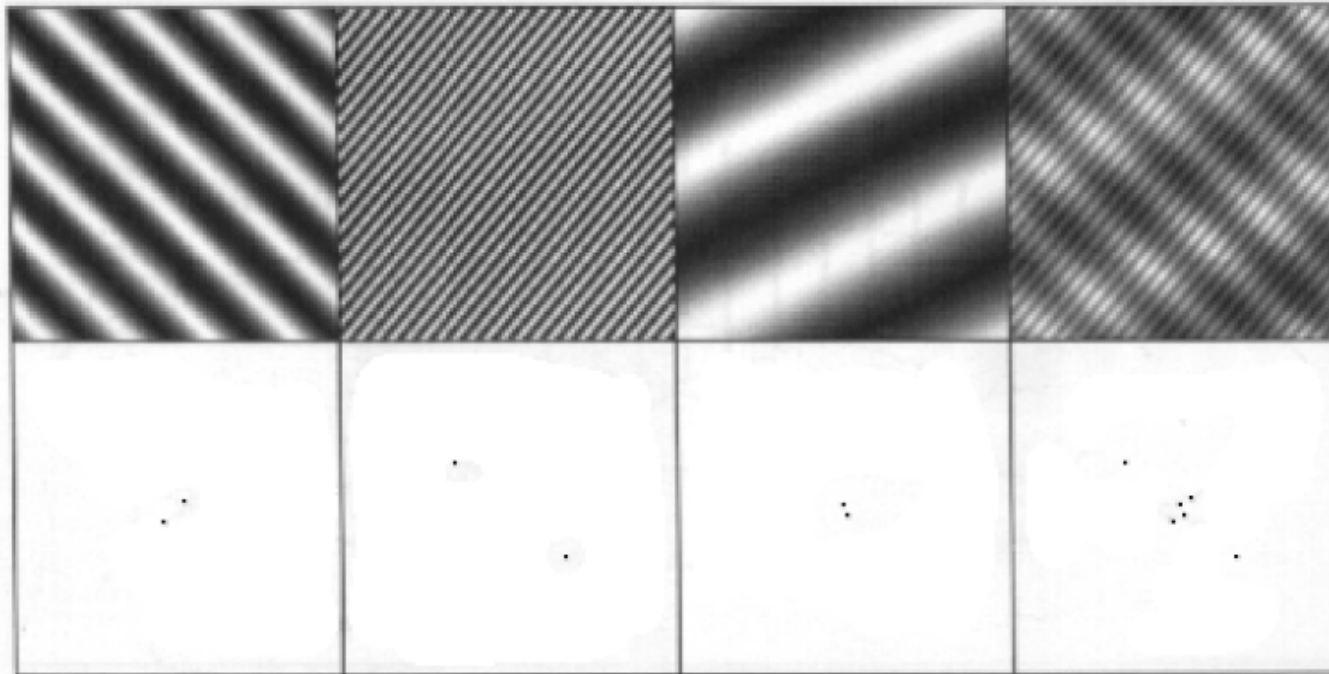
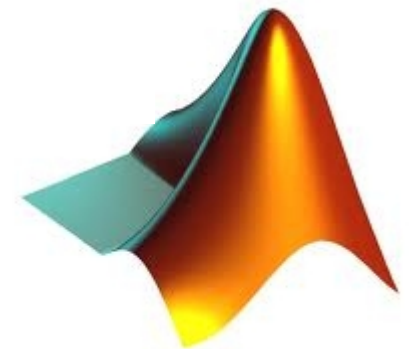
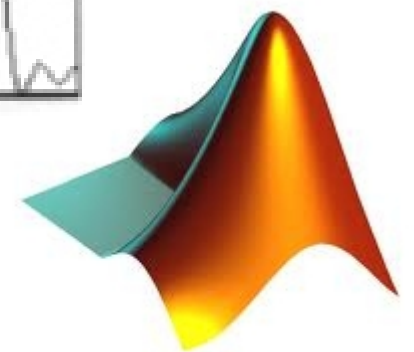
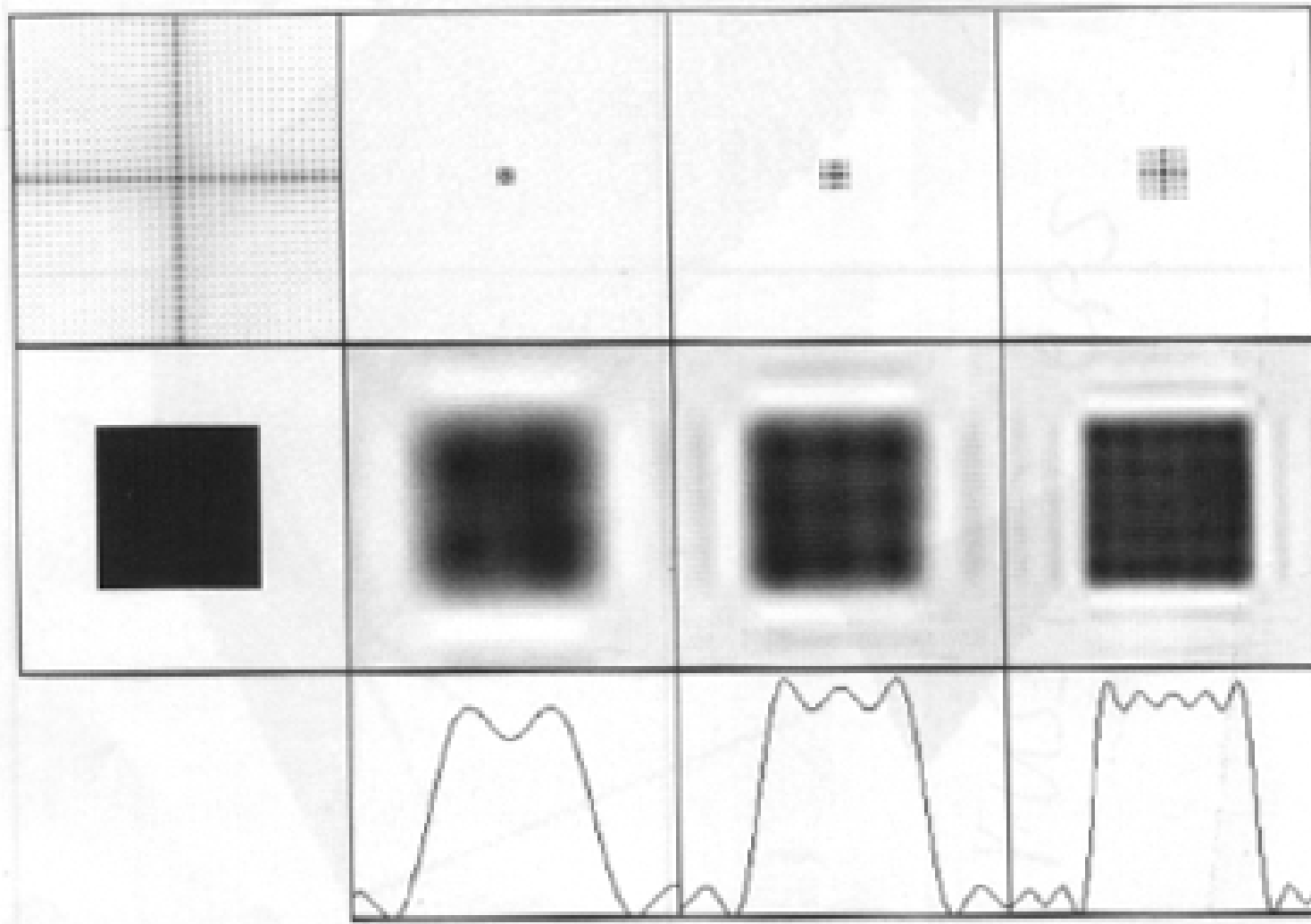


Figure 2: Images with perfectly sinusoidal variations in brightness: The first three images are represented by two dots. You can easily see that the position and orientation of those dots have something to do with what the original image looks like. The 4th image is the sum of the first three.

(Taken from p.177 of [1].)



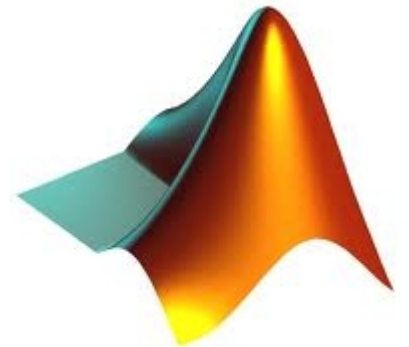
# FFT



# FFT MATLAB

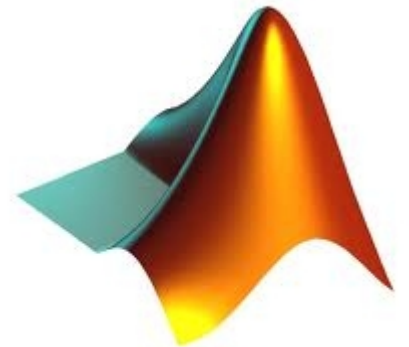
## 2-D Fast Fourier transform

```
PS = fftshift(log(abs(fft2(I))+1));  
M = max(PS(:));  
image(uint8(255*(PS/M)));
```



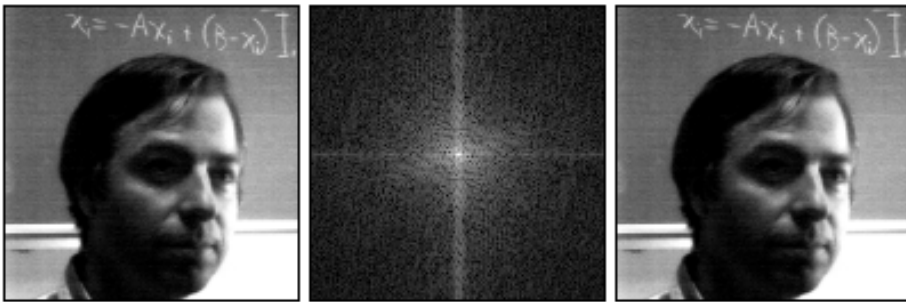
# FFT ImageJ

- Image Processing and Analysis in Java
- Vytvorený v Jave – umožňuje ho spustiť na všetkých OS
- Open Source
- <http://rsbweb.nih.gov/ij/>

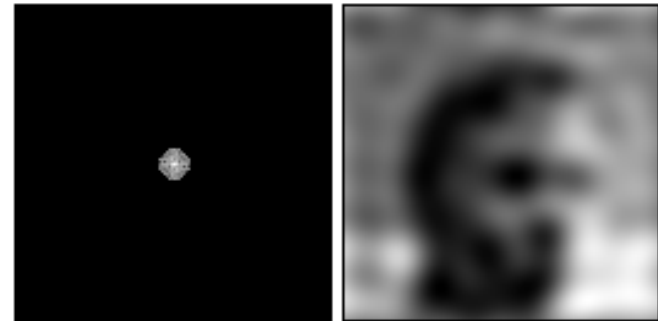


# FFT ImageJ

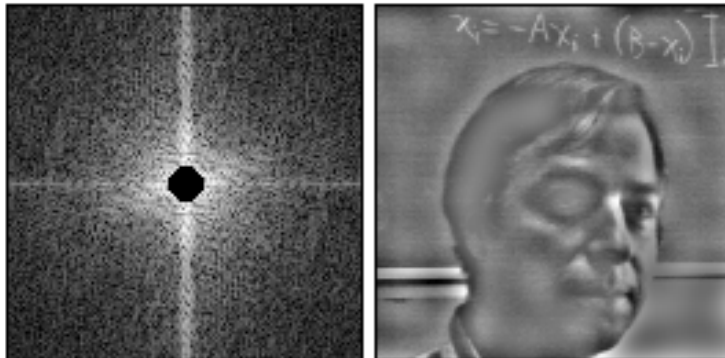
**Brightness Image    Fourier Transform    Inverse Transformed**



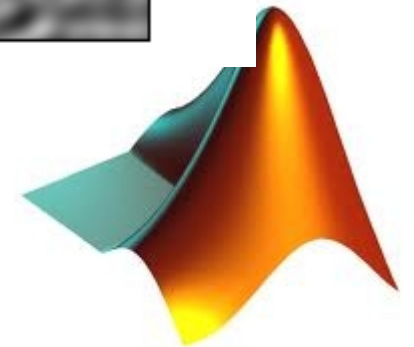
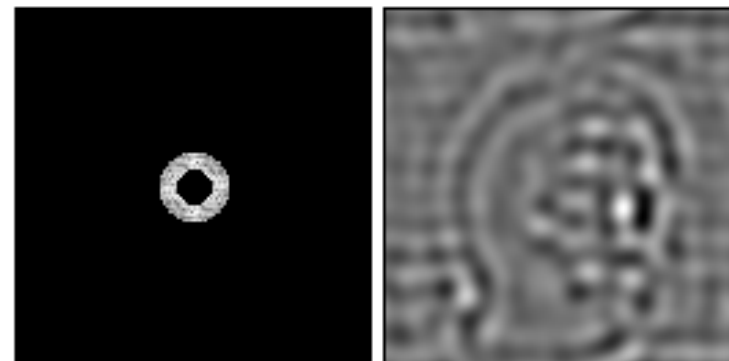
**Low-Pass Filtered    Inverse Transformed**



**High-Pass Filtered    Inverse Transformed**



**Band-Pass Filtered    Inverse Transformed**



# DCT

- pre typický obrázok so spojitými prechodmi farieb je väčšina vizuálne najdôležitejších informácií o obrázku koncentrovaná v malom počte kosínusových funkcií nízkych frekvencií
- frekvenčné koeficienty sú reálne

$A = \text{dct2}(B);$

$B = \text{idct2}(A);$

<http://www.mathworks.com/help/toolbox/images/ref/dct2.html>

