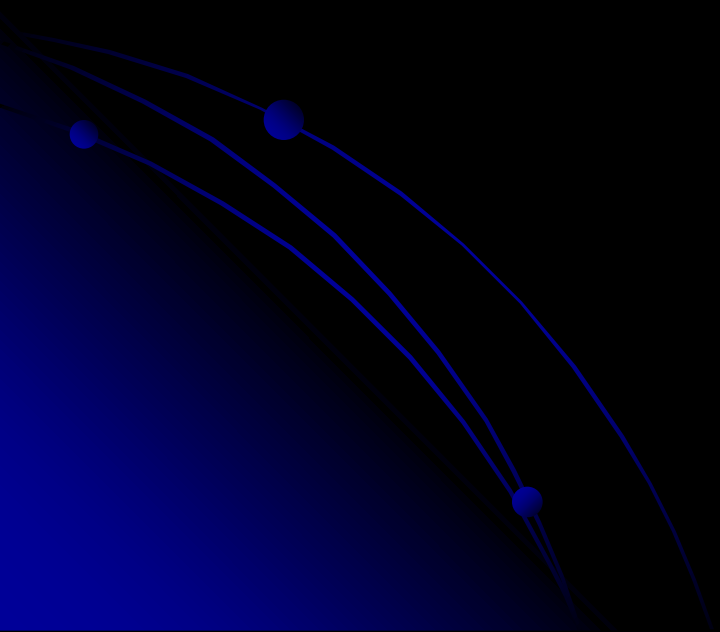
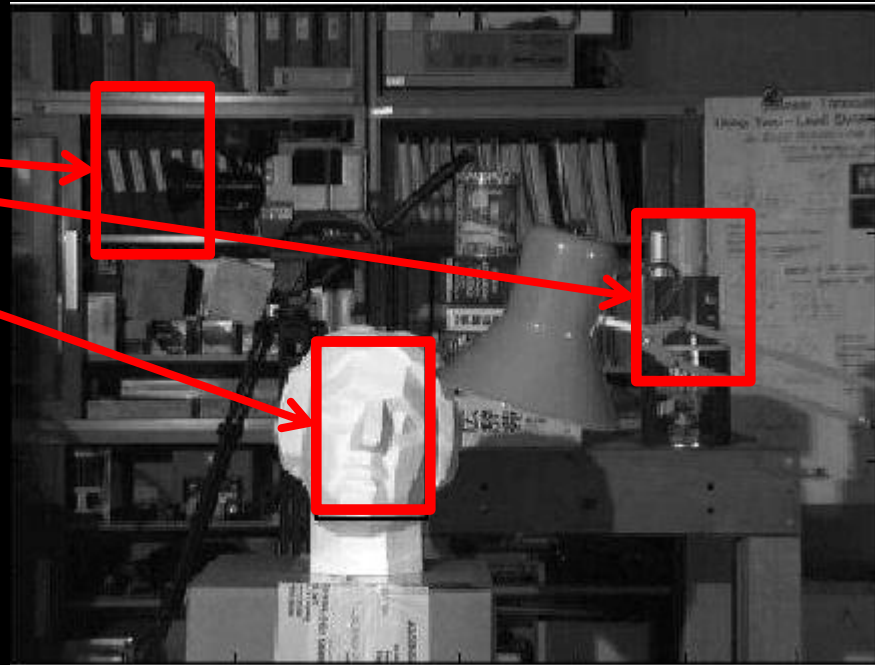


Hľadanie objektov



Prikladanie šablón



$M \times N$ obraz

$P \times Q$ šablóna

$O(MNPQ)$

Ak nepoznáme škálu šablóny, ešte horšie

Nájdí  v obraze

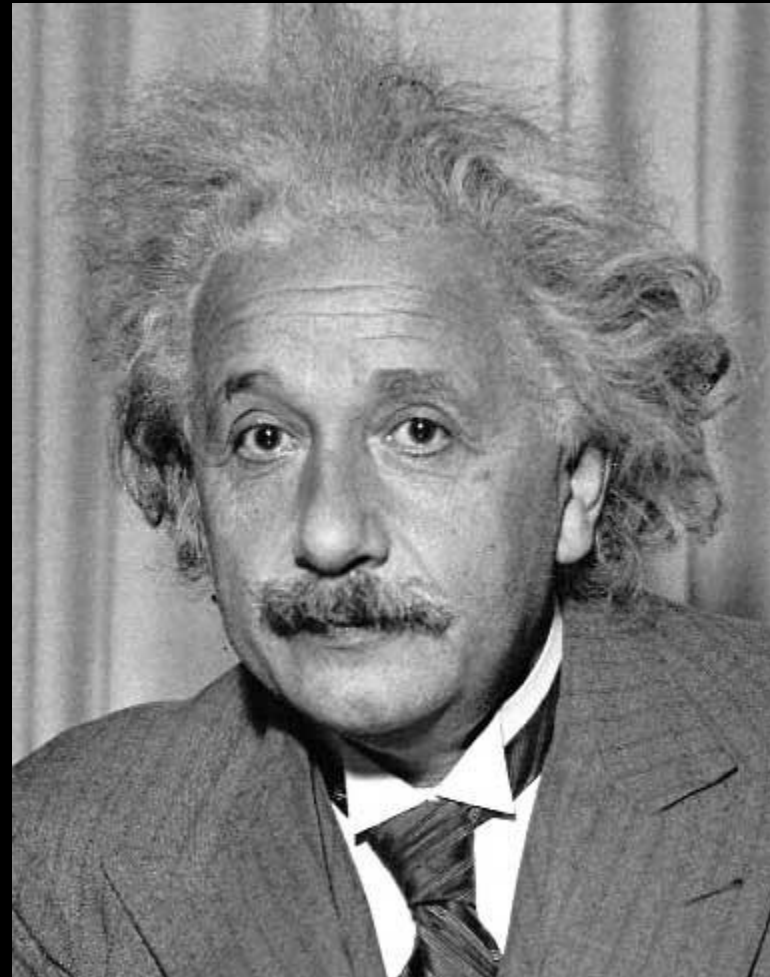
Ktorú mieru podobnosti
použiť?

Korelácia

Korelácia s nulovým
priemerom

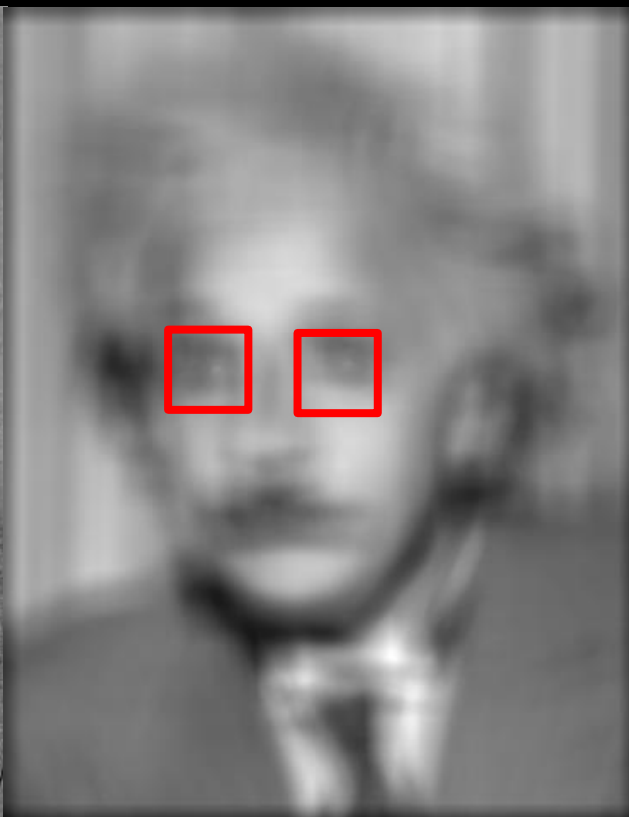
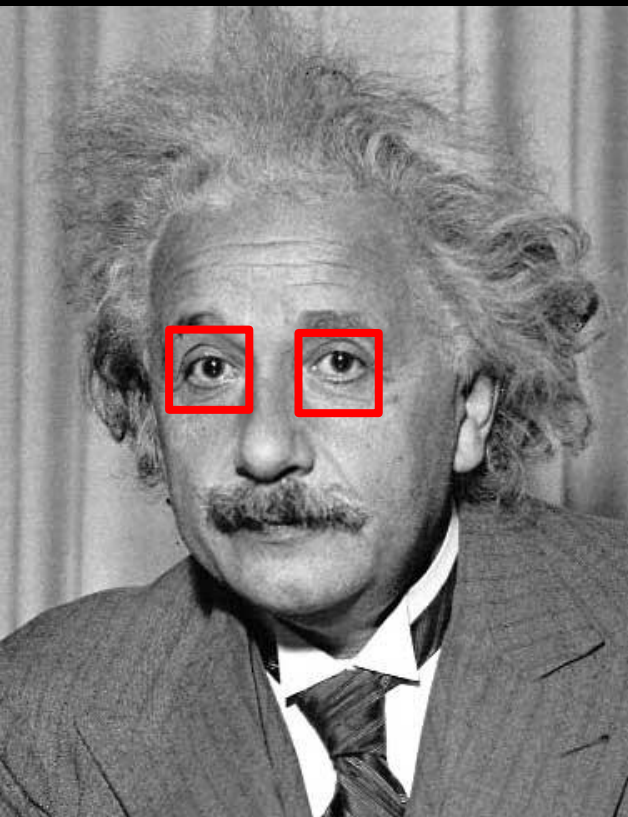
Suma štvorcov vzdialeností

Normalizovaná korelácia



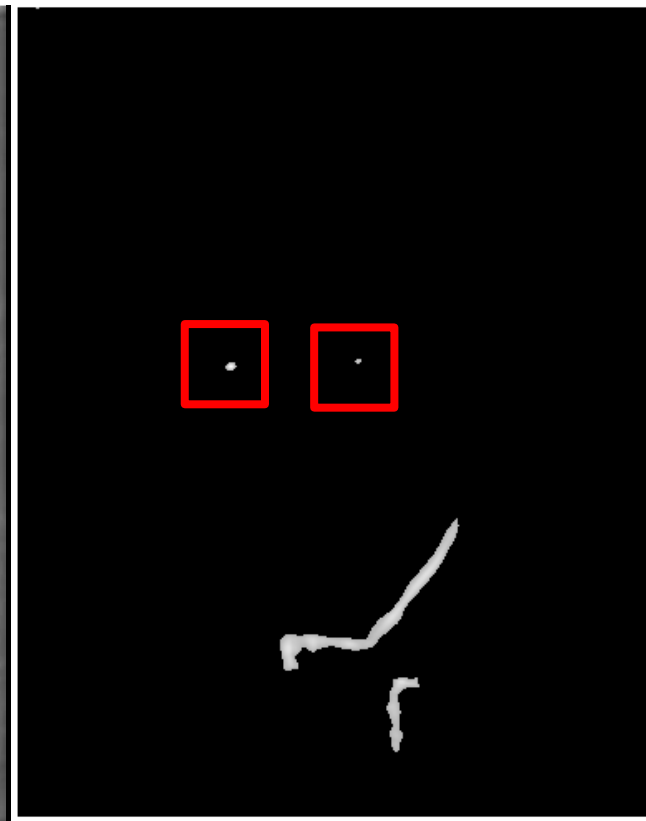
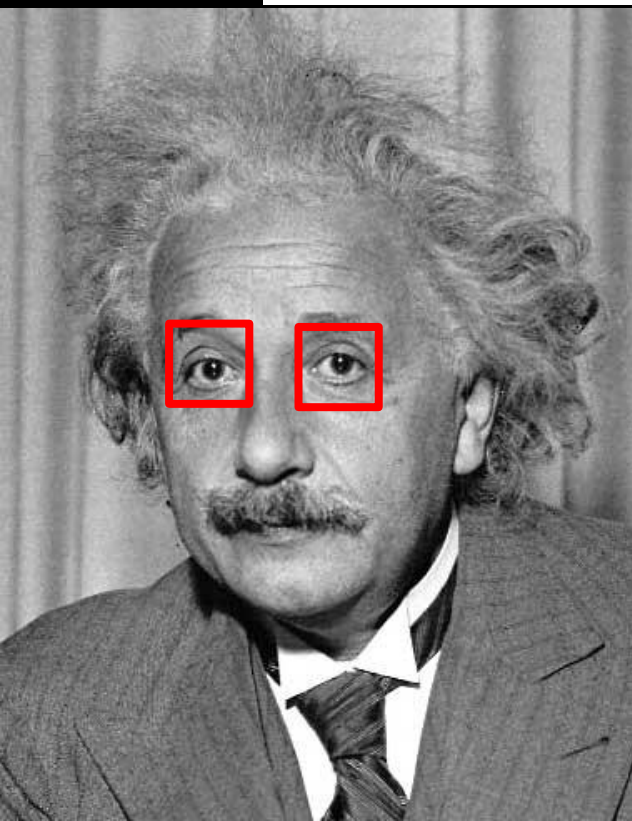
Korelácia

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$



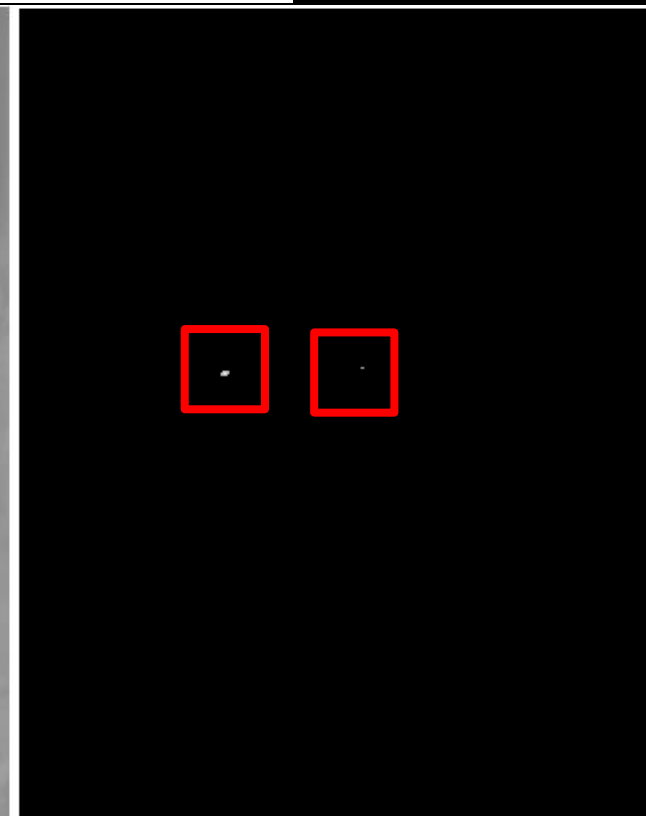
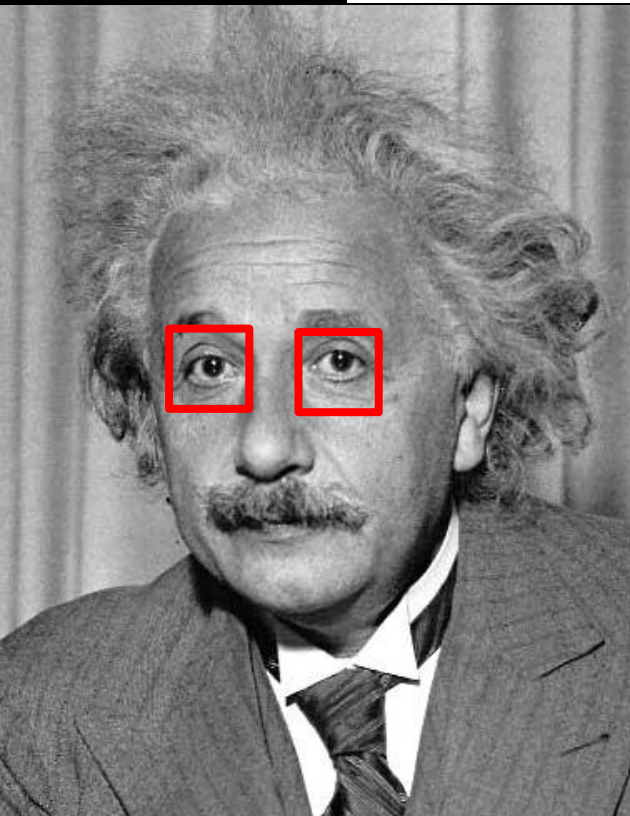
Korelácia s nulovým priemerom

$$h[m,n] = \sum_{k,l} (g[k,l] - \bar{g}) (f[m+k, n+l])$$

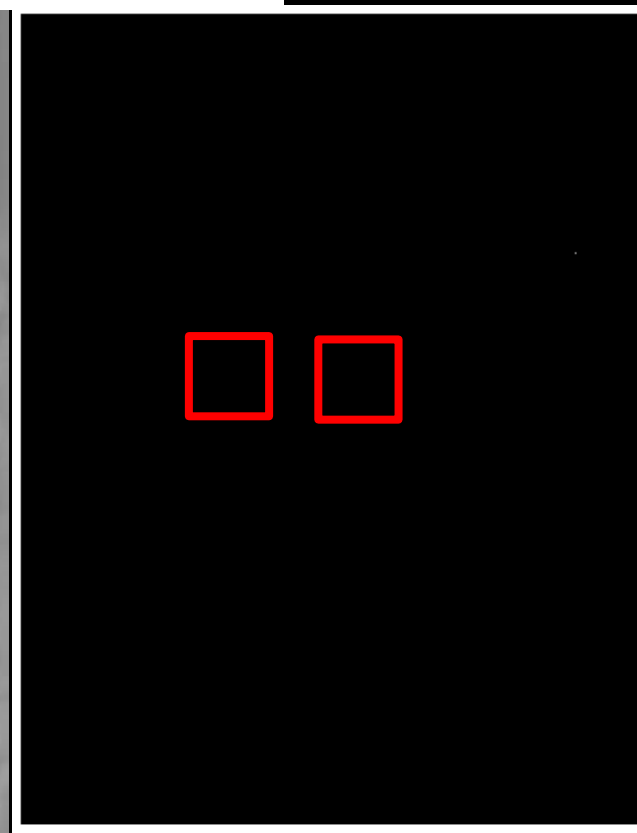
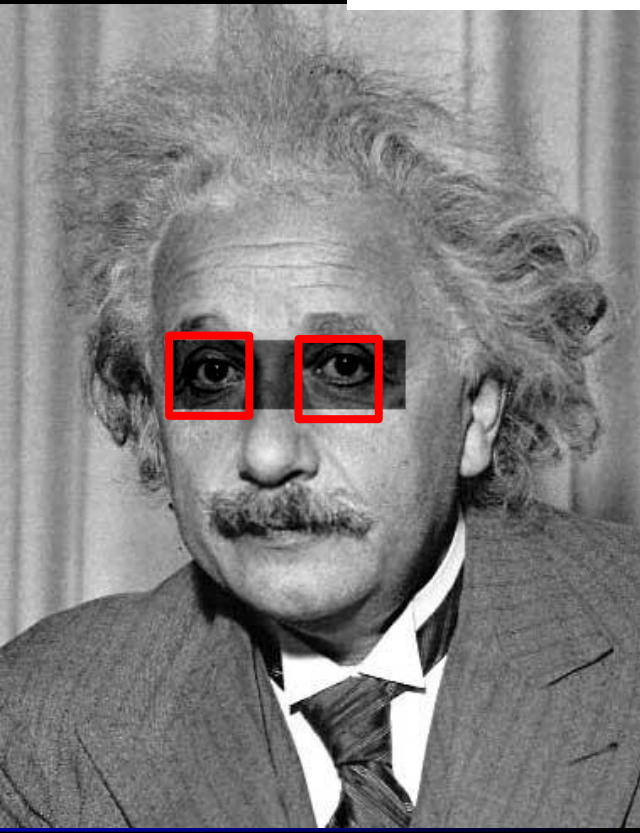


Suma štvorcov vzdialeností

$$h[m,n] = \sum_{k,l} (g[k,l] - f[m+k,n+l])^2$$

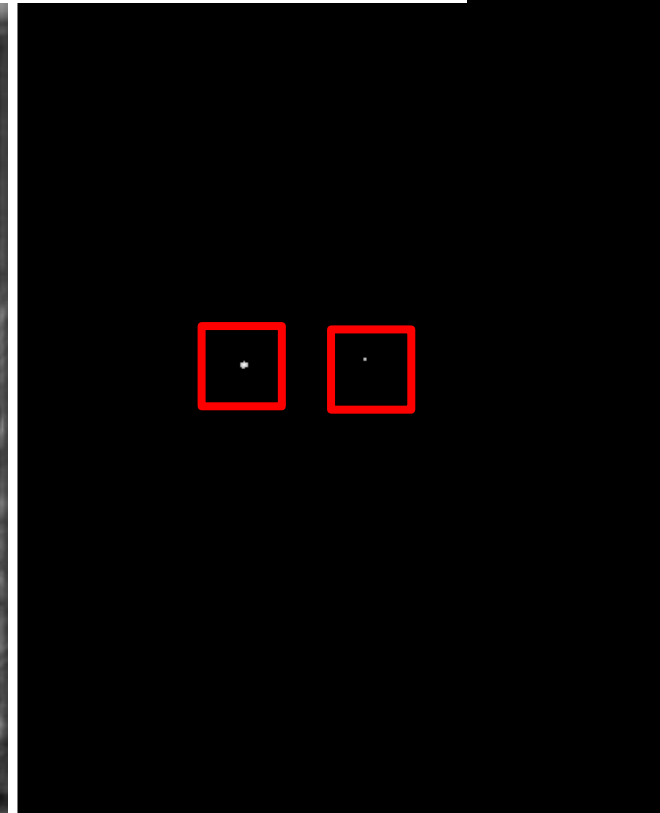
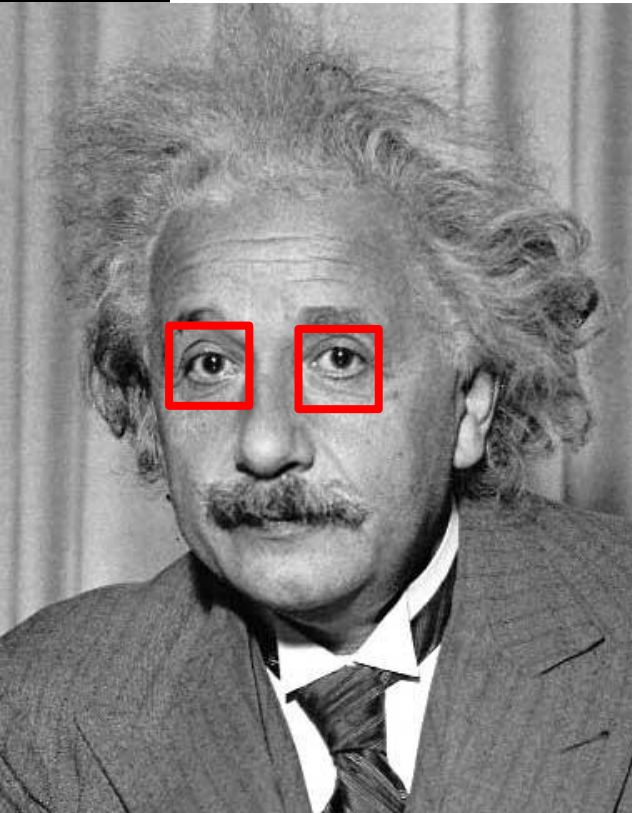


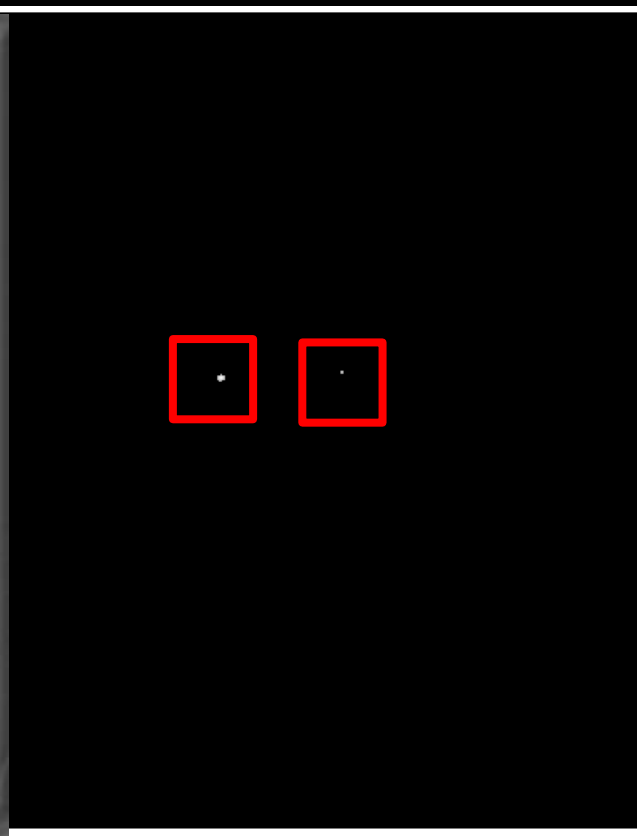
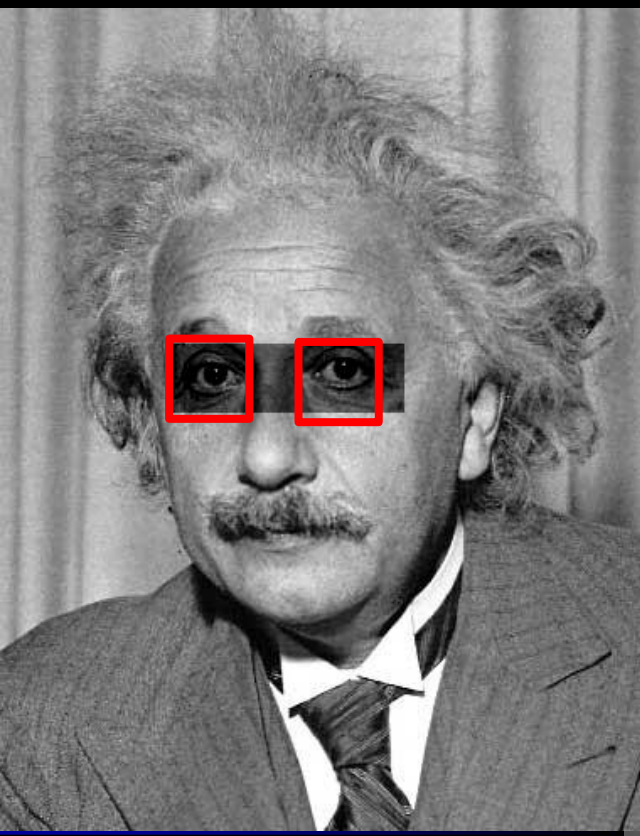
$$h[m,n] = \sum_{k,l} (g[k,l] - f[m+k,n+l])^2$$



Normalizovaná korelácia

$$h[m, n] = \frac{\sum_{k,l} (g[k, l] - \bar{g})(f[m + k, n + l] - \bar{f}_{m,n})}{\left(\sum_{k,l} (g[k, l] - \bar{g})^2 \sum_{k,l} (f[m + k, n + l] - \bar{f}_{m,n})^2 \right)^{0.5}}$$





Ktorú mieru podobnosti použiť?

Korelácia – rýchla, znásobuje intenzity,
nevhodná

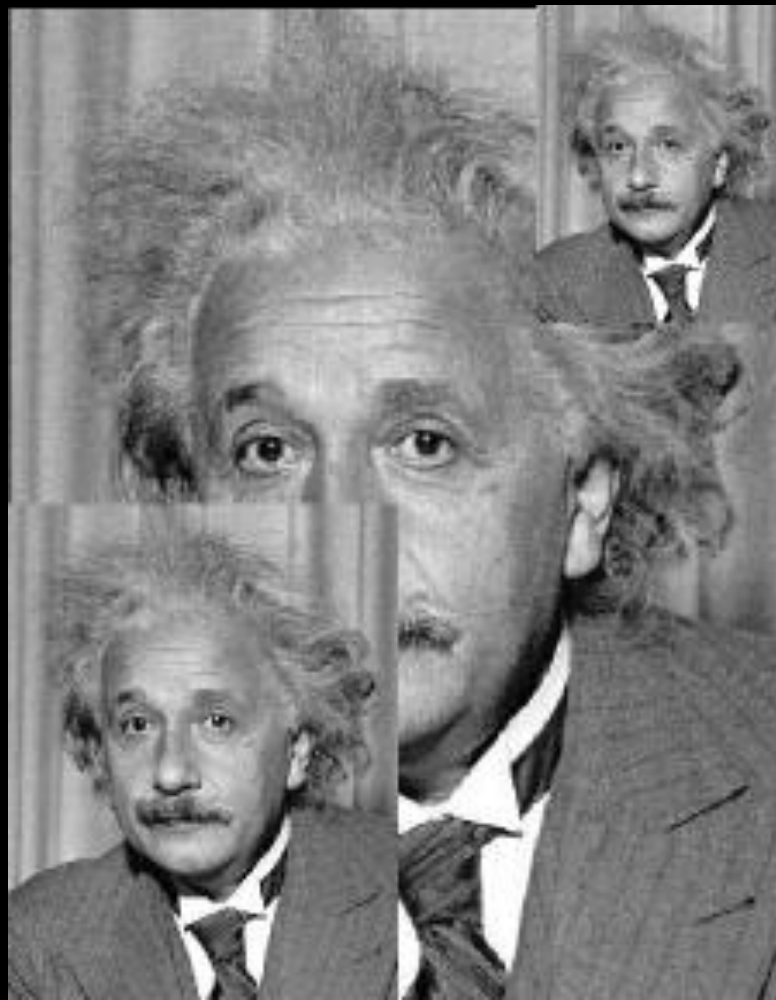
Korelácia s nulovým priemerom – rýchla,
deteguje aj falošné výskyty

- Suma štvorcov vzdialeností – pomalšia, citlivá
na zmenu intenzity

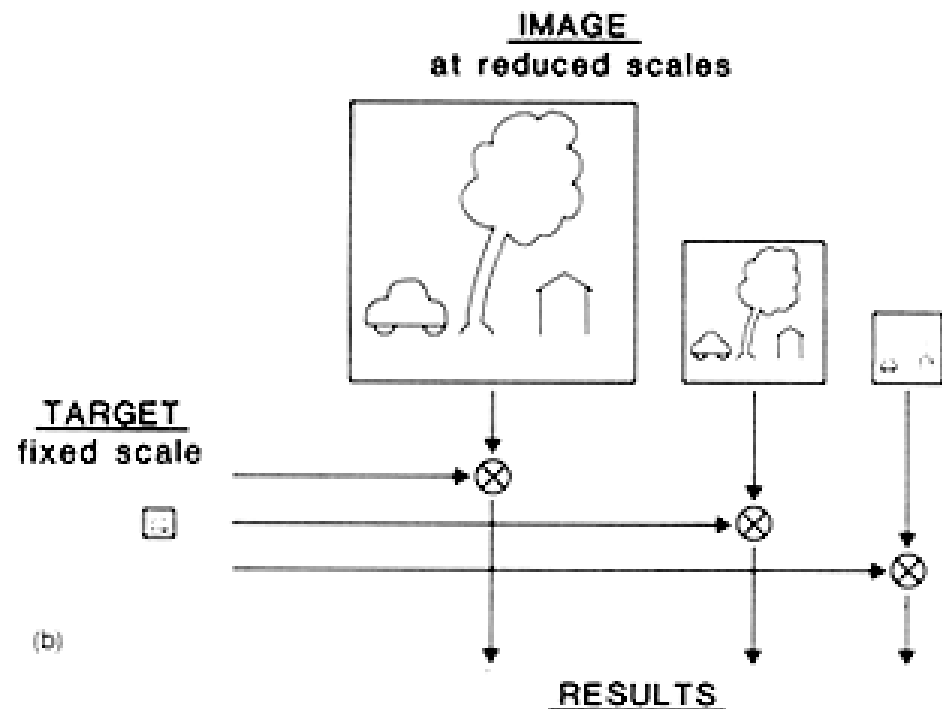
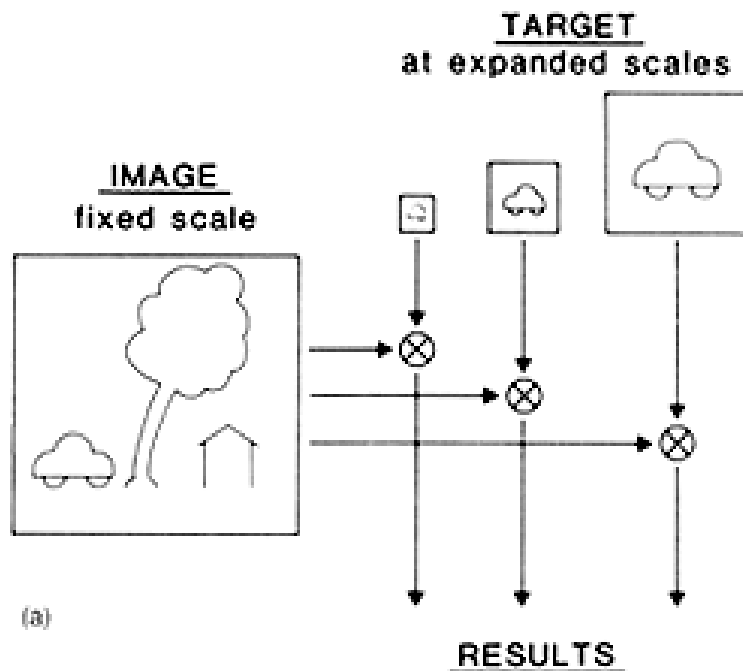
Normalizovaná korelácia – najpomalšia,
invariantná voči zmene kontrastu a
intenzity

Nájdí  v obraze

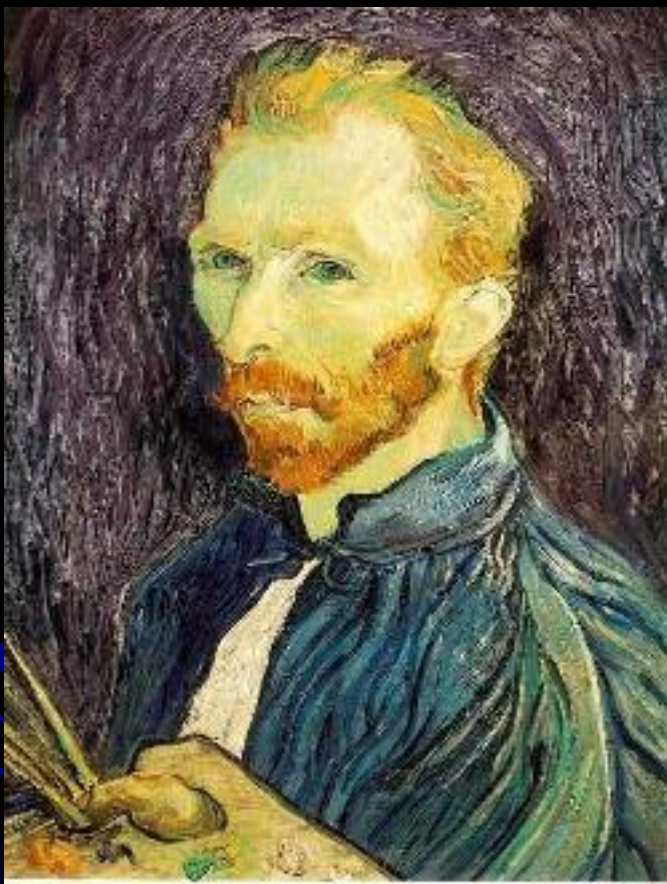
?



Hľadanie objektov rôznych veľkostí



Škálovanie

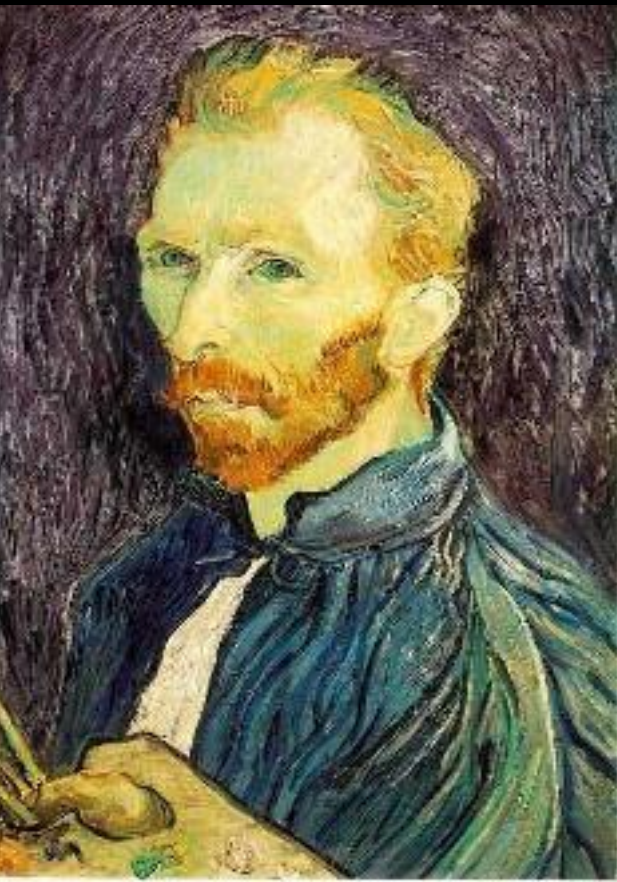


1/4



1/16

Zahod' každý druhý riadok a stĺpec



$1/2$

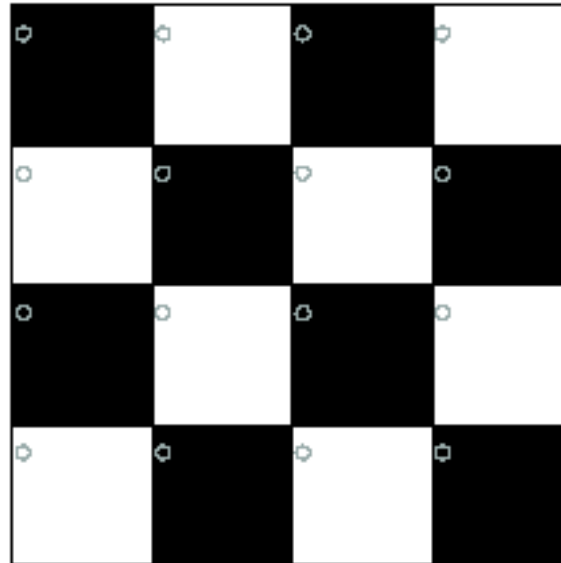
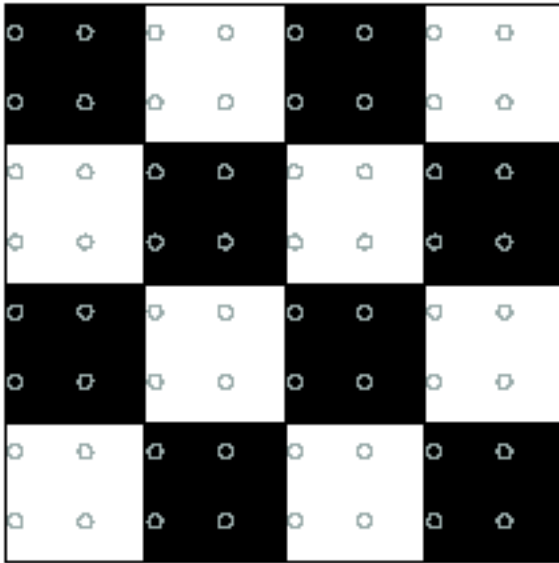


$1/4$ (2x zoom)

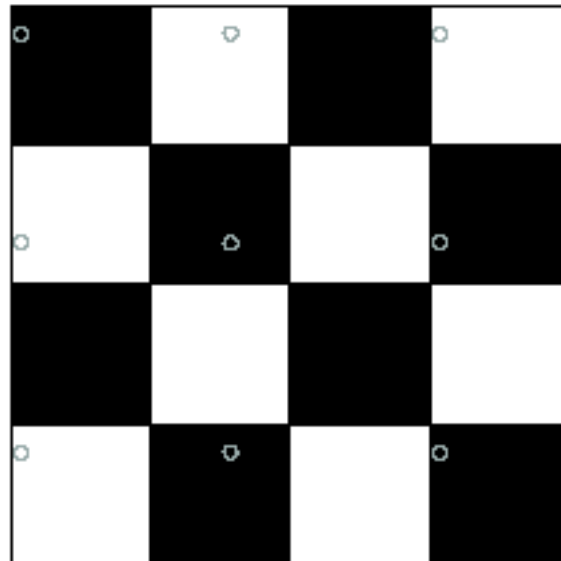
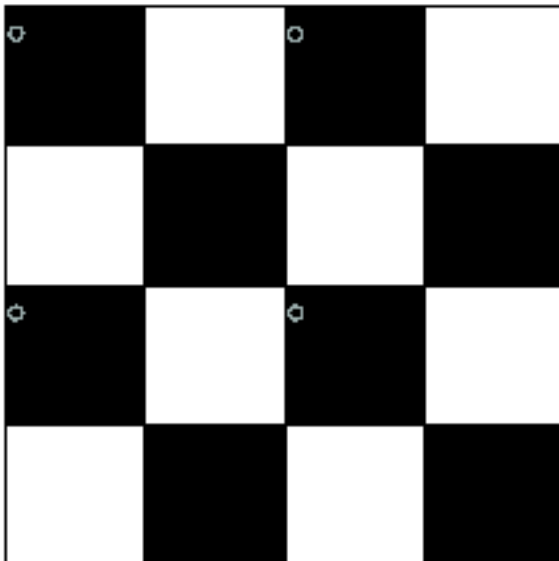


$1/8$ (4x zoom)

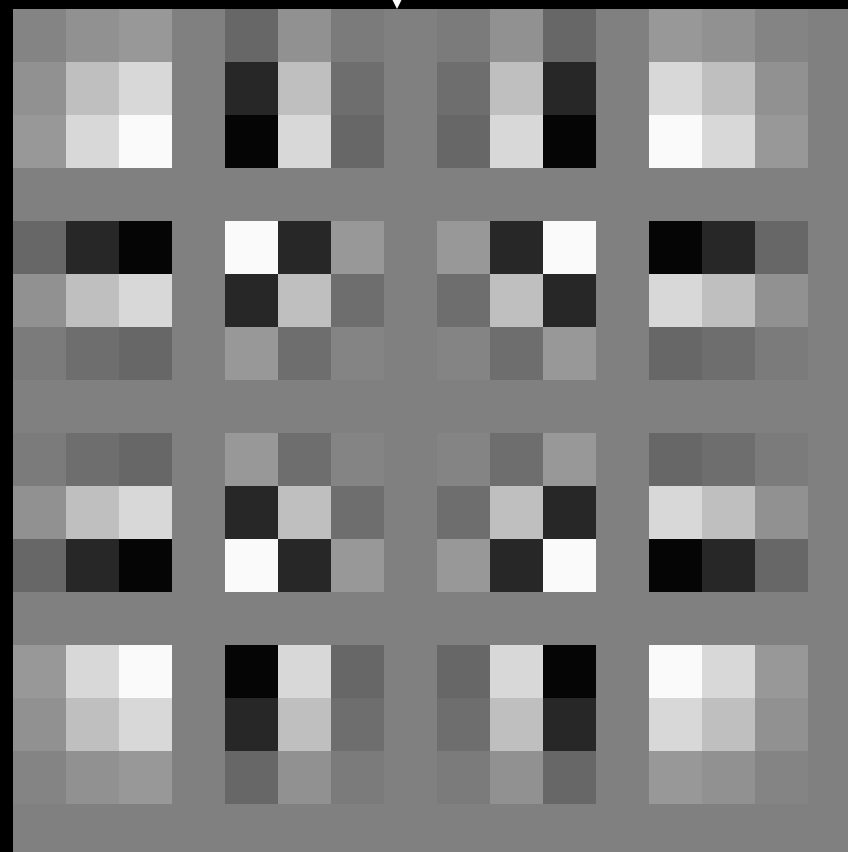
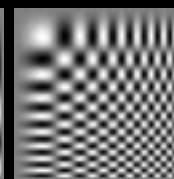
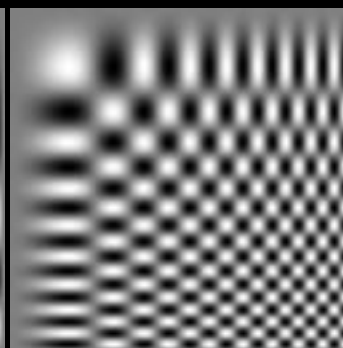
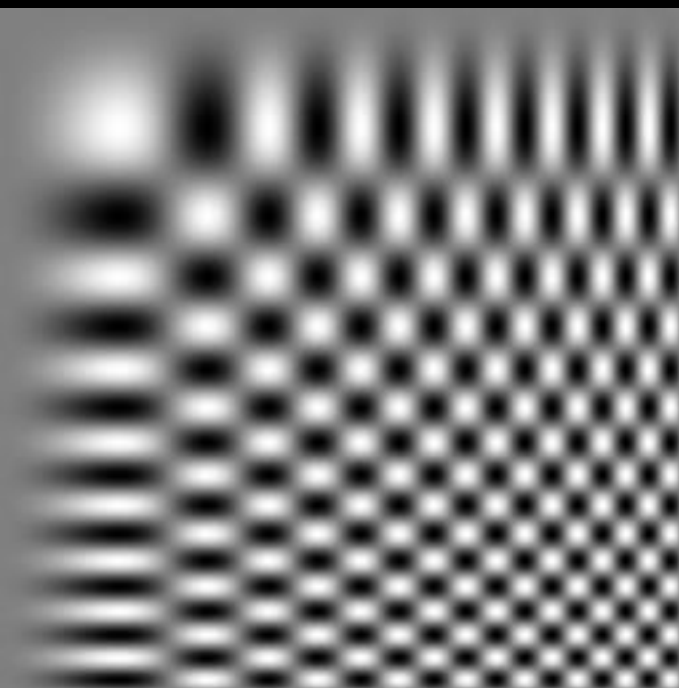
Dobré a zlé vzorkovanie



Dobré vzorkovanie:
Dostatočne veľa
vzoriek, alebo
„dobré“ vzorky

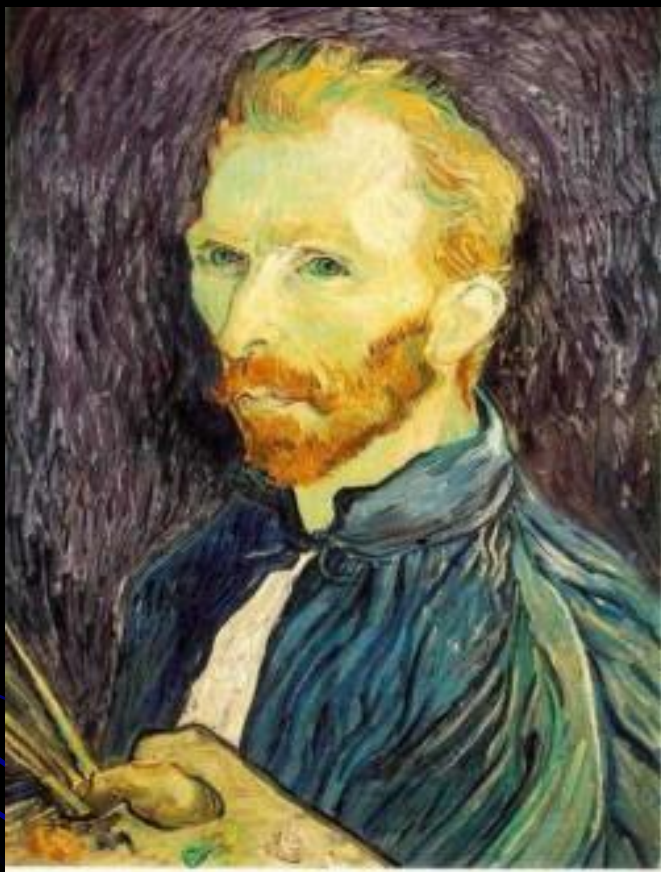


Zlé vzorkovanie:
Výsledkom je
aliasing!



Zahod' každý druhý riadok a stĺpec

Škálovanie s rozostrením



Gauss a potom škálovanie



Gaussian $1/2$



G $1/4$



G $1/8$



$1/2$



$1/4$ (2x zoom)



$1/8$ (4x zoom)

Gaussovská pyramída

$$G_1 = (G_0 * \text{gaussian}) \downarrow 2$$



$G_0 = \text{Image}$

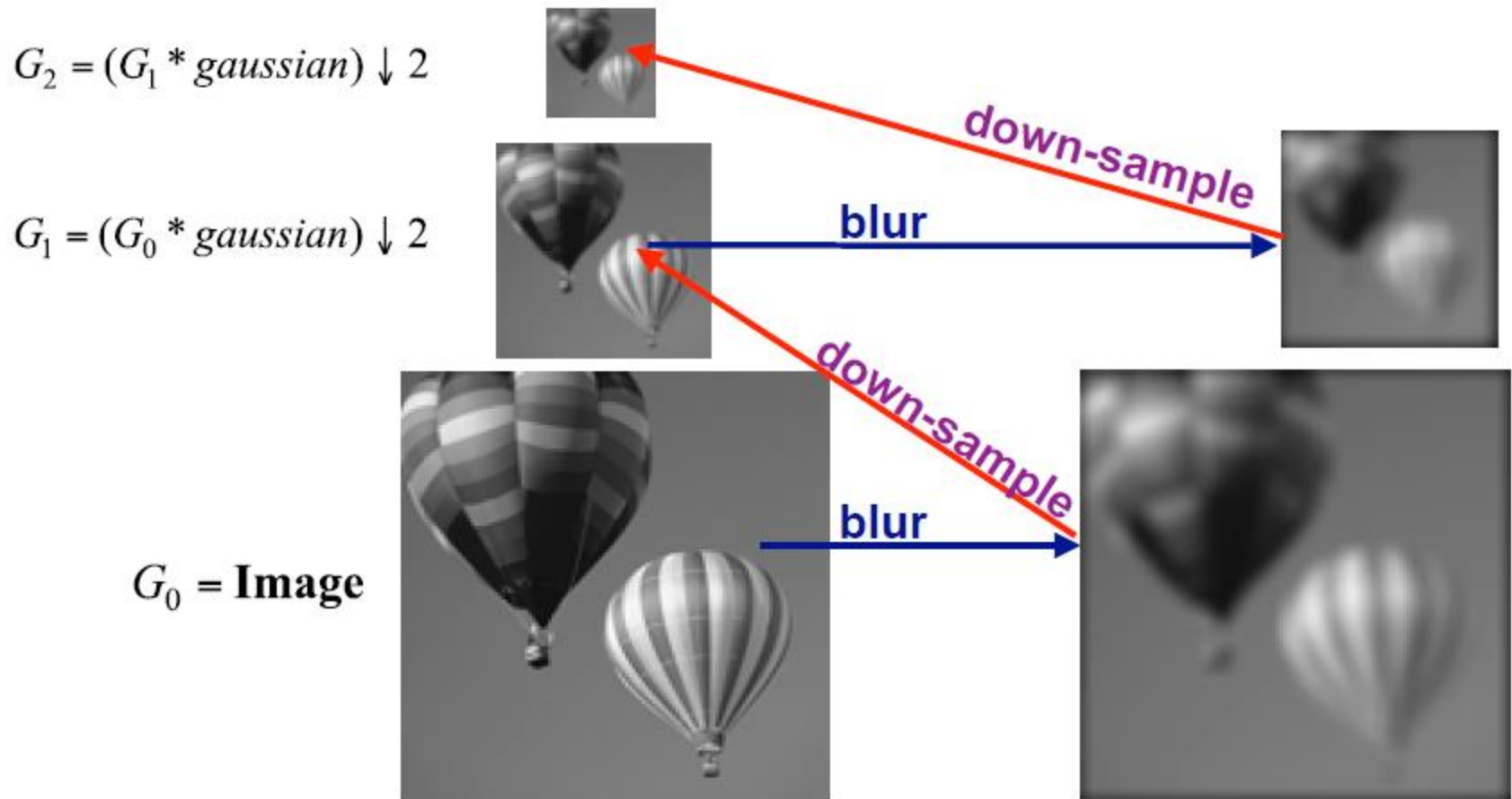


blur

down-sample



Gaussovská pyramída



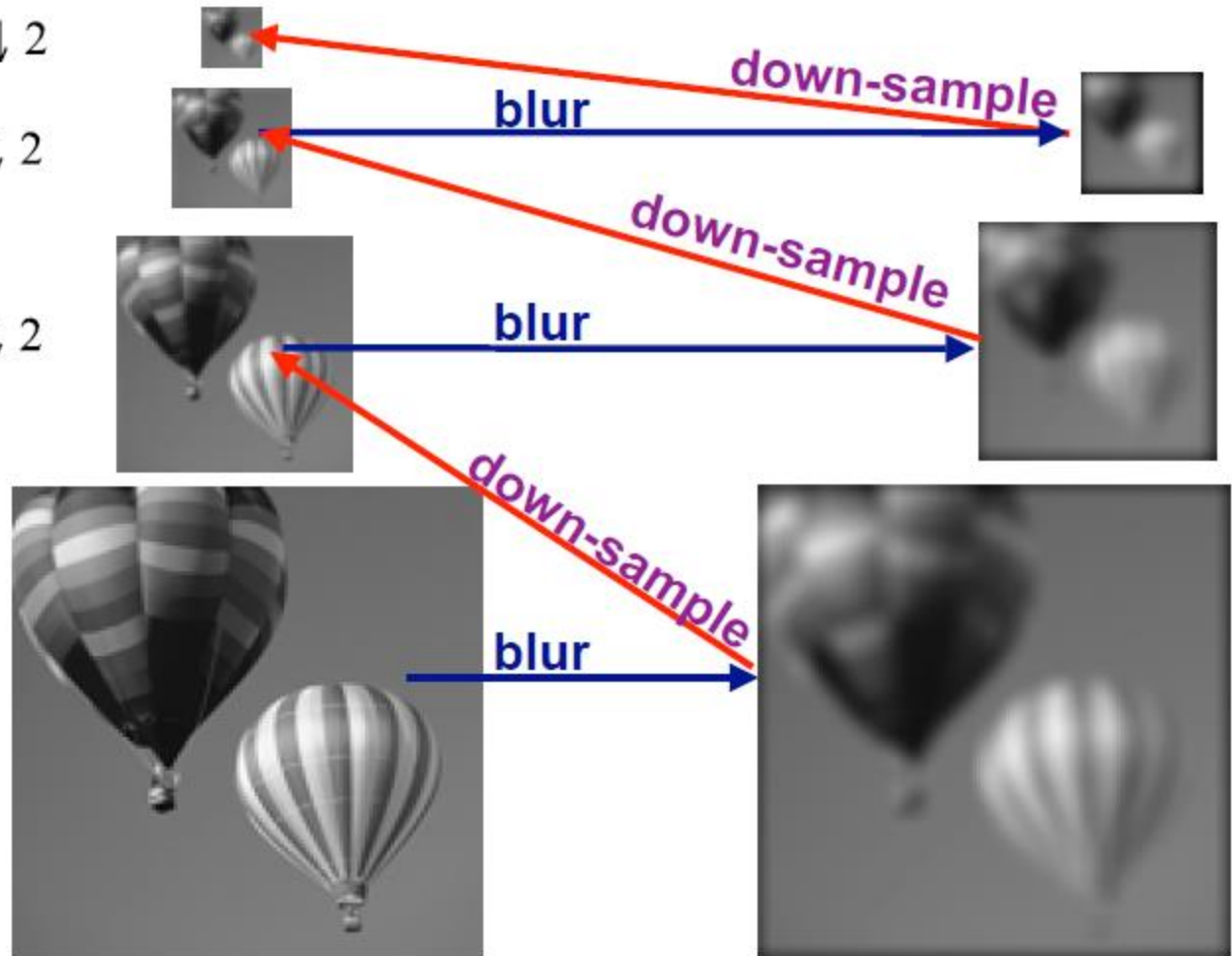
Gaussovská pyramída

$$G_3 = (G_2 * \text{gaussian}) \downarrow 2$$

$$G_2 = (G_1 * \text{gaussian}) \downarrow 2$$

$$G_1 = (G_0 * \text{gaussian}) \downarrow 2$$

$$G_0 = \text{Image}$$



Gaussovská pyramída

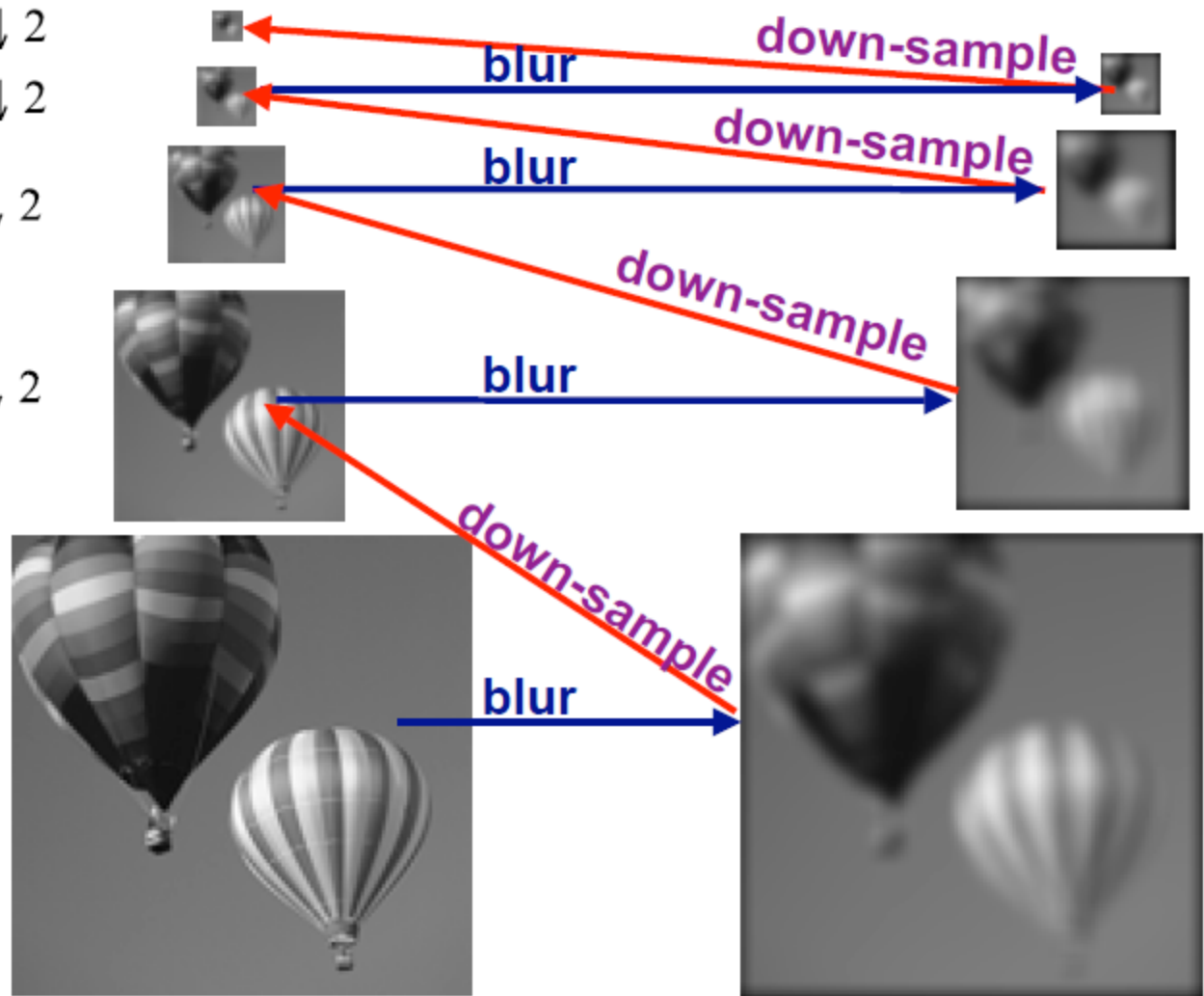
$$G_4 = (G_3 * \text{gaussian}) \downarrow 2$$

$$G_3 = (G_2 * \text{gaussian}) \downarrow 2$$

$$G_2 = (G_1 * \text{gaussian}) \downarrow 2$$

$$G_1 = (G_0 * \text{gaussian}) \downarrow 2$$

$$G_0 = \text{Image}$$



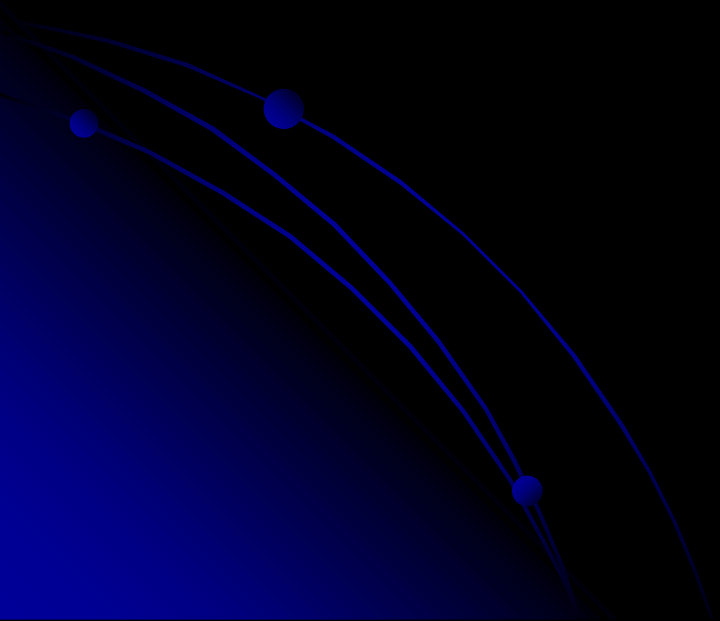
Priestorové prehľadávanie

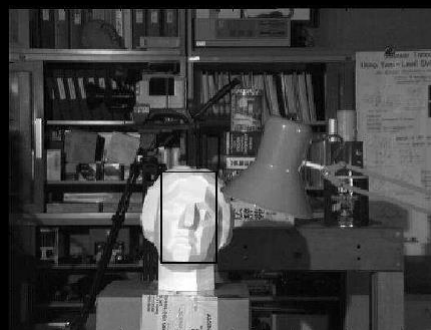
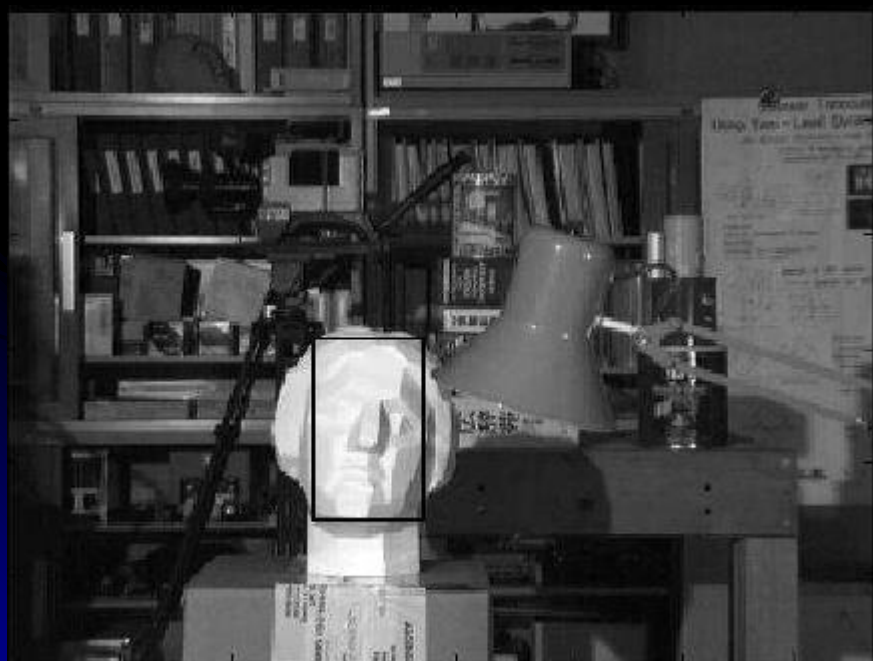
Pyramídový prístup

Začneme najviac degradovanou verziou

Nájdeme kandidátne oblasti

Ďalej hľadáme len v týchto oblastiach





GP – vysoko redundantné údaje

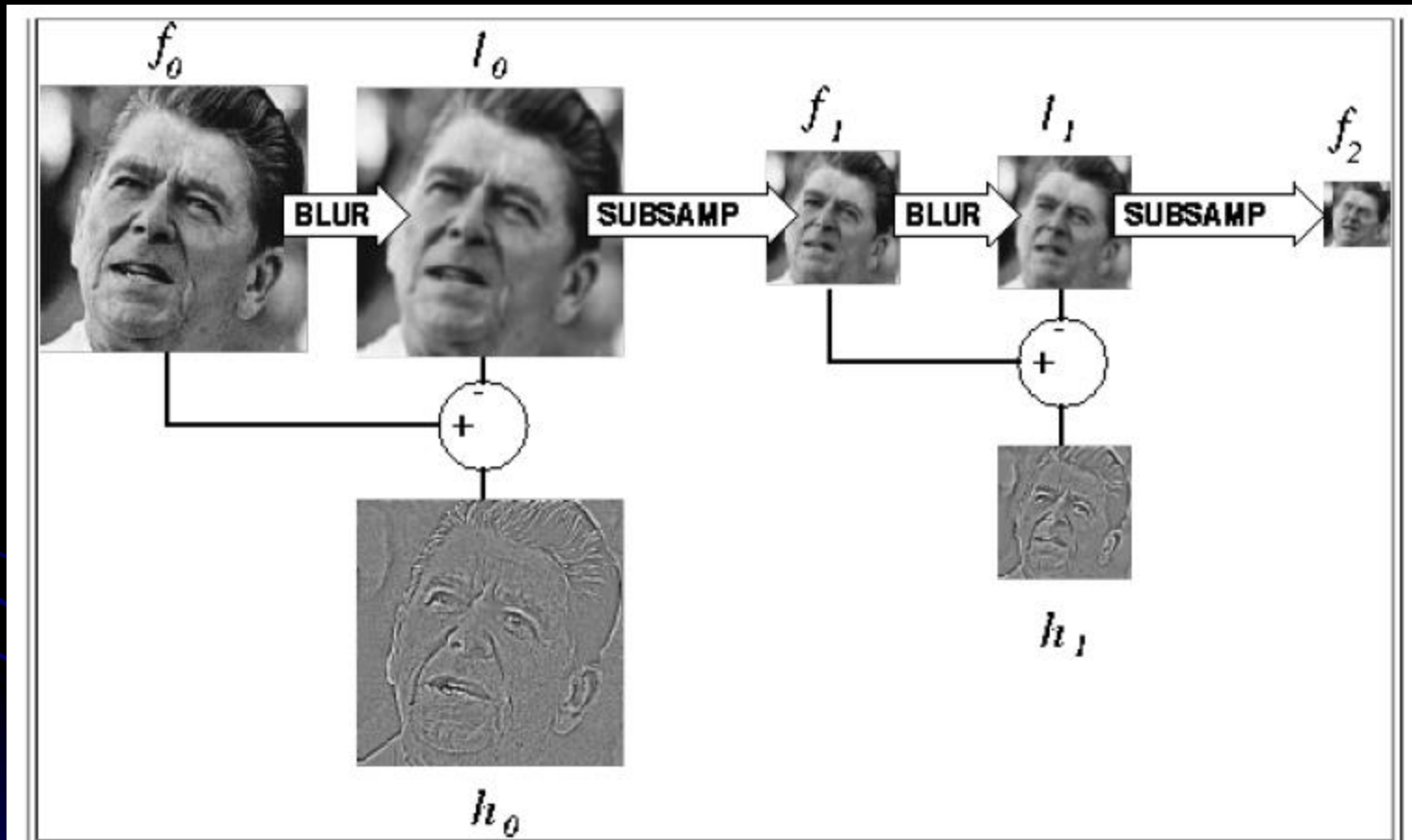
Nízkopriepustný filter – najnižšie frekvencie sú v každom obraze

Nepotrebuje uložiť celý obraz, stačí chyba



Laplacovská pyramída

Laplacovská pyramída



Pri výrobe GP, strácame info
Uložíme do LP

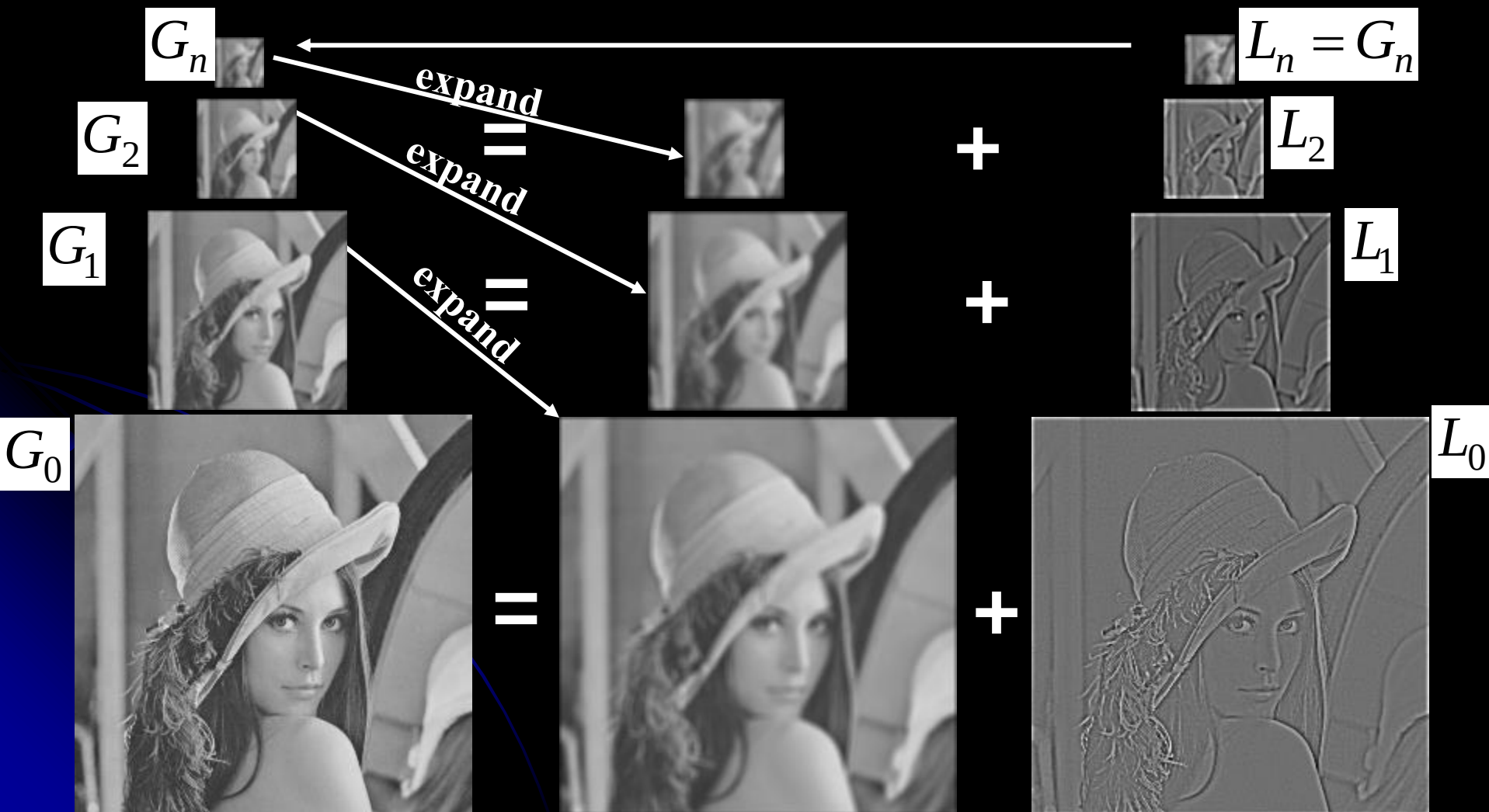
LP vs. GP

$$L_i = G_i - \text{expand}(G_{i+1})$$

$$G_i = L_i + \text{expand}(G_{i+1})$$

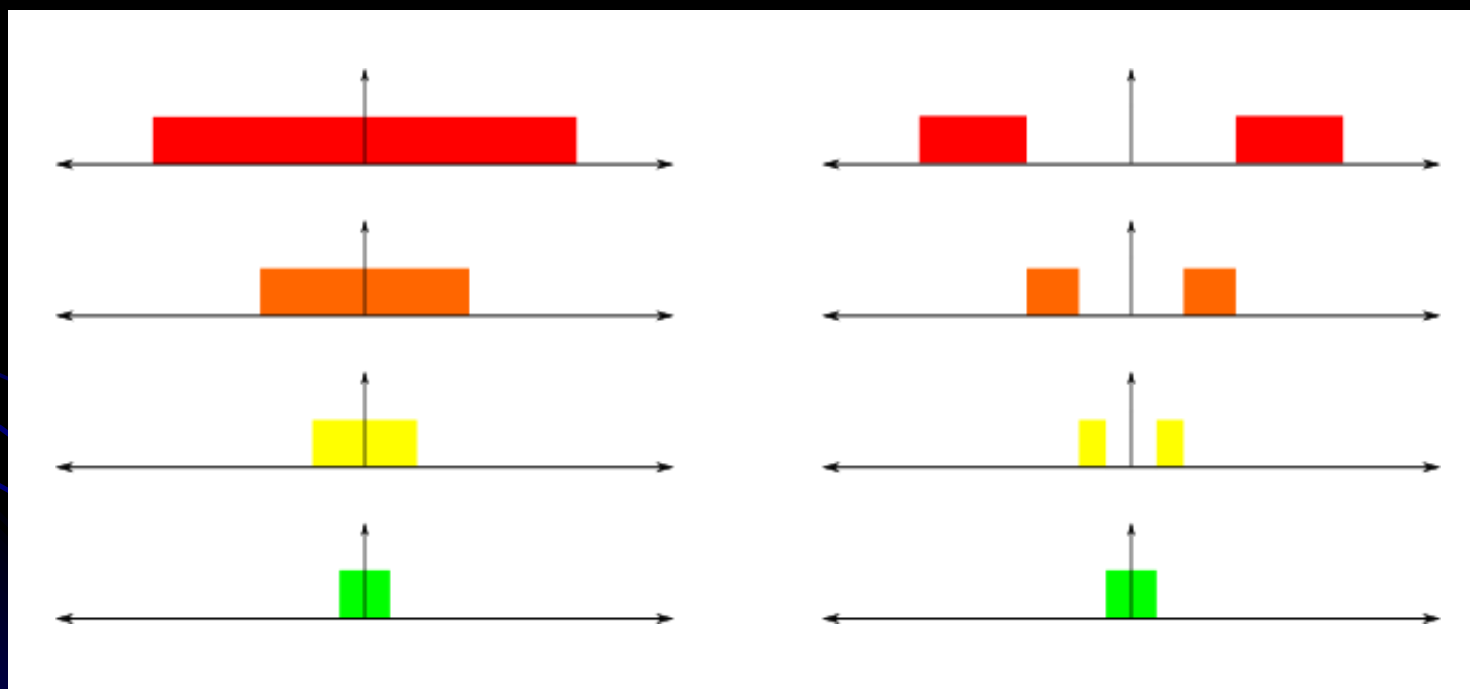
GP

LP

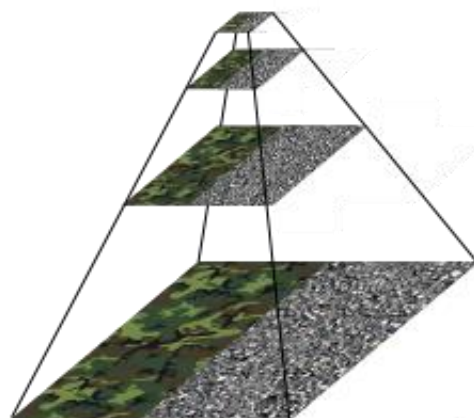
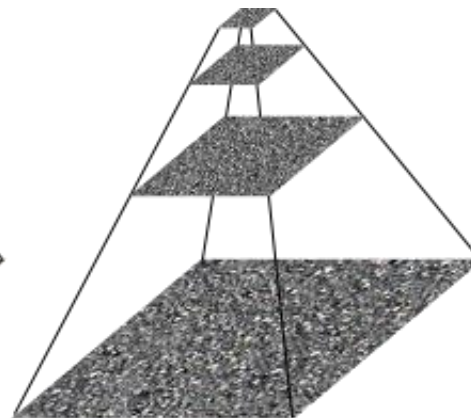
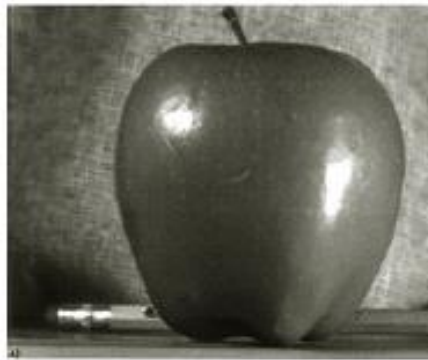


LP vs. GP

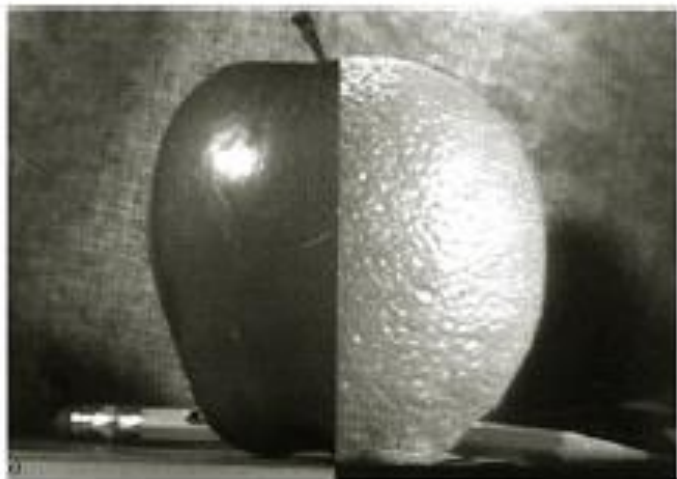
Frekvencie obsiahnuté v jednotlivých úrovniach



Kombinovanie obrazov



Jablanč

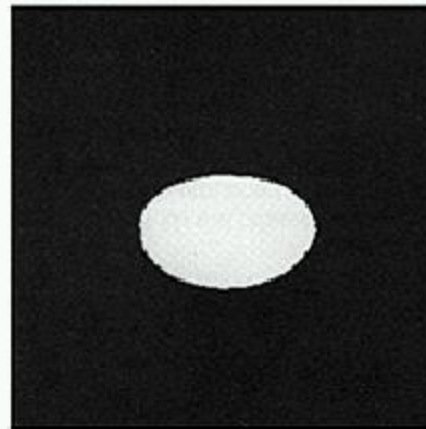


Kombinovanie regiónov

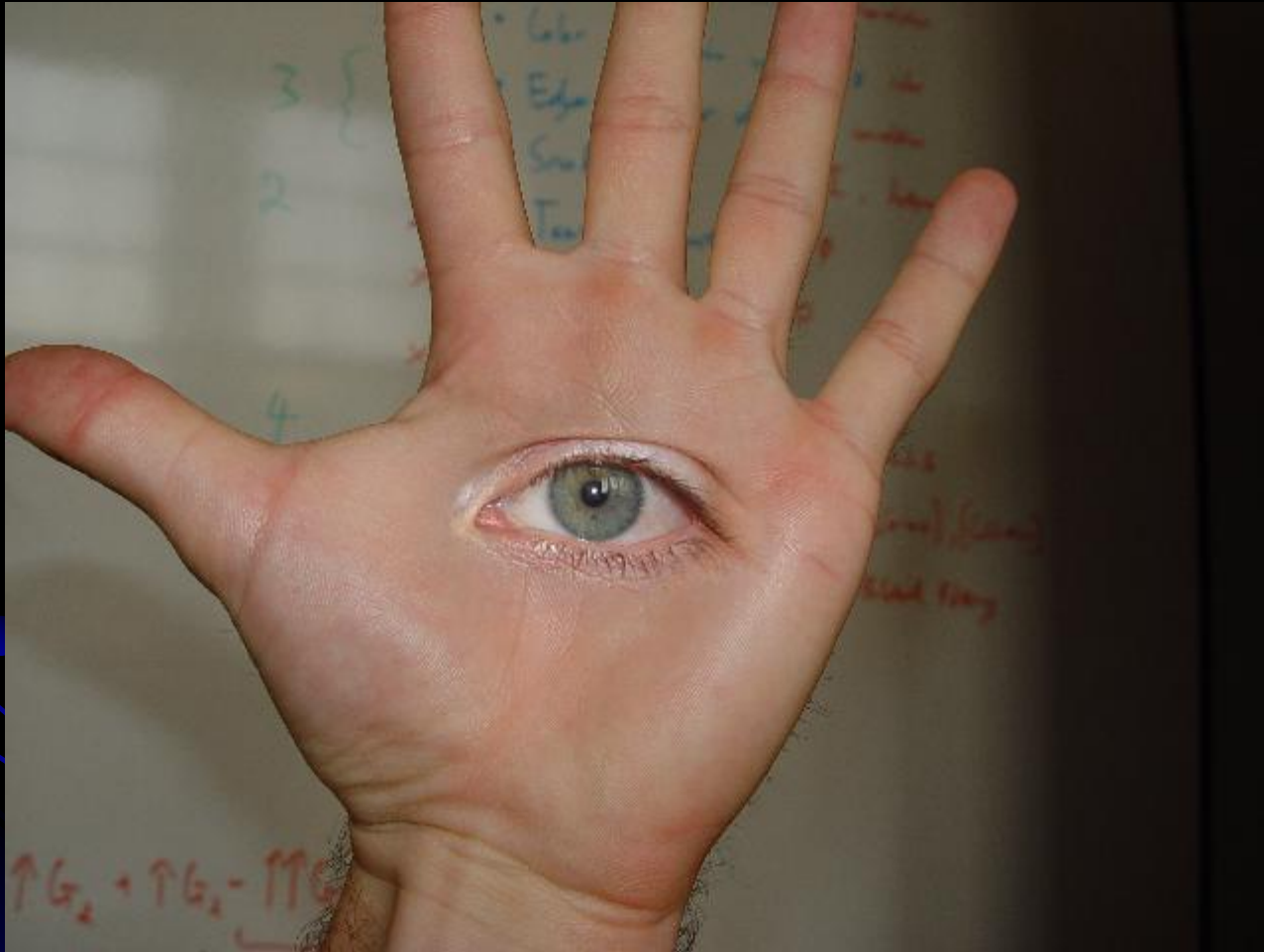
- Given two images A and B , and a mask M
- Construct Laplacian Pyramids L_a and L_b
- Construct a Gaussian Pyramid G_m
- Create a third Laplacian Pyramid L_c where for each level l

$$L_c(i, j) = G_m(i, j)L_a(i, j) + (1 - G_m(i, j))L_b(i, j)$$

- Sum all levels L_c in to get the blended image



Horror foto

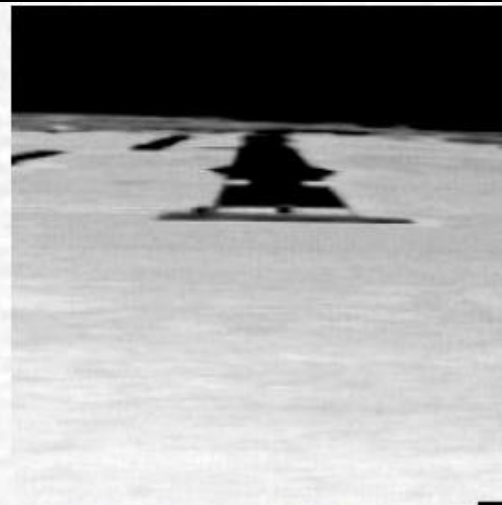


© prof. dmartin

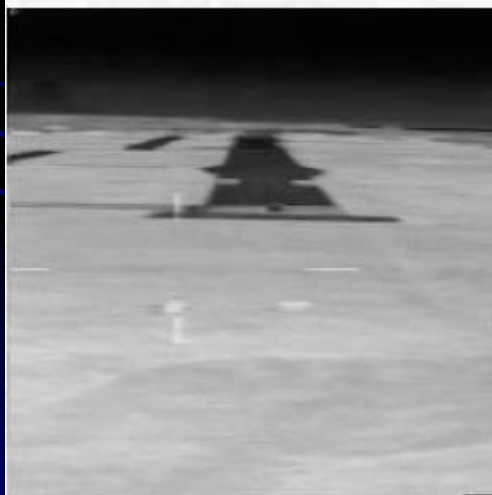
Multi-Sensor Fusion



Long Wave



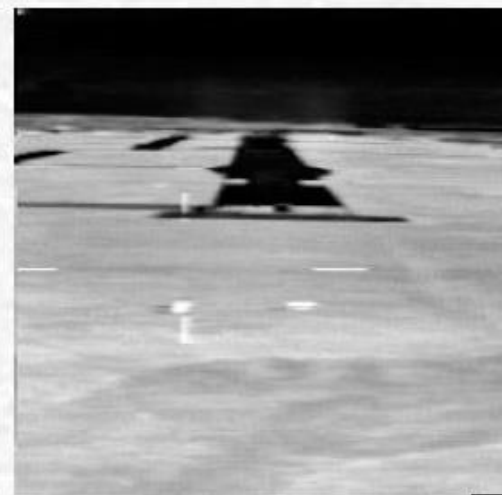
Medium Wave



Averaging

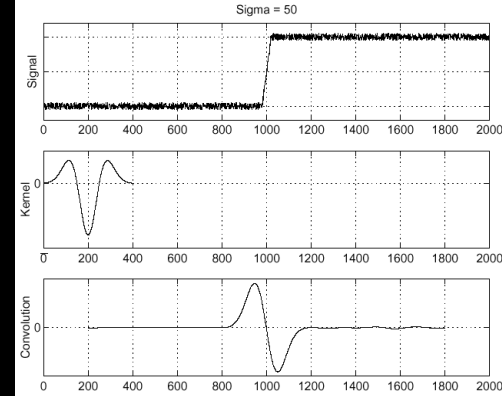


Selecting Maximum

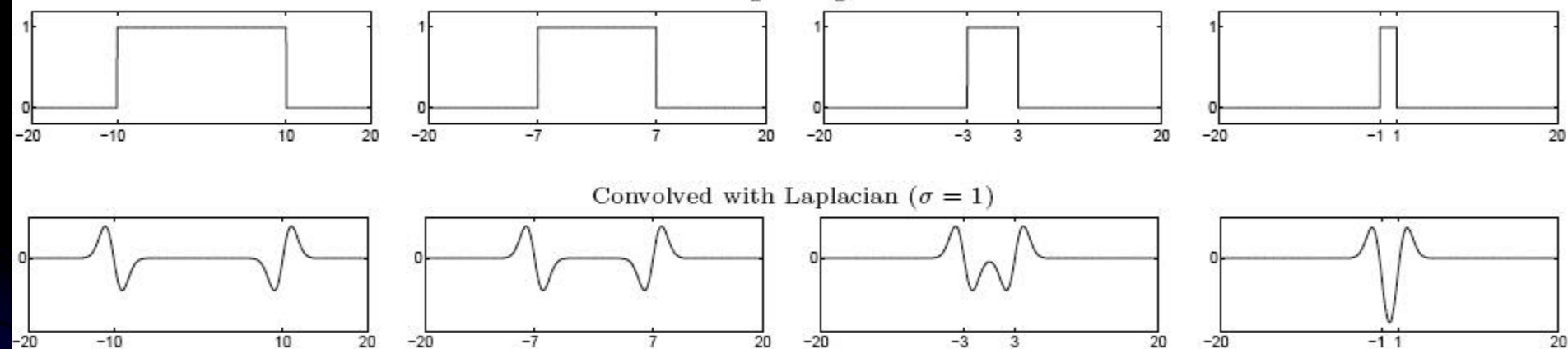


Laplacian Fusion

Škvvrny



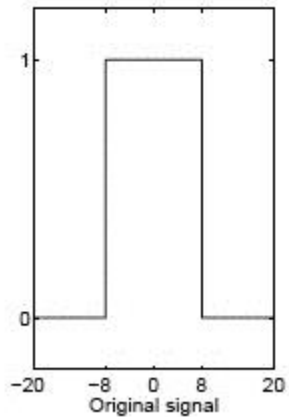
Original signal



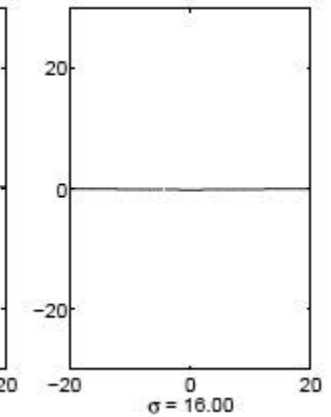
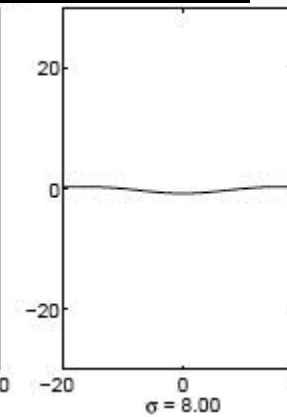
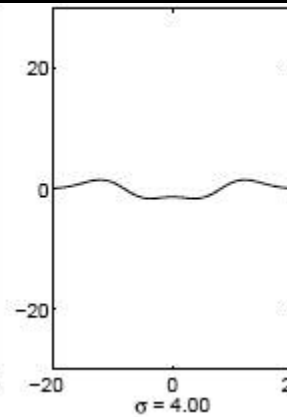
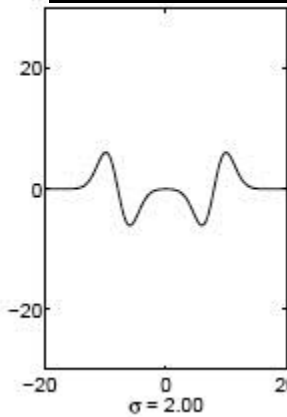
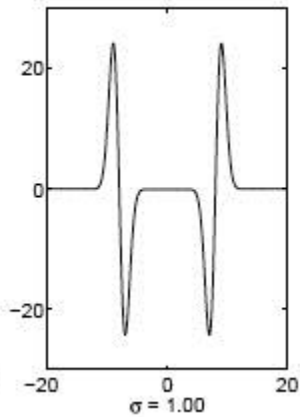
Odozva Laplaciánu bude maximálna v strede škvrny pri vhodnej škále

Normalizácia

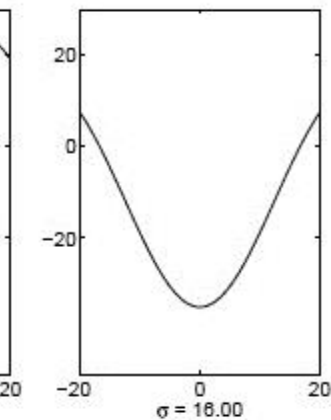
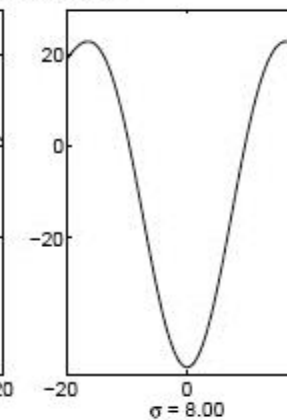
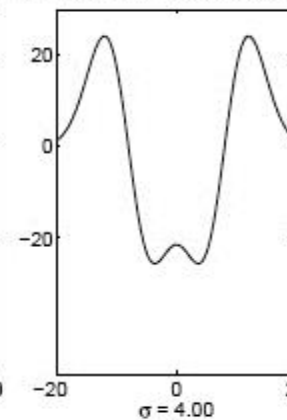
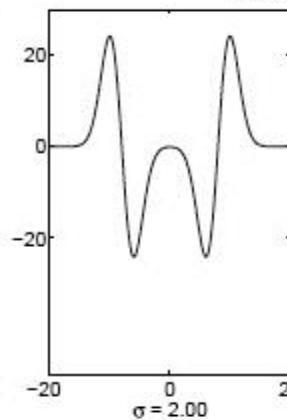
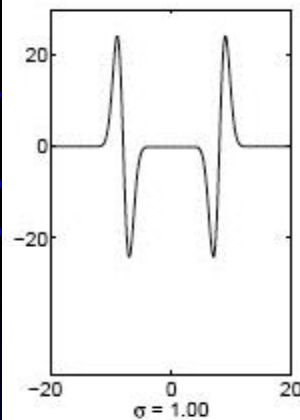
signál



Odozva Laplaciánu pri rôznej škále

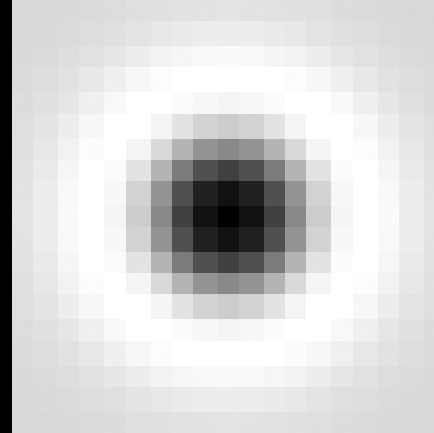
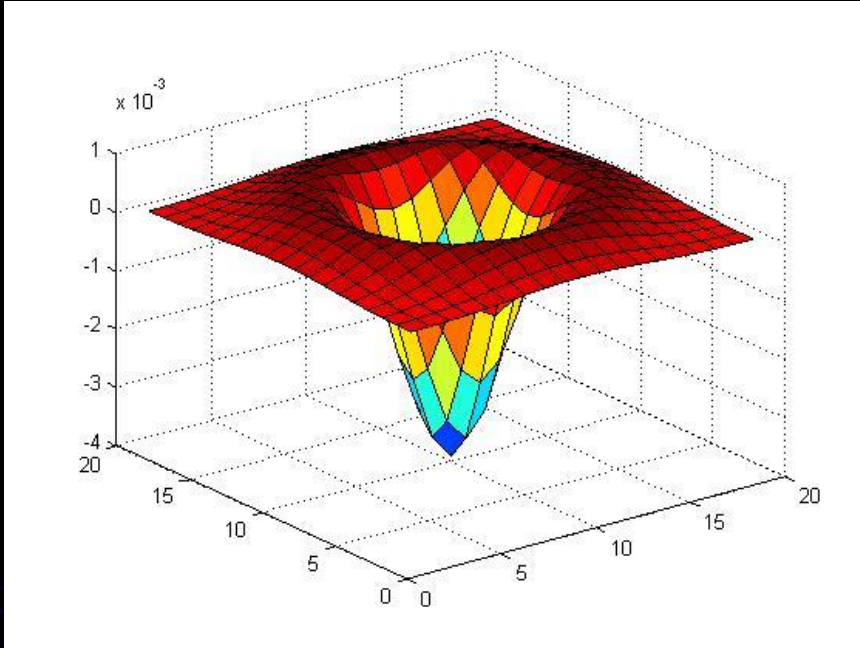


Normalizovaná odozva



maximum

2D LoG

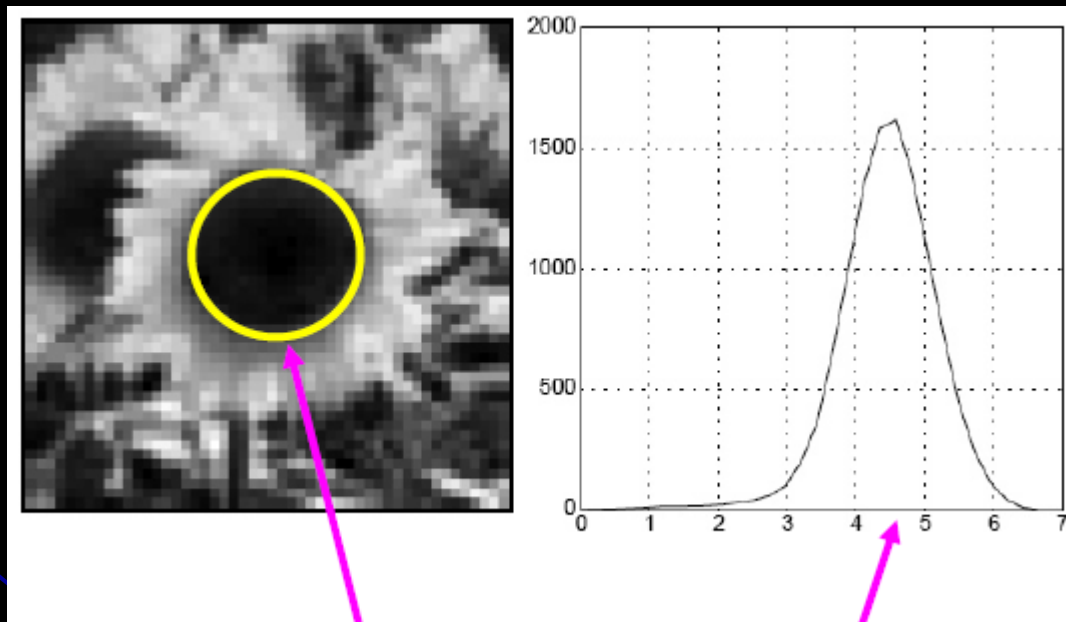


$$\nabla^2 G = \frac{\partial^2 G}{\partial x^2} + \frac{\partial^2 G}{\partial y^2}$$

normalizácia:

$$\nabla_{\text{norm}}^2 G = \sigma^2 \left(\frac{\partial^2 G}{\partial x^2} + \frac{\partial^2 G}{\partial y^2} \right)$$

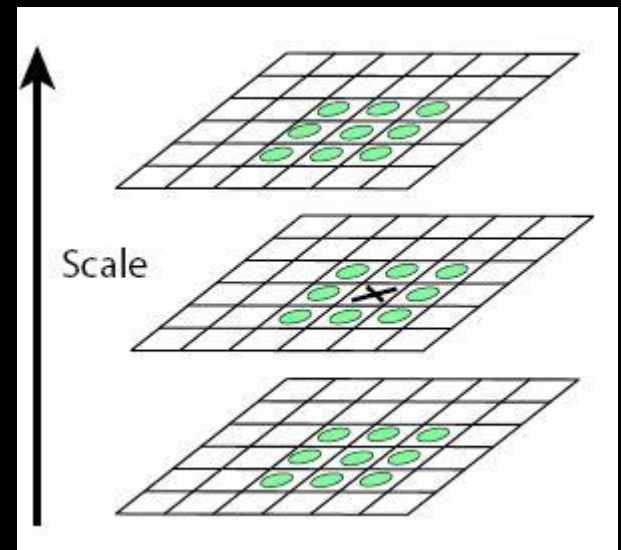
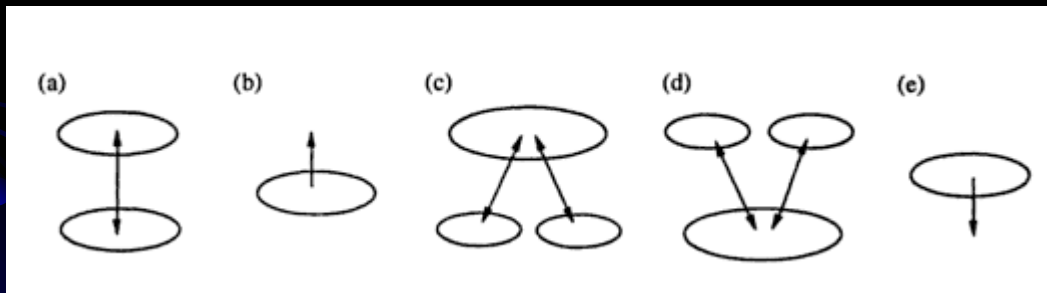
charakteristická škála škvryny
maximální odpověď Laplaceanu v strede škvryny



Detekcia škvrn v ŠP

Odozva Laplacián obrazu pri rôznych škálach

Maximá v ŠP







sigma = 11.9912



Lokálne príznaky

Skladajú sa z dvoch častí:

- Detektor na nájdenie zaujímavých bodov
- Deskriptor na ich popísanie

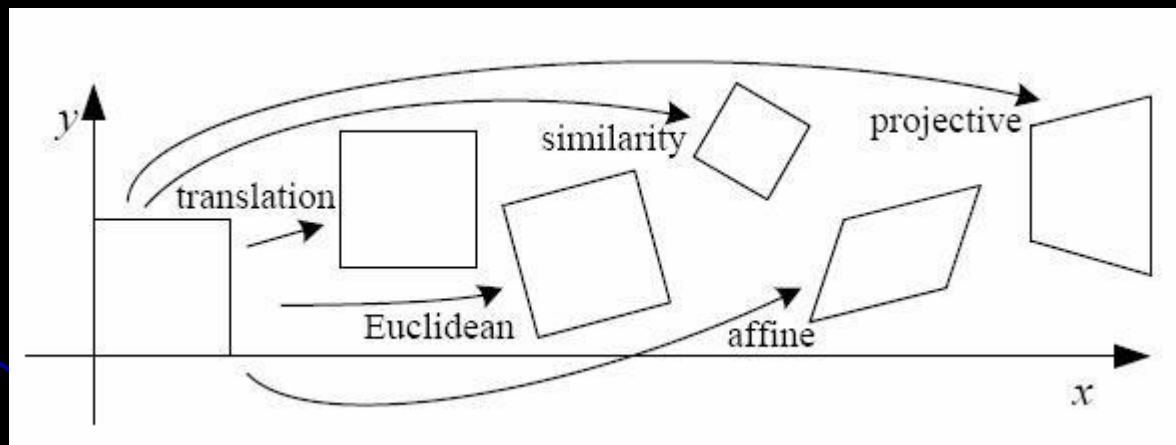
Porovnavanie

- Dôležitá je metrika!

Klasifikácia

- Obvykle počet zhôd

Invariantnost'



Výber zaujímavých bodov

Naivné:

Všetky body

Náhodné body

Rovnomerne
rozmiestnené body

Detektory:

Harris corners

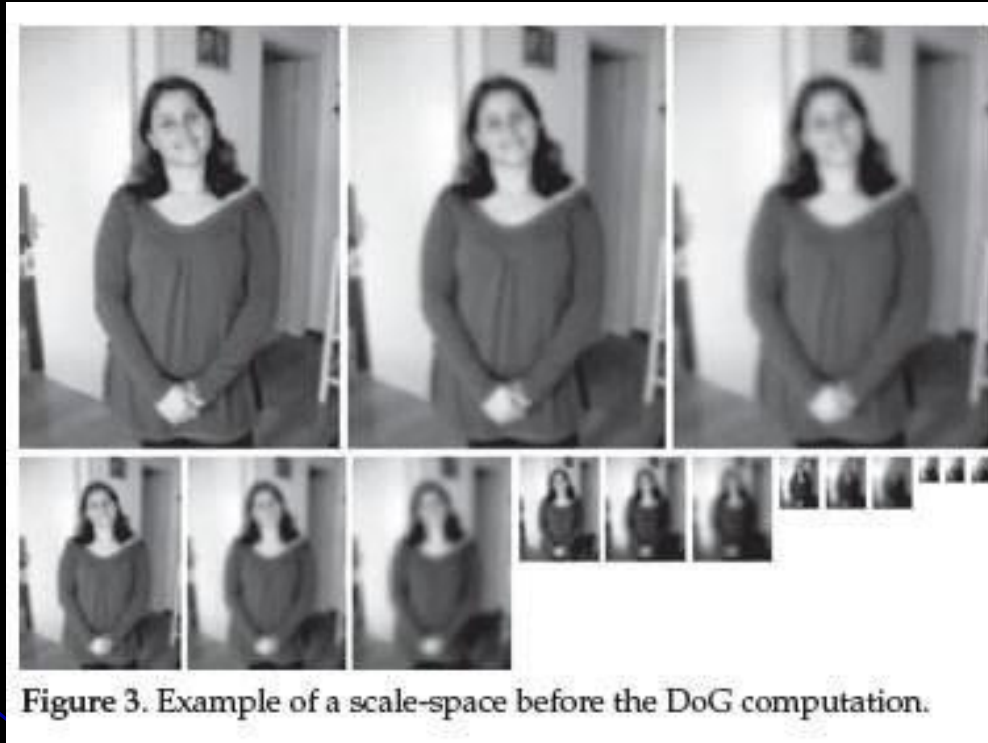
SUSAN

SIFT

SURF

FAST

SIFT



Hľadá zaujímavé body v DoG priestore

DoG priestor

Rovnica prenosu tepla

$$\sigma \nabla^2 G = \frac{\partial G}{\partial \sigma}$$

$$\frac{\partial G}{\partial \sigma} \approx \frac{G(k\sigma) - G(\sigma)}{k\sigma - \sigma}$$

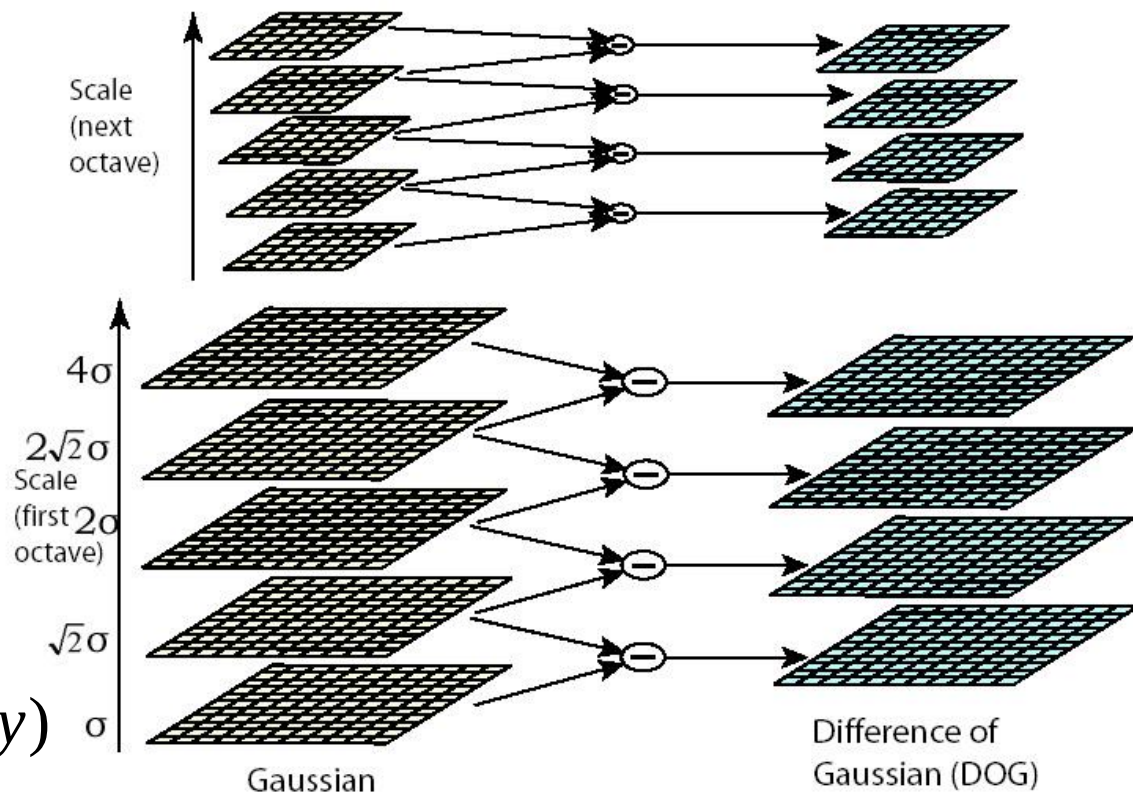
$$(k - 1)\sigma^2 \nabla^2 G \approx G(k\sigma) - G(\sigma)$$

$$\nabla_{\text{norm}}^2 G = \sigma^2 \nabla^2 G$$

$$D(x, y, \sigma) = \nabla_{\text{norm}}^2 G(x, y, \sigma) * I(x, y)$$

DoG priester

$$\begin{aligned}
 D(x, y, \sigma) &= \sigma^2 \nabla^2 G * I \\
 &\approx (G(k\sigma) - G(\sigma)) * I \\
 &\approx G(k\sigma) * I - G(\sigma) * I
 \end{aligned}$$



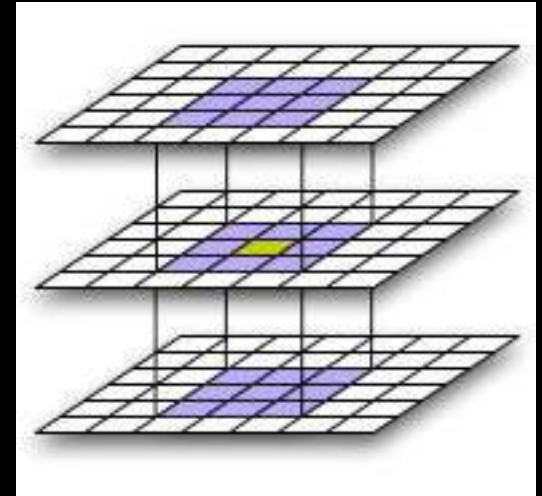
$$J(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$

SIFT

Zaujímavé body hľadá v 26 okoli v DoG

Hľadajú sa minimá a maximá
⇒ lokálne extrémny v 26 okoli

Určili sme pozíciu a škálu
Orientácia



$$\theta(x, y) = \arctan \frac{J(x, y+1) - J(x, y-1)}{J(x+1, y) - J(x-1, y)}$$

Odstránia sa
málo kontrastné body

body pozdĺž hrán

Hesseho matica druhých derivácií

$$\tilde{\mathbf{H}} = \begin{bmatrix} D_{xx} & D_{xy} \\ D_{xy} & D_{yy} \end{bmatrix}$$

$$Tr(\mathbf{H}) = D_{xx} + D_{yy} = \alpha + \beta$$

$$\alpha = r\beta$$

$$Det(\mathbf{H}) = D_{xx}D_{yy} - (D_{xy})^2 = \alpha\beta$$

$$\frac{Tr(\mathbf{H})^2}{Det(\mathbf{H})} = \frac{(\alpha + \beta)^2}{\alpha\beta} = \frac{(r\beta + \beta)^2}{r\beta^2} = \frac{(r+1)^2}{r}$$



(a)



(b)



(c)



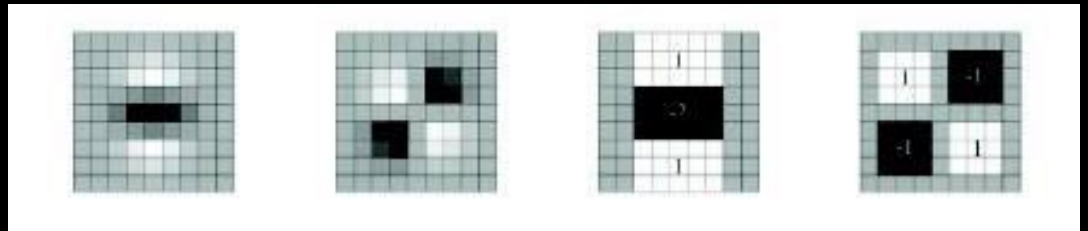
(d)

Figure 5. This figure shows the stages of keypoint selection. (a) The 233×189 pixel original image. (b) The initial 832 keypoints locations at maxima and minima of the difference-of-Gaussian function. Keypoints are displayed as vectors indicating scale, orientation, and location. (c) After applying a threshold on minimum contrast, 729 keypoints remain. (d) The final 536 keypoints that remain following an additional threshold on ratio of principal curvatures.

SURF

Namiesto vytvárania Gaussovej pyramídy
filtruje obrázkov rôznymi veľkosťami filtrov

Filter = aproximácia druhých parciálnych
derivácií Gausiánu

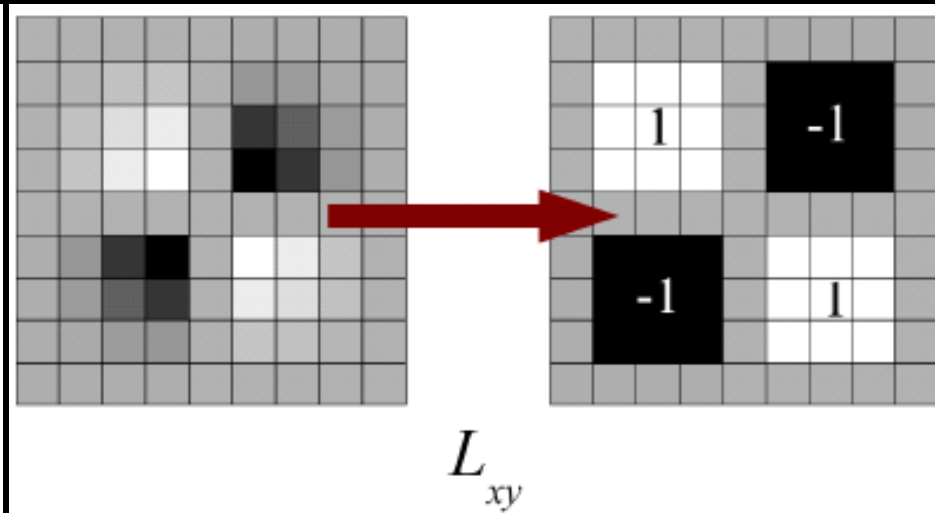
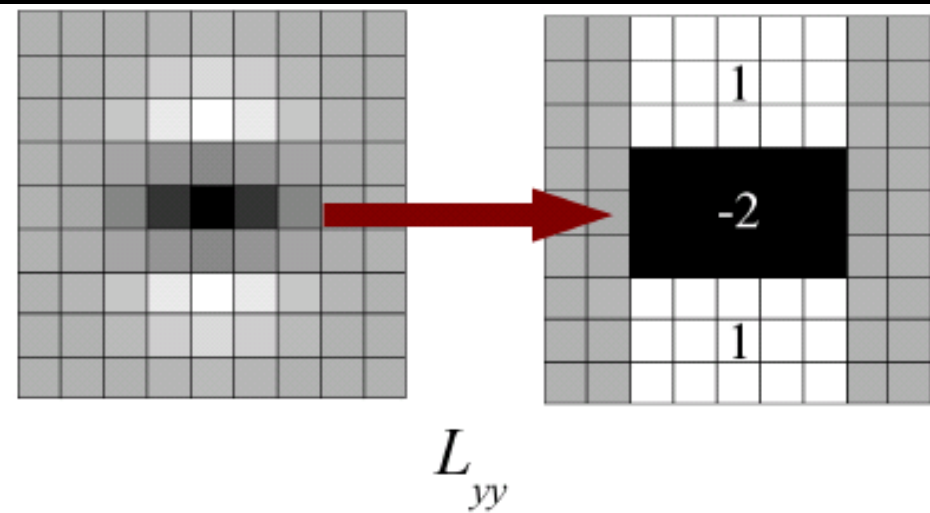


SURF: Speeded Up Robust Features

Herbert Bay, Tinne Tuytelaars, and Luc Van Gool, ECCV 2006

$$SIFT : H_{approx}^{SIFT} = \begin{bmatrix} D_{xx} & D_{xy} \\ D_{yx} & D_{yy} \end{bmatrix}$$

$$SURF : H_{approx}^{SURF} = \begin{bmatrix} \hat{L}_{xx} & \hat{L}_{xy} \\ \hat{L}_{yx} & \hat{L}_{yy} \end{bmatrix}$$



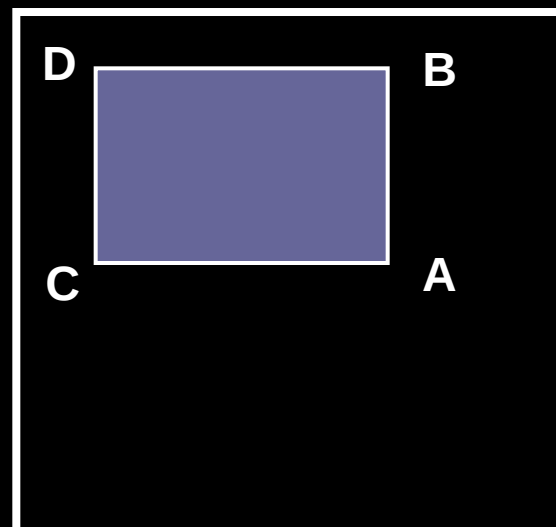
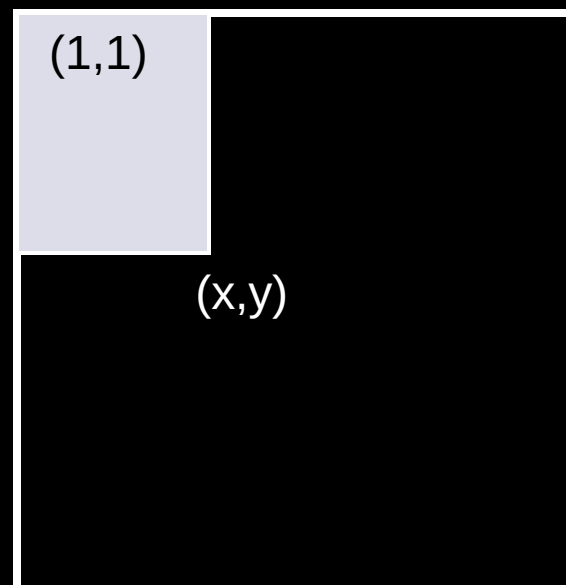
Integrálne obrazy

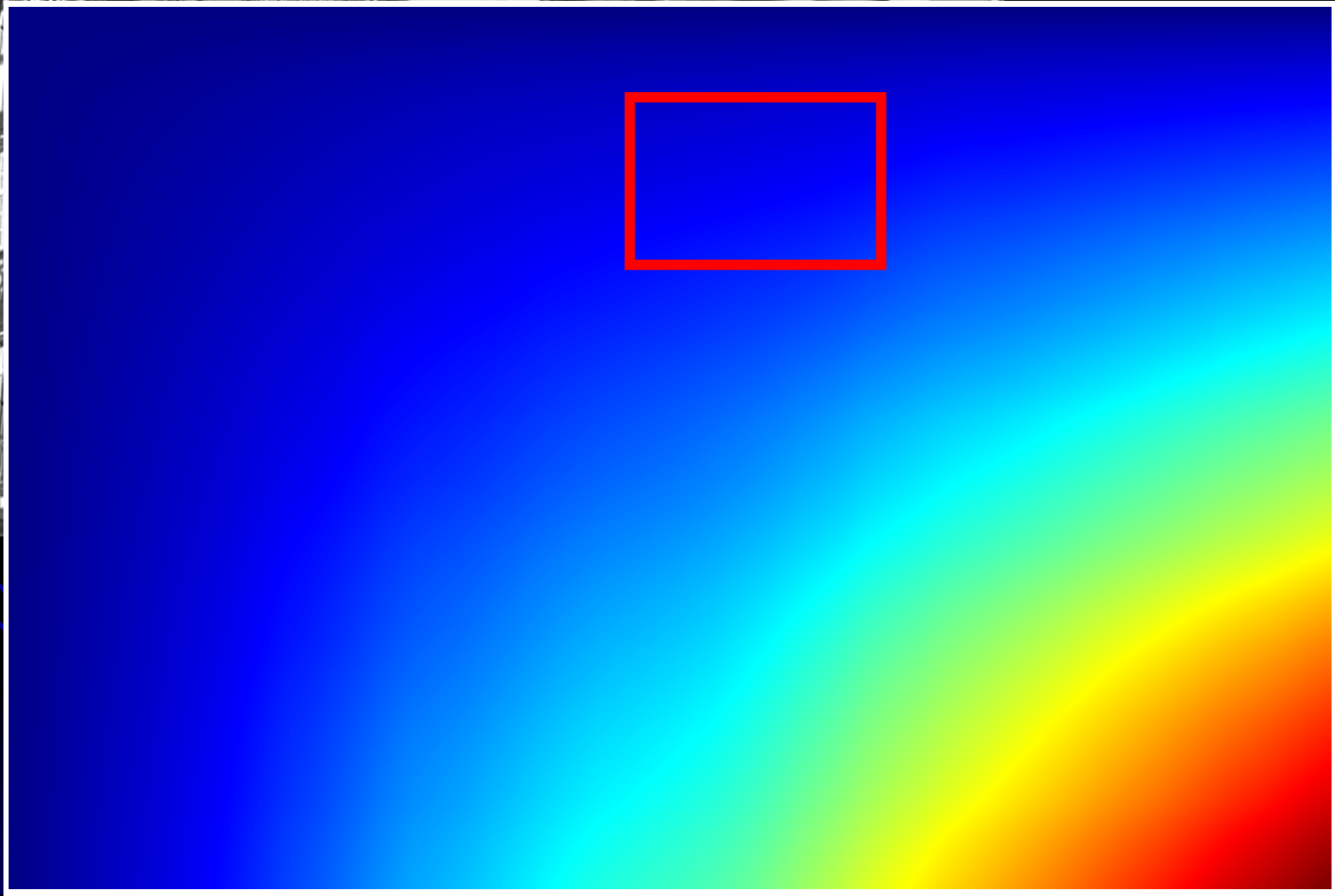
Suma bodov vľavo hore

$$IO(x, y) = \sum_{i=1}^x \sum_{j=1}^y I(i, j)$$

Suma bodov v
obdĺžnikovom okne
(ABCD) pôvodného
obrazu =

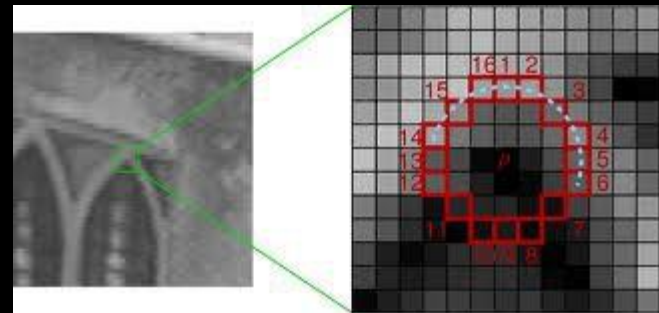
$$IO(A) - IO(B) - IO(C) + IO(D)$$





FAST

Porovnanie hodnoty intenzity bodu a jeho susedov na Bresenhamovej kružnici s polomerom r



E. Rosten and T. Drummond. "Machine learning for high-speed corner detection,". ECCV 2006

Popis zajímavých bodů

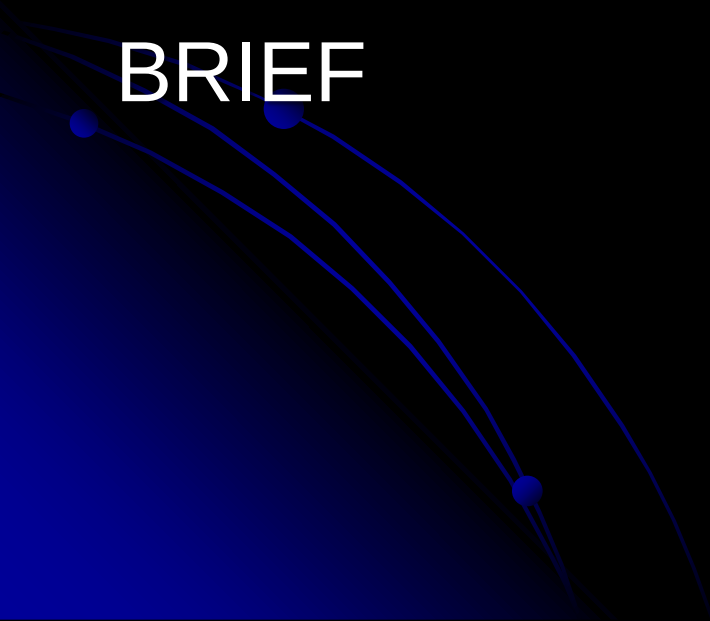
Raw data

HOG

SIFT

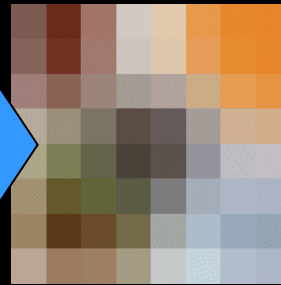
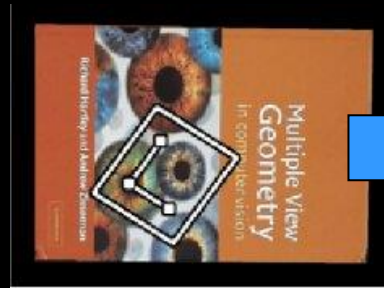
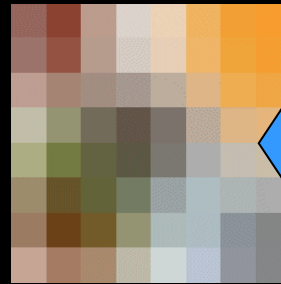
SURF

BRIEF



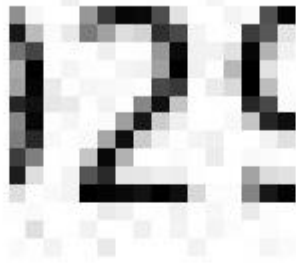
Raw data

Vektor intenzít okna

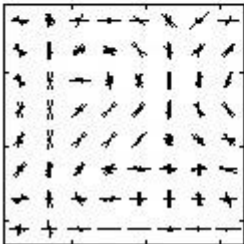


HOG

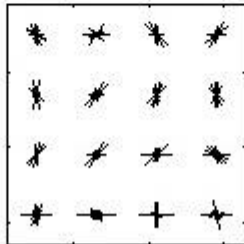
Histogram of Oriented Gradients



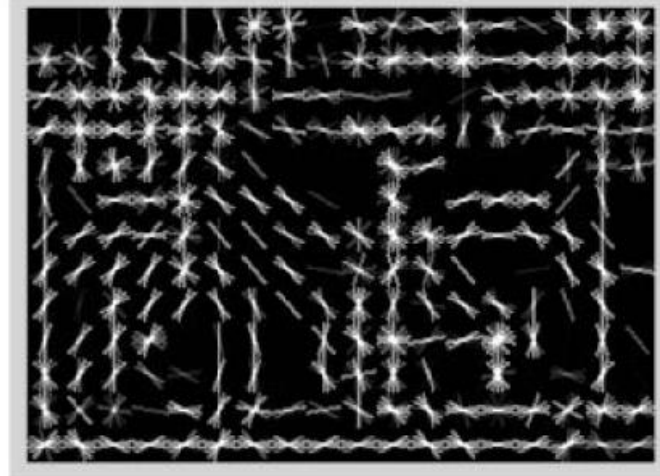
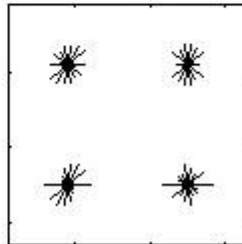
CellSize = [2 2]
Feature length = 1764



CellSize = [4 4]
Feature length = 324

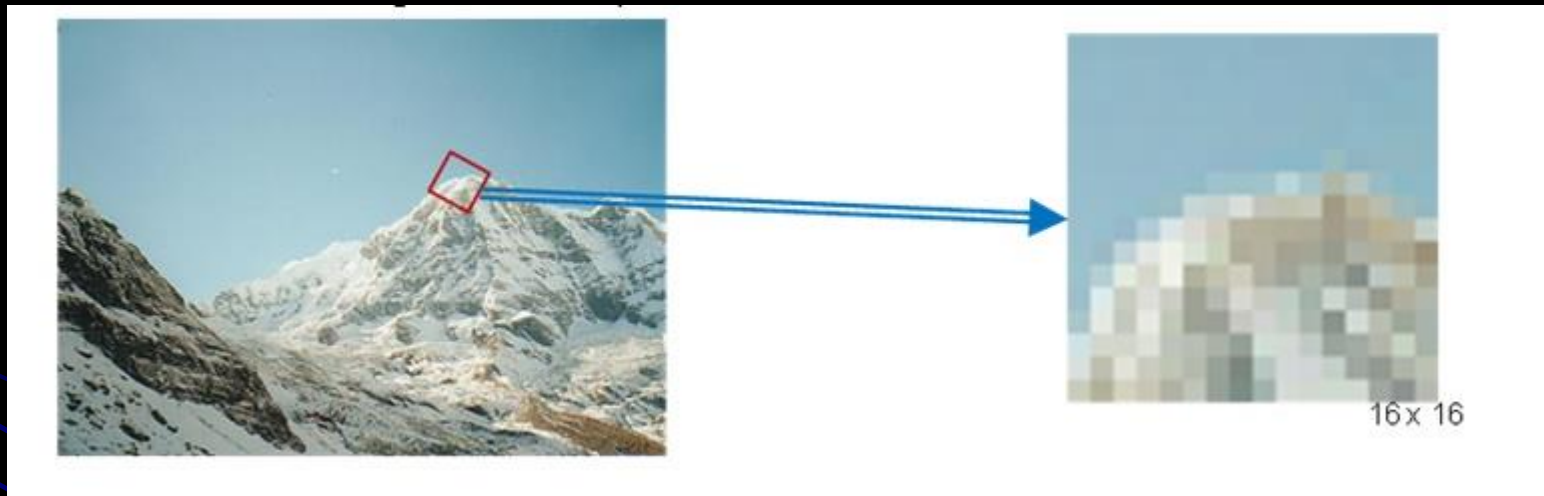


CellSize = [8 8]
Feature length = 36



SIFT

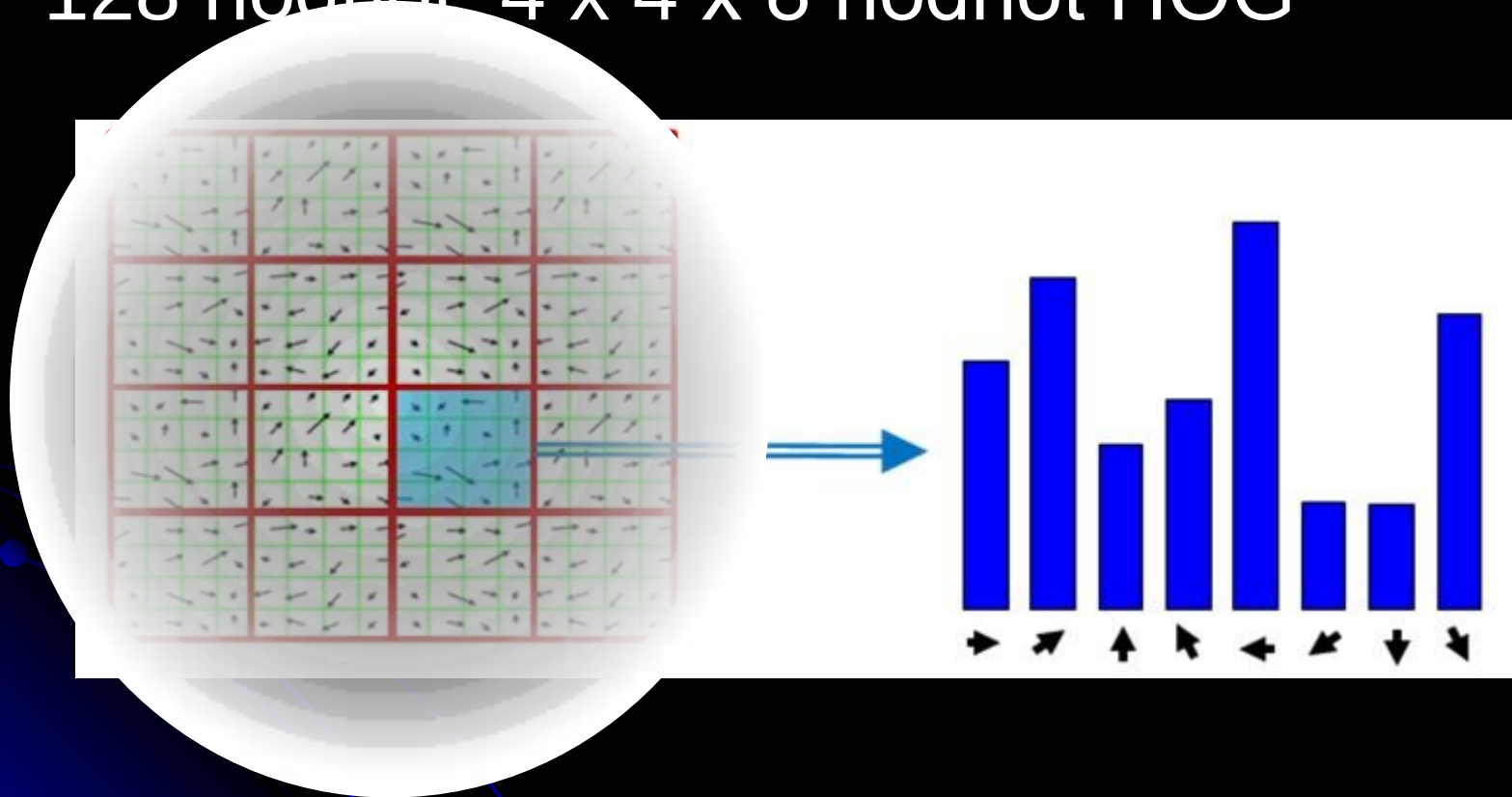
Používa HOG



Okno okolo zaujímavého bodu otočí podľa orientácie

SIFT

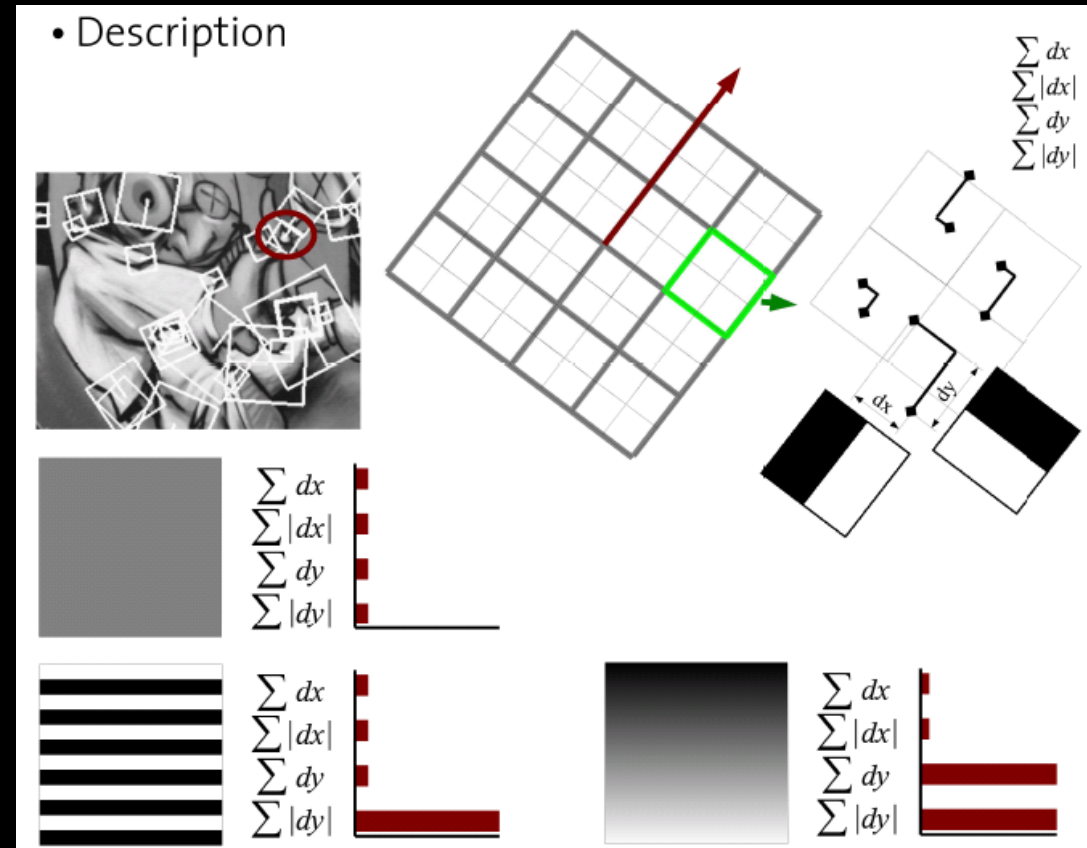
128 hodnôt · 4 x 4 x 8 hodnôt HOG



SURF

Haar wavelet odozvy vo vertikálnom smere
a horizontálnom smere

4 príznaky x
16 oblastí =
64 hodnôt



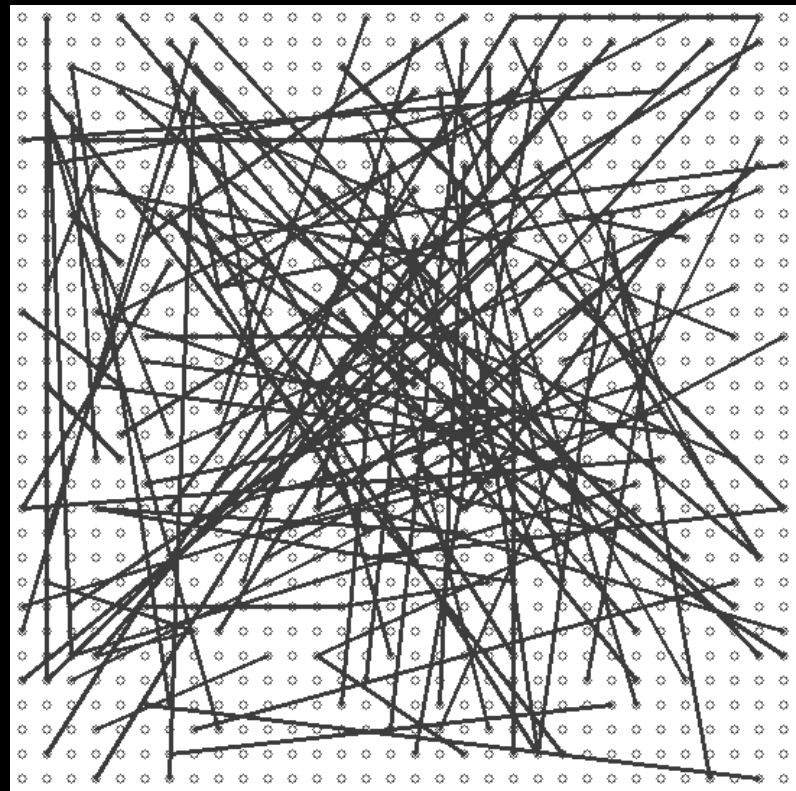
BRIEF

jeden z prvních binárních deskriptorů

porovnává intenzitu dvojíc pixelů v okolí
zaujímavých bodů

=> bitový deskriptor

- 256 / 128 bitů



Porovnanie bodov

Euklidovská vzdialenosť

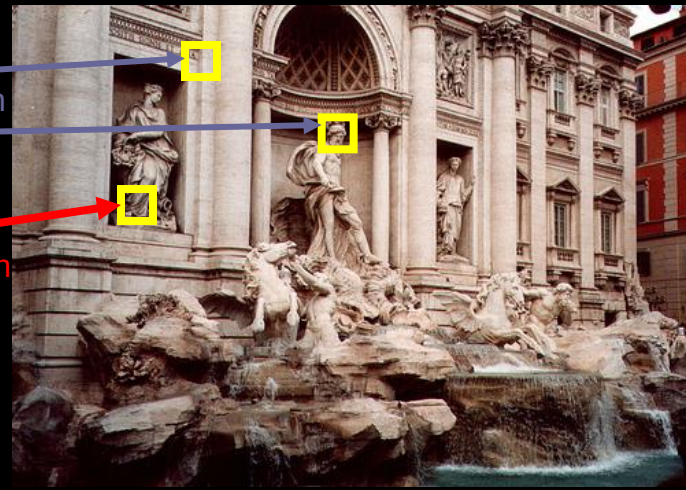
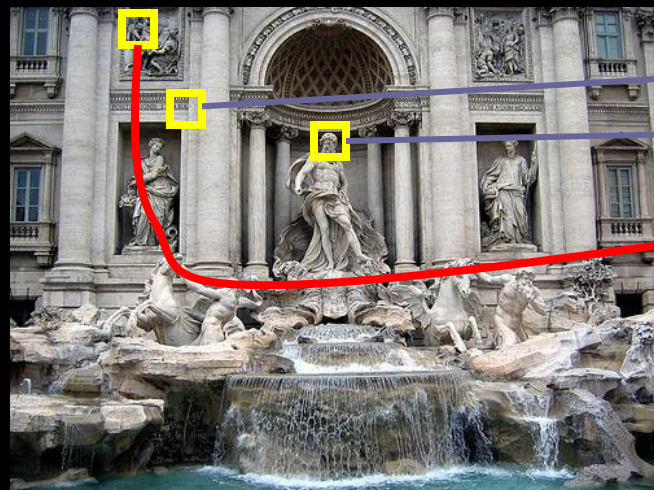
$$d_e(p, q) = \sqrt{\sum_{i=1}^n (p_i - q_i)^2}.$$

Hammingova vzdialenosť

$$d_h(p, q) = \sum_{i=1}^n \delta(p_i, q_i) / n$$

where

$$\delta(p, q) = \begin{cases} 0 & \text{if } (x < 0 \wedge y < 0) \vee (x = 0 \wedge y = 0) \\ 1 & \text{if } \textit{otherwise} \end{cases}.$$



50
true match

75

200
false match

feature distance

