

20 Years of Volume Rendering

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Overview

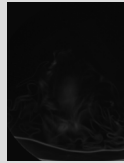
- Volume data and scanning modalities
- Volume visualization
 - Volume viewing
 - Mapping
 - Volume rendering
 - Direct volume rendering
 - Isosurfacing
- Conclusions

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Volume Data

- A spatial sequence of 2D images – slices
- Produced by
 - 3D scanners (tomographs)
 - Different physical background
 - Different and complementary properties
 - Simulation
- Areas of application:
 - Medicine
 - Physics
 - Geology
 - ...
 - Computer (volume) graphics

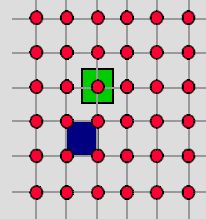


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3D Discrete Space

- 3D grid point (sample): ●
 $P = [x, y, z], x, y, z \in Z$
- Value at sample P: density
- Voxel: ■
 - Voronoi neighborhood of P
 - NN interpolation
- Cell: ●●●●
 - 8 samples
 - higher order interpolation

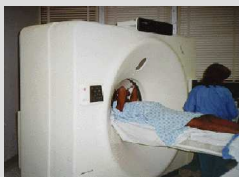


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Volume Data Acquisition

- Different physical configurations
- Example: A CT scanner
 1. One-dimensional X-ray projections
 2. Reconstruction

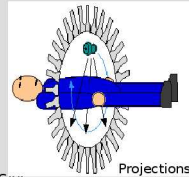


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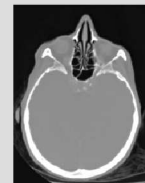
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Volume Data Acquisition

- Different physical configurations
- Example: A CT scanner
 1. One-dimensional X-ray projections
 2. Reconstruction



Reconstruction
from projections

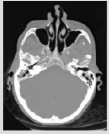


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3D Modalities (1)

Computed tomography – CT



- X-ray based
- Consistent scale (Hounsfield units, -1000..3095)
- High spatial resolution (below 1mm³)

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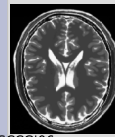
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3D Modalities (2)

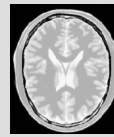
Magnetic Resonance Imaging



T1



T2



PD

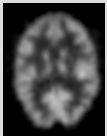
- Interaction of hydrogen nuclei with external magnetic field
- Good soft tissue contrast
- Numerous free parameters

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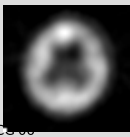
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3D Modalities (3)

Nuclear Imaging – PET, SPECT



PET



SPECT

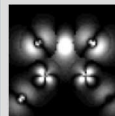
- Scanning protocol:
 1. Dopant introduction
 2. Radiation measurement
- Low resolution images
- Shows organ activity

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3D Modalities (4)

Synthetic data



Simulated electron density



Voxelized teapot model

- Physical simulation
- Voxelization
 - Conversion of geometric objects to volumes

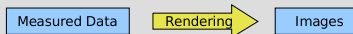
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Volume Visualization

Visually perceivable data presentation

- Understanding, not photorealism
- Simple volume viewing
 - Straightforward presentation of measured data



- Mapping techniques
 - Measured densities are mapped to visual attributes (transparency, color)

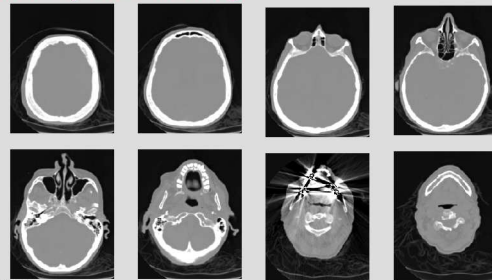


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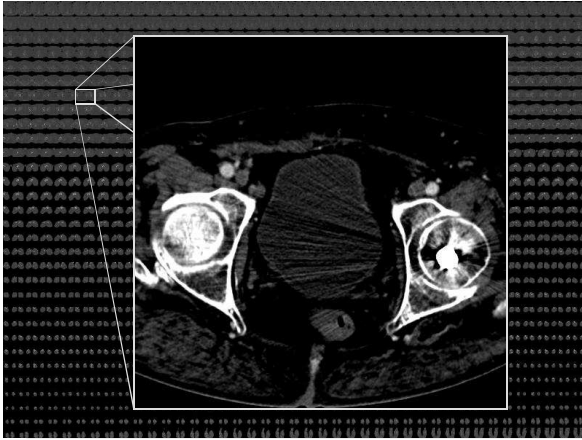
Volume Viewing (1)

Slice-by-slice viewing



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Volume Viewing (2)

Multiplanar reconstruction
- Definition of new cutplanes

Axis aligned

Oblique

Combined

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Volume Viewing (3)

Curved planar reconstruction
- Volume cutting along a line

→

Kanitsar 2002

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Volume Viewing (4&5)

Reprojection
- Add all values along a viewing ray
- Simulation of X-ray projection

Maximum intensity projection
- Register the brightest value along a viewing ray
- Suitable for thin structures

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Volume Visualization by Mapping

↓

Data Acquisition
CT, MRI, USG, PET, SPECT

↓

Mapping
Visual attributes

↓

Rendering
Surface & Volume Techniques

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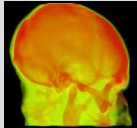
Why Do We Need Mapping?

- No visual representation readily exists for 3D data
- Area of interest is occluded by the black background
- We need something to make the background transparent

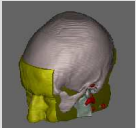
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Mapping

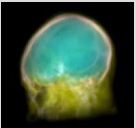
- Mapping:** Assignment of visual attributes to data:
 - transparency, color, reflectance, surface strength...
- “Area of interest” specification achieved:



Density-based
classification



Space-based
segmentation

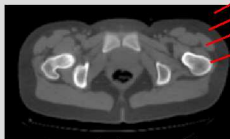


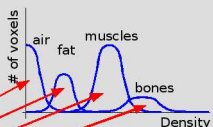
Combined

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Mapping by Density Classification

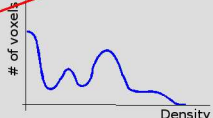
- Prerequisites:**
 - Areas of interest can be identified solely by density value
 - Neighbors in histogram are neighbors in space





of voxels

Density

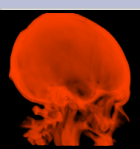


of voxels

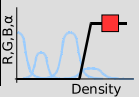
Density

SCCG'06 CT scan of a human pelvis 20/65

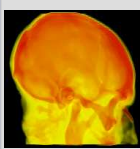
Density Classification by Transfer Functions



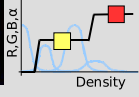
Bone only

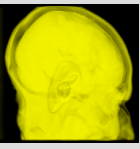


$R, G, B, \alpha = f(\text{density})$

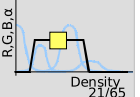


Bone & soft





Soft only



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TF Design Questions

- How to set TFs to get desired appearance
 - A typical inverse problem
- How to set TFs for unknown data
 - Meaningful TFs reflect data properties
- One possible answer: **Design Gallery** (Marks 1997)
 - Automatically generated selection of perceptually different images
 - Exhaustive search of the space of all possible TFs

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Design Gallery



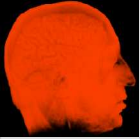
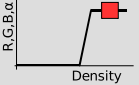
[Marks 1997]

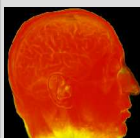
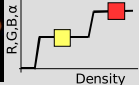
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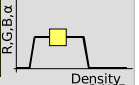
Transfer Functions with General Data

MRI Data:

- The histogram/position model not fulfilled
- No TF can separate the tissues
- Additional info required

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Additional Information for Better Rendering

We need to localize the Tfs

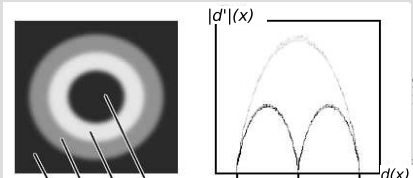
- Partial problem solution by **multidimensional TFs**:
 - $|d'|$ vs. d scatterplots
 - LH-histograms
- Full solution by **segmentation**

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Two- (multi-)dimensional TFs (1)

- TF design paradigm based on $|d'|$ vs. d scatterplot analysis
- Observation: special arc-shaped of blurred data

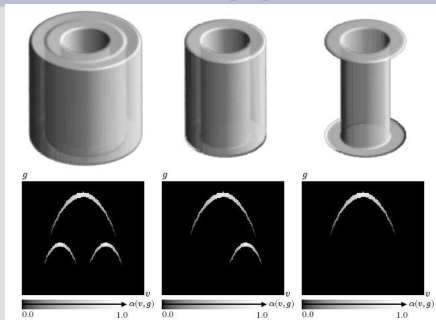


[Kindlmann 1998]

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Two- (multi-)dimensional TFs (2)



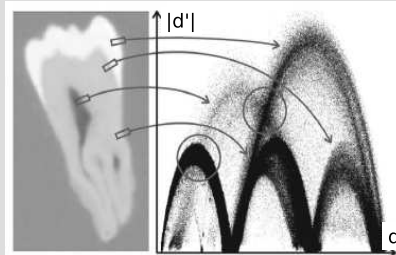
[Kindlmann 1998]

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Two- (multi-)dimensional TFs (3)

- A complex dataset: $|d'|$ vs. d scatterplot



[Sereda 2006]

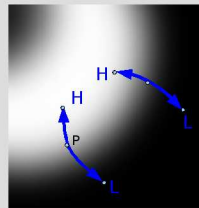
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TF Design by LH-Histograms (1)

LH-Histogram:

- Downhill and uphill stationary values
- A boundary is represented by a single point

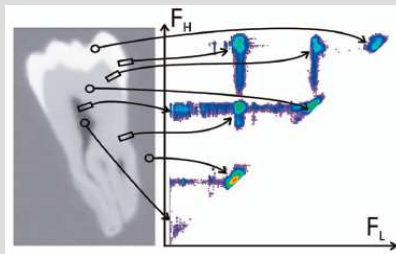


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TF Design by LH-Histograms (2)

- A complex dataset: LH-Histogram

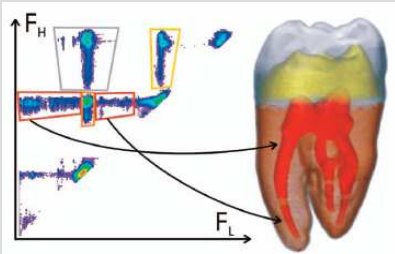


[Sereda 2006]

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TF Design by LH-Histograms (3)



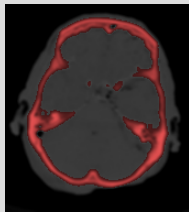
[Šereda 2006]

Mapping by Spatial Segmentation

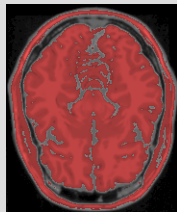
- The process of **isolating objects of interest** from the rest of the scene (Castleman, 1979)
- Techniques:
 - Gradient-, density- and/or texture-based
 - Fully automatic, semiautomatic, manual
 - See CV & IP literature for more
- Complexity
 - from trivial to hard

Segmentation by Thresholding

- Applicable for data, when density TFs are also OK



CT data: easy by thresholding



MRI data: impossible by thresholding

Volume Data and Segmentation

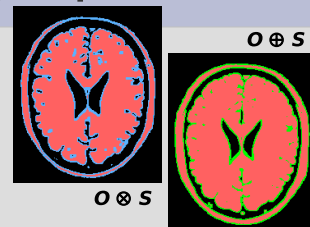
- Large number of anatomically distinct objects
- Variability of object shapes
- Variability of scanner types and parameter settings
- 3D nature of objects
- High demands on segmentation precision
- No universal technique exists

Interactive Segmentation (The ISEG Tool)

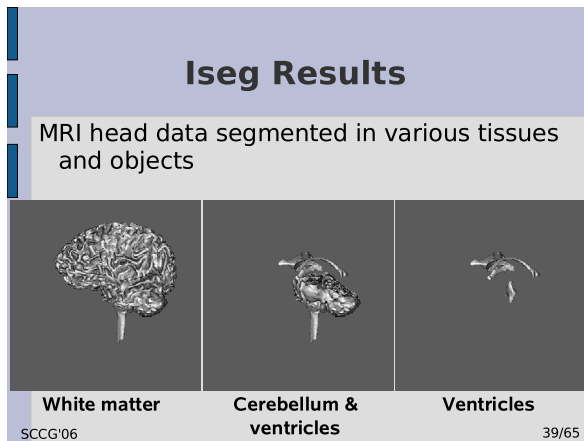
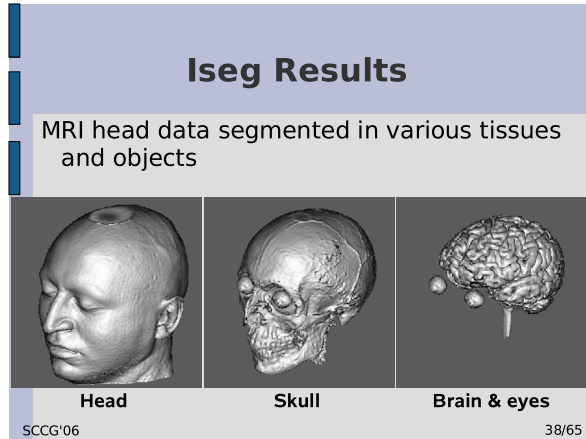
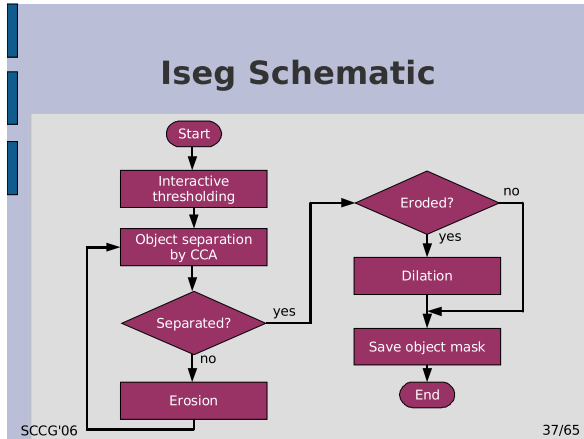
- Anatomic organs are connected and homogeneous:
 - Objects identification by
 - Thresholding
 - Connected component analysis (CCA)
- Objects are sometimes interconnected
 - Objects separation by morphological operations

Morphologic Operations

- Erosion $O \otimes S$
 - Peeling the outer layer off
- Dilation $O \oplus S$
 - Thickening by adding a layer
- Erosion + Dilation \neq Original !!



Structuring elements



- ### Mapping: Summary
- **Transfer function based:**
 - Color & transparency assigned to voxels
 - Semitransparent volumes
 - Display of volumes
 - **Segmentation-based**
 - Unambiguous object definition
 - Color & transparency assigned to objects
 - Display of surfaces
- (not used for classification of rendering techniques)
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- ### Classification of Rendering Techniques (1)
- Based on the basic rendering primitive
- **Surface rendering**
 - Basic primitive: 2D patches (polygons)
 - Extra data structure: a surface model
 - Decoupling of the model and the data
 - Rendered by standard CG approaches
-
- Triangulation by the Marching Cubes technique, approx. 200000 polygons
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Classification of Rendering Techniques (2)

Volume rendering

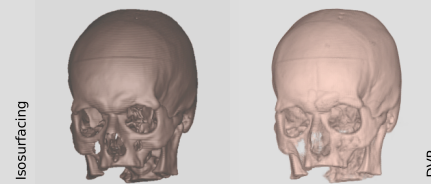
- Basic primitive: the voxel itself
- Rendering directly from volume data:
- Two flavors:
 - TF based: **Direct volume rendering (DVR)**
 - All volume samples potentially contribute to the image
 - Segmentation (object) based: **Isosurfacing**
 - Only visible surfaces are displayed

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DVR vs. Isosurfacing

- Rendering algorithms are similar
- Isosurfacing is a limit case of DVRs with special TF and parameter setting

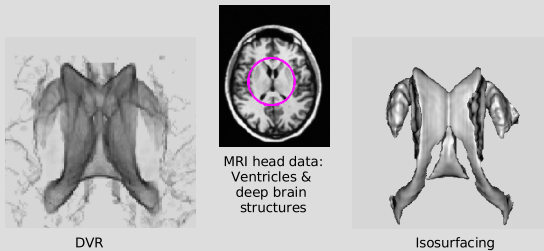


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When to Prefer DVR?

- Low data contrast, weak edges, thin objects



DVR

MRI head data:
Ventricles &
deep brain
structures

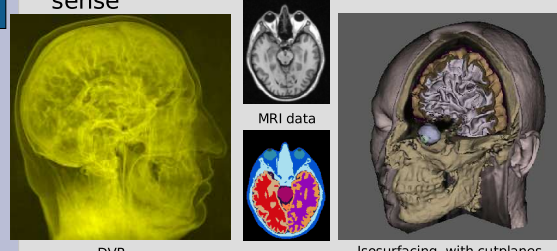
Isosurfacing

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When to Prefer Isosurfacing?

- Numerous & complex objects, TFs make no sense



DVR

Object labels

Isosurfacing with cutplanes

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DVR Basics

- Simplified light interaction with semi-transparent material (**Beer's Law**)

$$\frac{dI(t)}{dt} = \rho(t)I(t) - k(t)\rho(t),$$

$I(t)$: Light intensity at the point t
 $\rho(t)$: Optical density (attenuation)
 $k(t)$: Chromacity
 $k(t)\rho(t)$: Light emission rate at t
 $\rho(t)I(t)$: Light attenuation at t

- Numerical evaluation
 - Per-segment compositing by Porter&Duff's operators
 - Front-to-back order
 - Back-to-front order

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DVR Techniques (1)

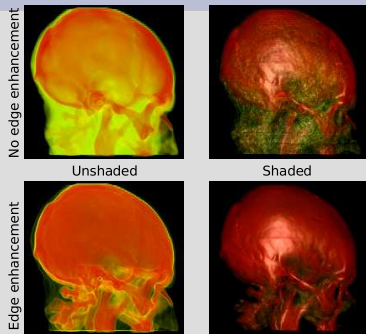
Free/adjustable parameters:

- Transfer functions: $\rho(t) = f_\rho(d(t))$
 $k(t) = f_k(d(t))$
- Edge accentuation: $\rho(t) \sim |\nabla d(t)|$
- Shading: $s(t) \sim \nabla d(t) \cdot \vec{p}$
- Depth cueing
- ...

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DVR Techniques (2)



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DVR Algorithms

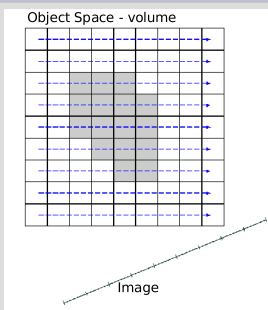
- **Object order algorithms** (splatting)
 - Projection of samples from volume to image
 - Compositing in image plane
- **Image order algorithms**
 - Ray casting based
 - Sequence of samples along the ray
 - Compositing along the ray

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Object Order VR: Splatting (1)

- Samples/voxels are projected (splatted) onto the viewing plane
- Back-to-front of front-to-back order
- One sample projects onto several pixels: footprint



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Object Order VR: Splatting (2)

- Traversal order depends on viewing angles
- The most parallel scanline to image is chosen
- Popping artifacts:

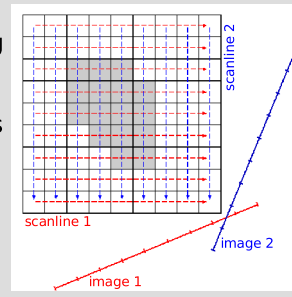


rot=45°



rot=45.1°

[Mueller, 1998]



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Object Order VR: Splatting (3)

- Image aligned sheet-buffer
- No popping

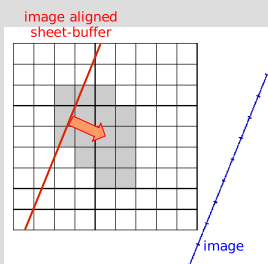


rot=45°



rot=45.1°

[Mueller, 1998]

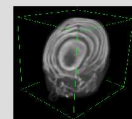
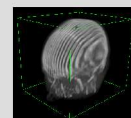
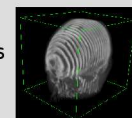


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HW Acceleration by Texture Mapping

- Do the costly part by hardware
- 2D Textures
 - compositing only
 - volume aligned slices
 - three copies of the volume required
- 3D Textures
 - interpolation & compositing
 - image aligned slices
- Shading possible in fragment programs



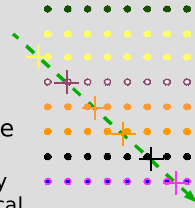
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Image Order VR by Ray-Casting

1. Shoot rays from each pixel
2. Define a sequence of samples
3. Accumulate color and opacity along each ray

- CPU and GPU implementations possible
- Acceleration required:
 - Adaptive sampling, empty space skipping, hierarchical subdivision, early termination

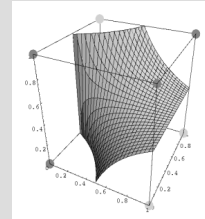


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Isosurfacing Basics

- Isosurface definition by interpolation & thresholding
- Interpolation domain:
 - Original densities
 - Segmentation labels



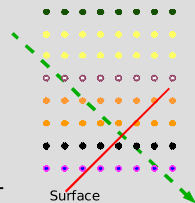
Interpolation surface within a single cell

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Isosurfacing Basics

- Isosurface definition by interpolation & thresholding
- Interpolation domain:
 - Original densities
 - Segmentation labels
- Algorithms:
 - (First hit) ray tracing
 - Ray/surface intersections by numerical root finding
- CPU and GPU implementations possible
- Acceleration required

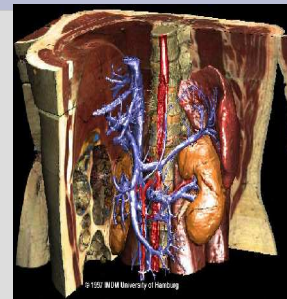


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Ray Casting Advantages

- Simplicity and flexibility
- Combination of techniques possible:
 - DVR, isosurfacing, MIP, CPR, cutplanes
 - per object definition of techniques and parameters



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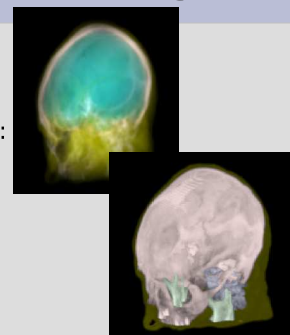


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Conclusion

- We have plentiful volume rendering techniques
- We still do not have enough memory
- The computers are still not fast enough
- The doctors still prefer slice-by-slice viewing (but getting better recently...)

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And what hapenned 20 (18) years ago?

Two papers were published:

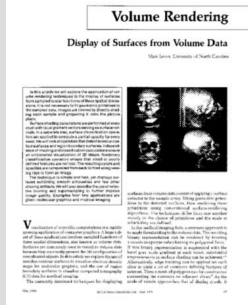
- Drebin, Carpenter, Hanrahan: Volume Rendering (Siggraph)
- Marc Levoy: Display of Surfaces from Volume Data (IEEE CG&A)



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