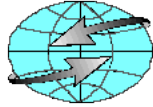




Slovak University of Technology Bratislava



FACULTY OF ELECTRICAL ENGINEERING AND INFORMATION TECHNOLOGY



Department of Telecommunications

Spectral Domain Image Segment Restoration

Diploma Thesis

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Image Reconstruction

- Filling in the missing areas or modifying the damaged ones in a **non-detectable** way by an observer not familiar with the original image
- Quite new method in digital image processing (1999)
- Visual system of human contains mechanisms actively connecting image regions that are physically disconnected on the retina – **visual completion**
- Application: data loss during transmission, compression

Existing Methods

- Inpainting – image interpolation
 - Bertalmio, TV, CDD,...
 - Commonly applicable when small area is damaged
 - Not able to fix larger regions
- Texture synthesis
 - Resynthesizer
 - Heavy on computational time
 - Working with whole image
- Combination of both methods

Analysis and Design of Solution

Main Scheme

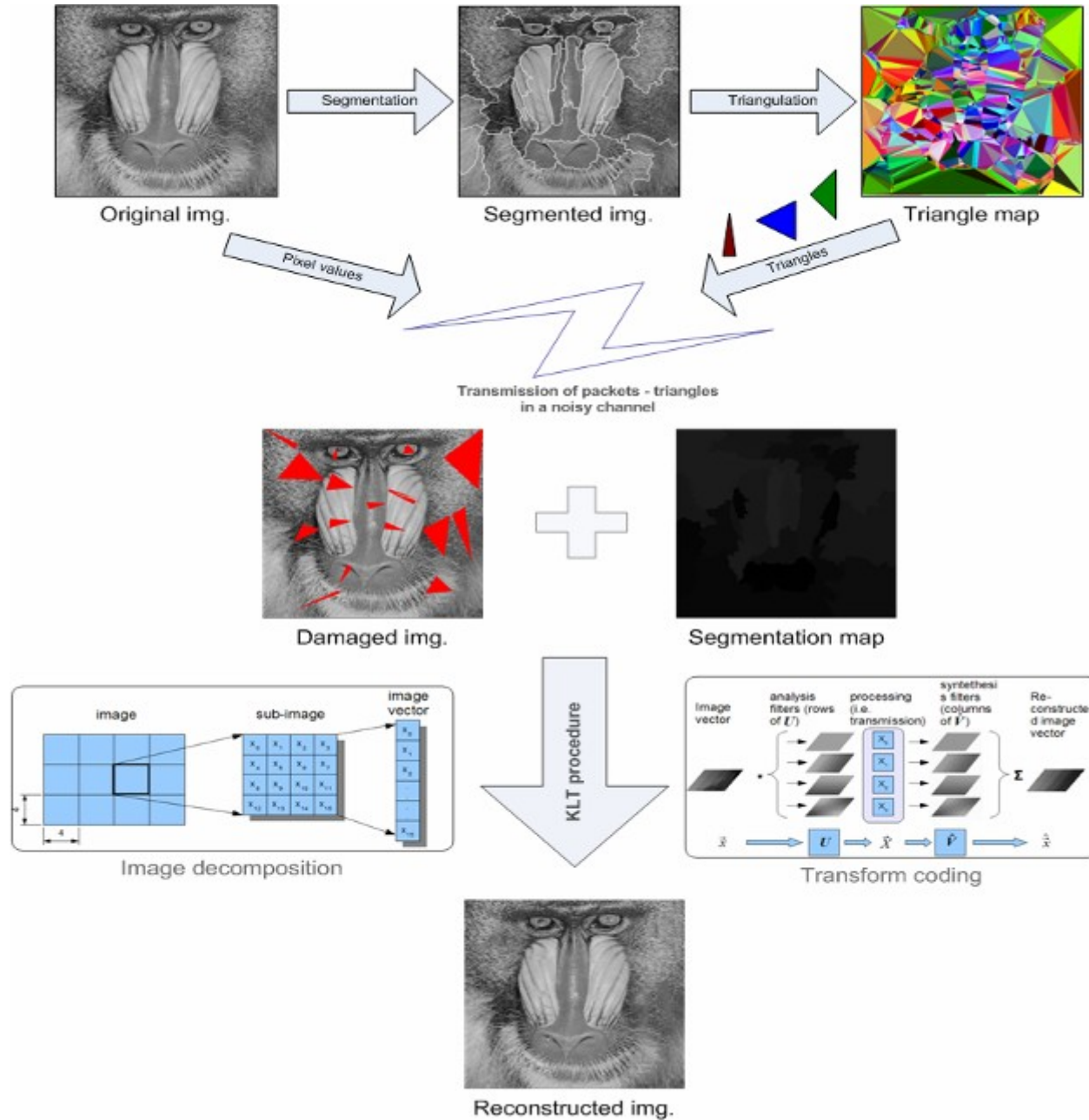


Image Segmentation

- Connecting basic elements to the whole
- JSEG approach was used for this work – based on testing homogeneity of a given texture pattern
- Assumptions:
 - Each image contains homogeneous regions
 - Each image region can be represented by a set of few colors
 - The colors between two neighboring regions are distinguishable

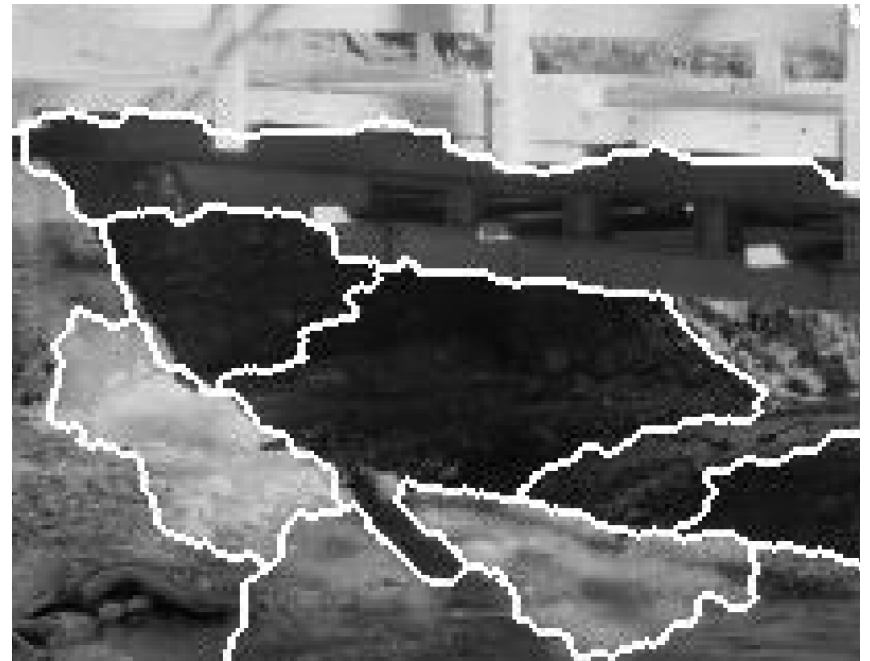
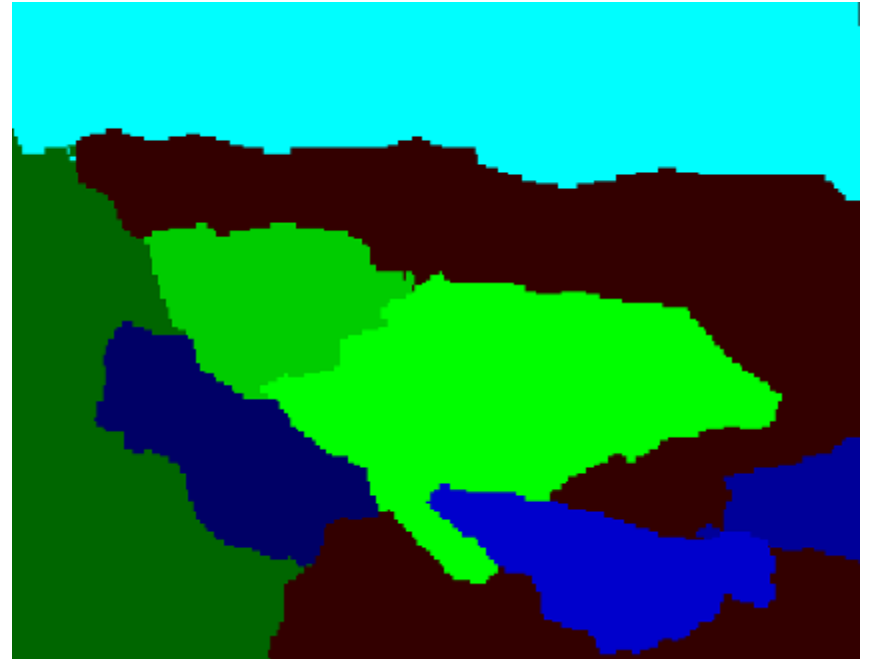


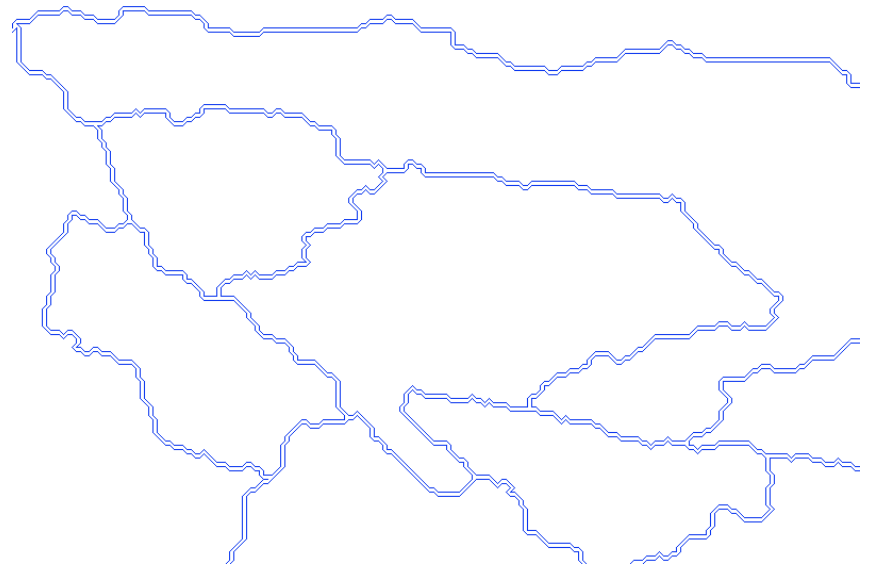
Image Segmentation

- Segmentation map – each image region is defined by unique label



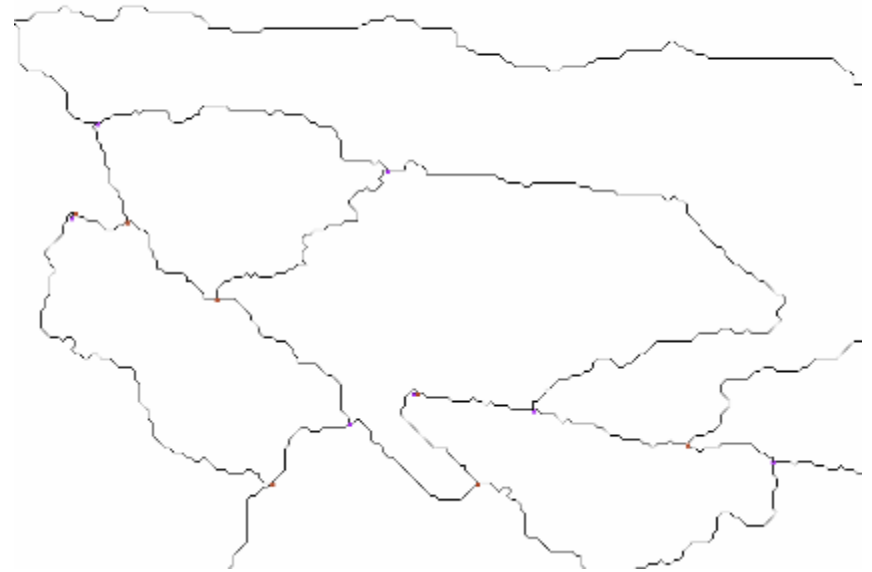
Polygonal Approximation of the Region Boundaries

- Region boundary – value of at least one of neighboring pixels differs from the region value
- There are cases of two parallel boundaries between regions



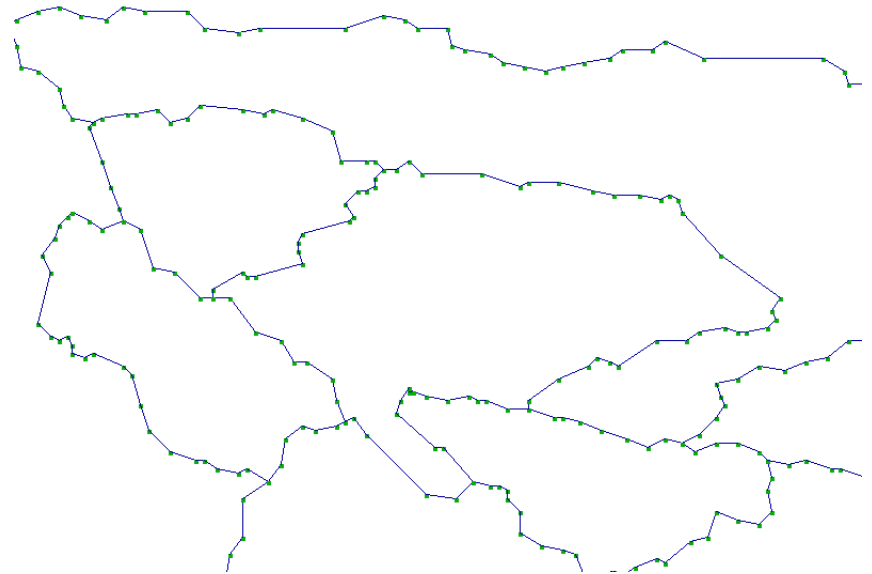
Polygonal Approximation of the Region Boundaries

- Doubled boundaries have to be reduced to be only one pixel wide
- Removing of very small segments by attaching to their larger neighbors has significant impact on the resulting code efficiency



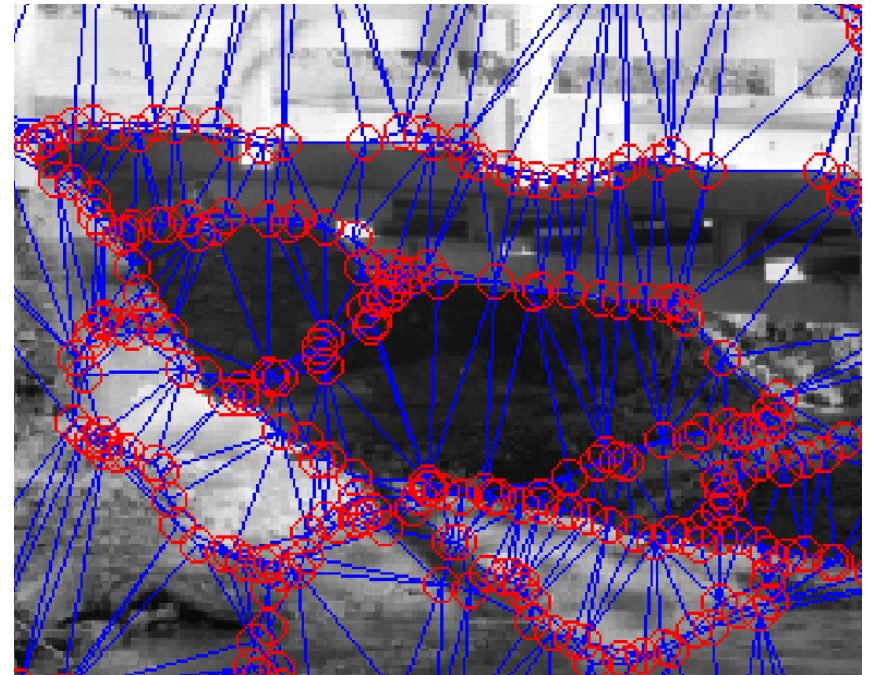
Polygonal Approximation of the Region Boundaries

- The boundaries of the segments are simply approximated with polygons
- The code is lossy – small influence on the quality of the resulting image



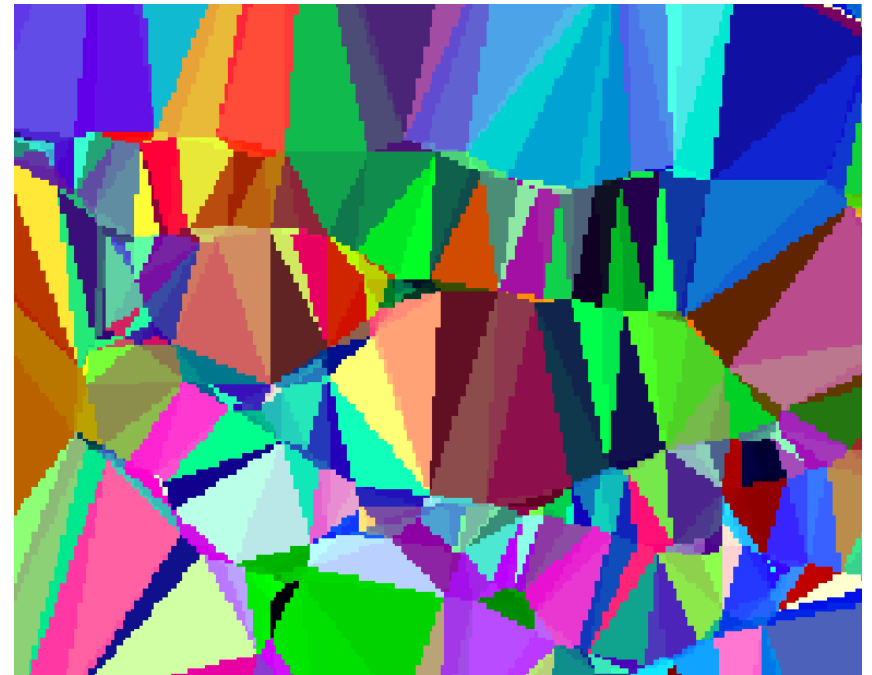
Triangulation of the Image Objects

- Image objects are divided into set of non-overlapping triangles using Delaunay triangulation that preserves original vertices of polygons



Triangulation of the Image Objects

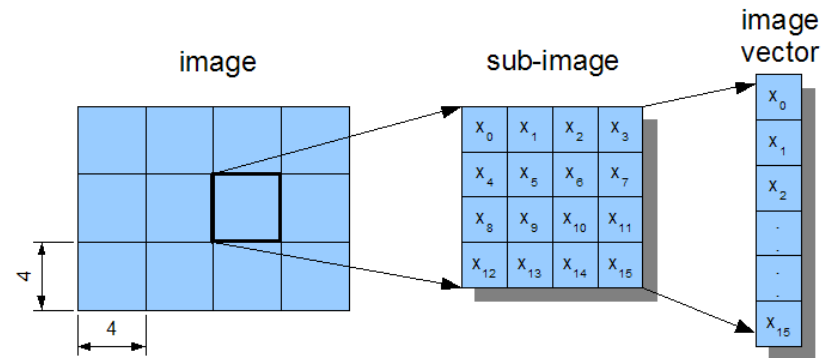
- Triangles are separated objects in the context of given image segment
- We assume loss or damage of these regions



Transform Coding

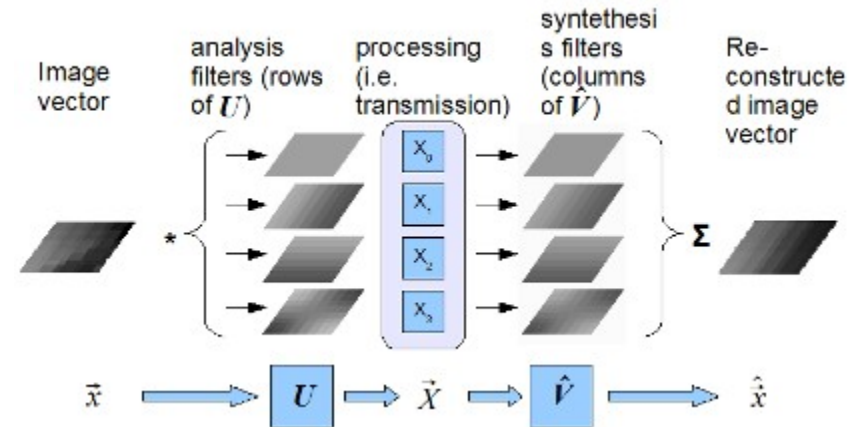
- Forward transformation

$$\vec{X} = \frac{1}{N} \cdot U \cdot \vec{x}$$



- Inverse (backward) transformation

$$\vec{x} = U^i T \cdot \vec{X}$$



Karhunen-Loève Transform (KLT)

- The transformation matrix satisfies relation
- C is the covariance matrix and Λ is a diagonal matrix with eigenvalues

$$UC = \Lambda U$$

$$\Lambda = \begin{pmatrix} \lambda_1 & 0 & \dots & 0 \\ 0 & \lambda_2 & & \vdots \\ \vdots & & \ddots & 0 \\ 0 & \dots & 0 & \lambda_M \end{pmatrix}$$

Karhunen-Loève Transform (KLT)

$$\vec{x}_D = U_D^T \vec{X}$$

- If we constrain approximation with D eigenvectors from the C matrix, than **approximated** vector is reconstructed
- KLT is **optimal** at mean square error
- The basis is created by **adaptive** way, according to available vectors
- Optimal value of **D is dependent to data**

KLT for Gappy Data

- **Only** damaged data are available !
- Image vector with missing values is artificially created with **mask vector m**
- The goal is to restore complete image vectors from damaged vectors of the **segment**
- **Error minimisation** leads to the system of linear equations
- The solution is vector with **spectral coefficients**, which we wanted

$$M \vec{\beta} = \vec{f}$$

Construction of the KLT Basis

- Missing values are filled in with **average value** available for the pixel
- This new set is used for the first approximation of the basis
- KLT procedure is then used for reconstruction of each damaged vector
- This process can be iteratively repeated

$$\gamma_i^{(k)} = \begin{cases} \gamma_i^{(k)} & \text{if } m_i^{(k)} = 1 \\ \gamma_D^{(k)}(\mathbf{0}) & \text{if } m_i^{(k)} = 0 \end{cases}$$

$$\gamma_i^{(k)}(\mathbf{1}) = \gamma \{ \gamma \gamma \gamma \}$$

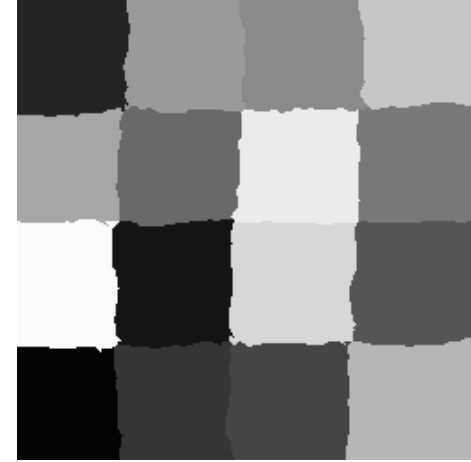
Measures of Quality

- Objective criterion:
 - mean square error
 - peak signal – noise ratio
- distance between two histograms

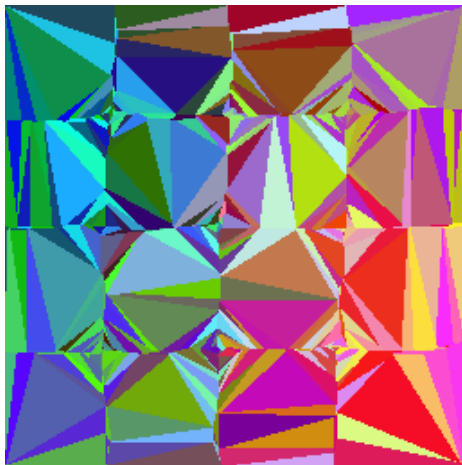
Results – Texture Restoration



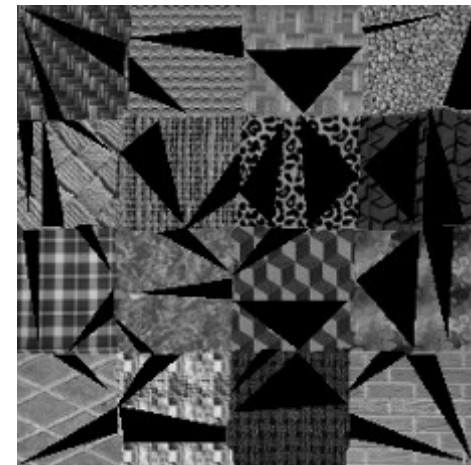
Original image 256x256 pixels



Segmentation map

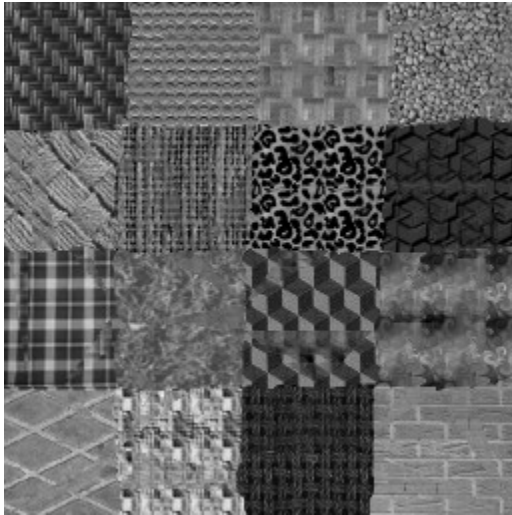


Triangle map

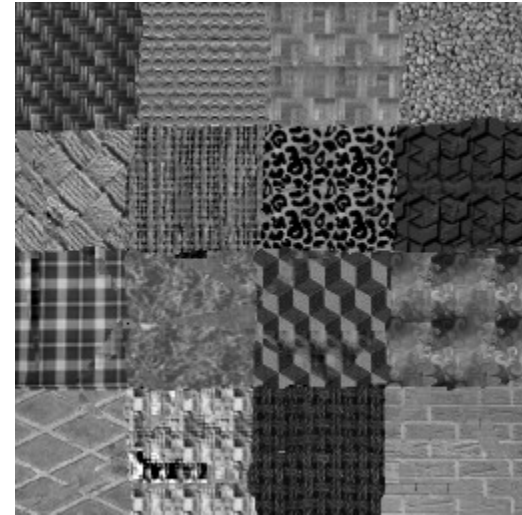


Damaged image – masked

Results – Texture Restoration

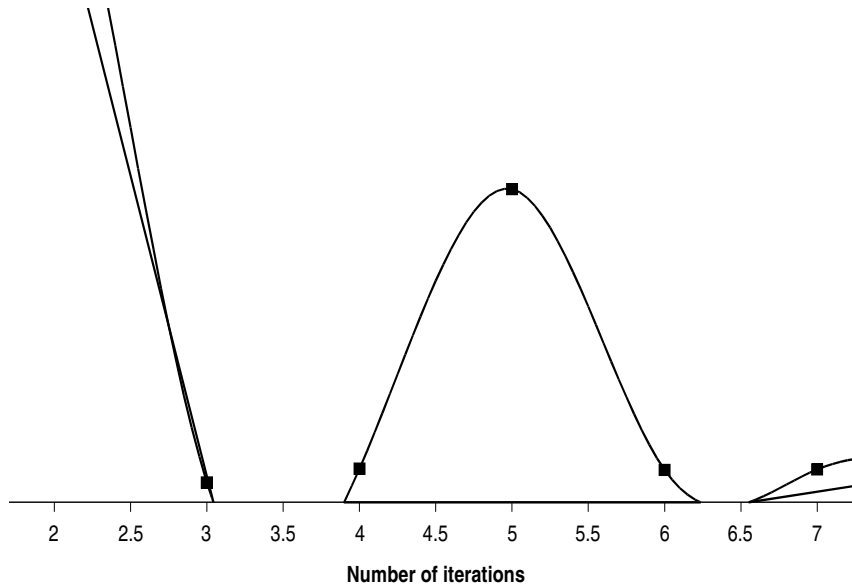


Restored image: KLT (D=2, 1 iteration)

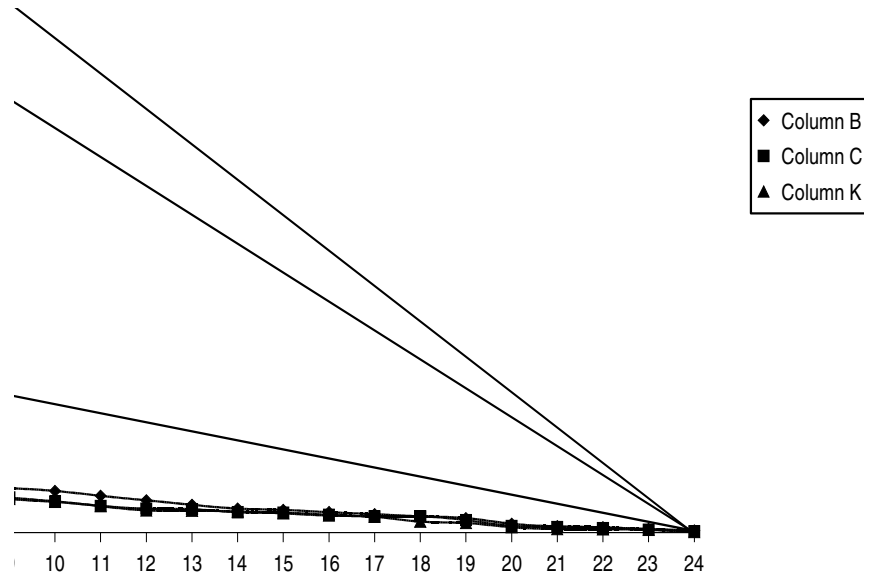


KLT (D=2, 10 iterations)

Graphs – Texture Restoration

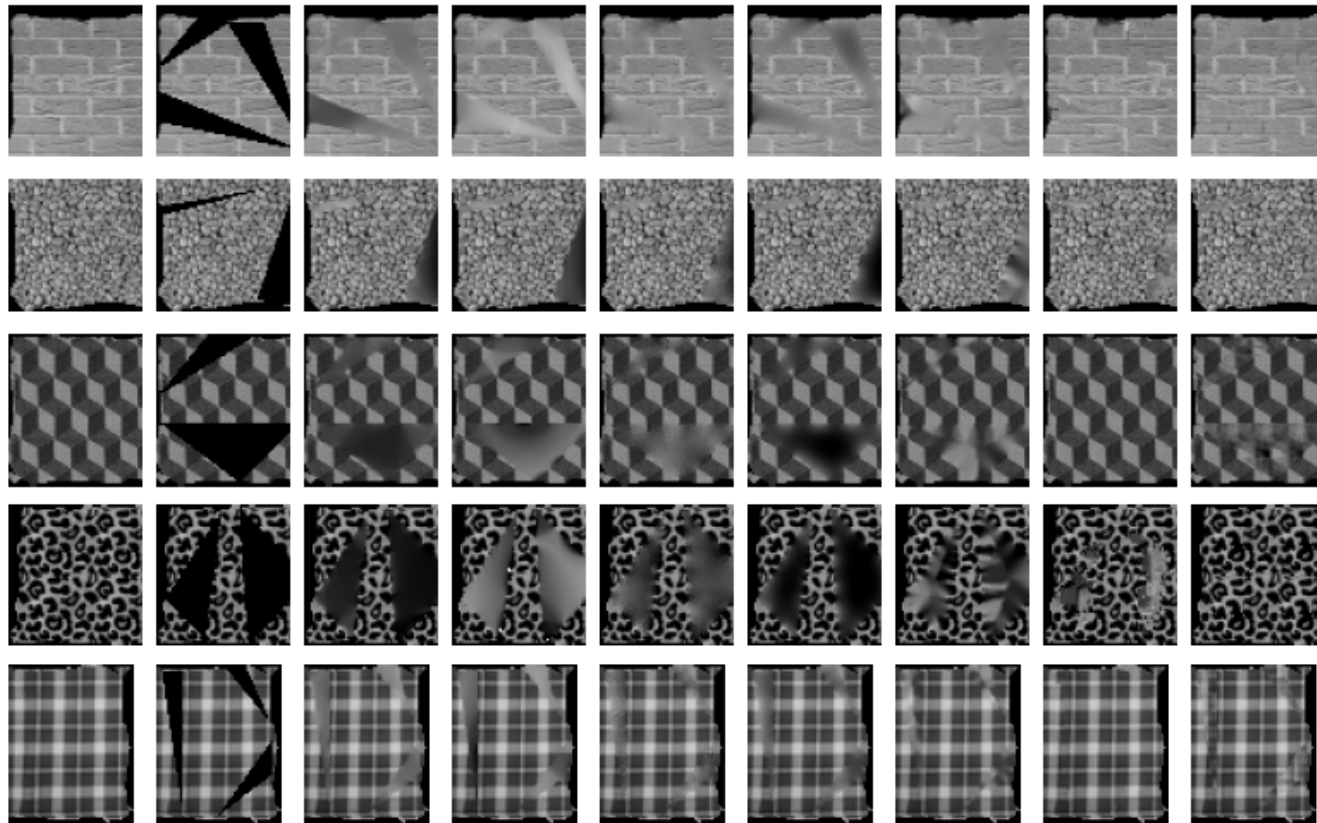


PSNR for segment no.2 –
processing image by segments
and as whole



Convergence of eigenvalues
spectrum KLT (D=2) for segment
no.8 – 1,2 a 10 iterations

Methods Comparison



a) b) c) d) e) f) g) h) i)

Methods comparison: a) original, b) damaged, c) Bertalmio, d) TV, e) CDD, f) Oliveira, g) Mean, h) Resynthesizer, i) KLT (D=2, 1 iteration)

Tables – Methods Comparison

Segment	Bertalmio	TV	CDD	Oliveira	Mean	Resynthesizer	KLT
12	16,508	19,614	21,377	18,420	20,868	21,123	23,148
13	9,774	9,949	11,360	9,428	16,016	16,707	17,031
14	15,040	16,065	17,684	14,189	16,151	26,436	19,450
15	10,668	10,748	12,326	10,656	11,623	12,324	14,368
16	17,353	16,193	18,658	18,769	18,585	24,471	17,709

Table with PSNR values in dB

Tables – Methods Comparison

Segment	Bertalmio	TV	CDD	Oliveira	Mean	Resynthesizer	KLT
12	1130	1018	680	1118	630	484	936
13	850	942	690	868	498	398	464
14	1032	1400	1370	1190	742	358	1280
15	2260	1714	2154	1634	1464	952	414
16	740	616	598	708	466	438	556

Histogram distance

Metóda	Čas CPU
Bertalmio	3 min 26,219 s
TV	1 min 19,828 s
CDD	1 min 38,906 s
Oliveira	1453 ms
Mean	171 ms
Resynthesizer	2 min 41 s
KLT	2.75 s

Computational time
(AMD Turion 64M, 1.8GHz)

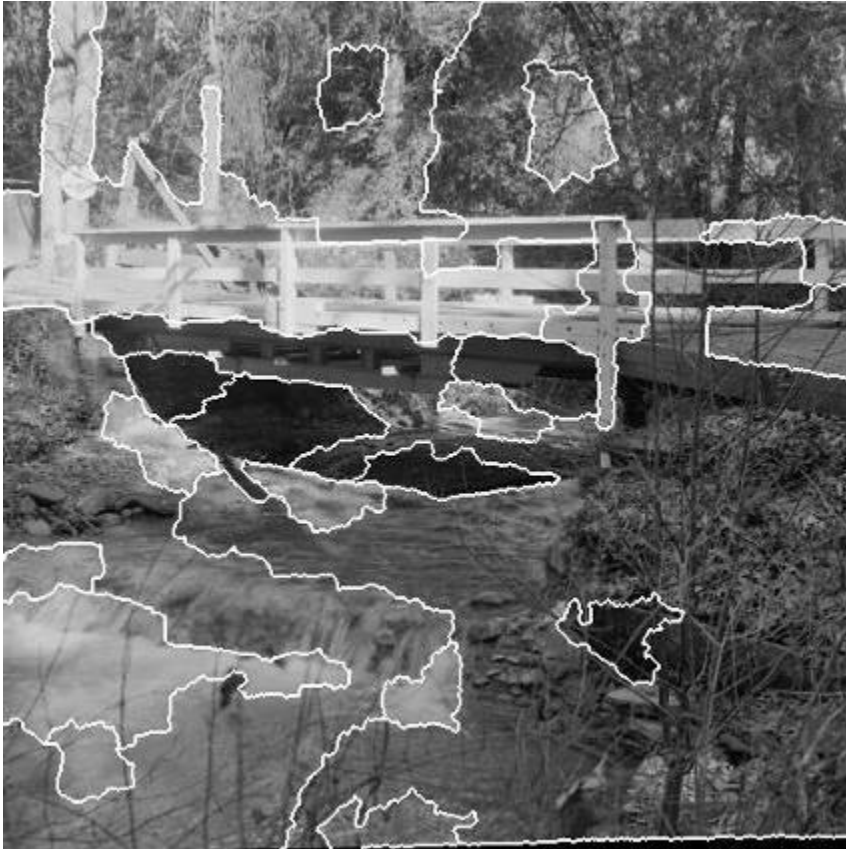
Segment	Poškodenie oblati (%)
12	26,23
13	18,56
14	26,33
15	38,80
16	16,87

Damaged area in %

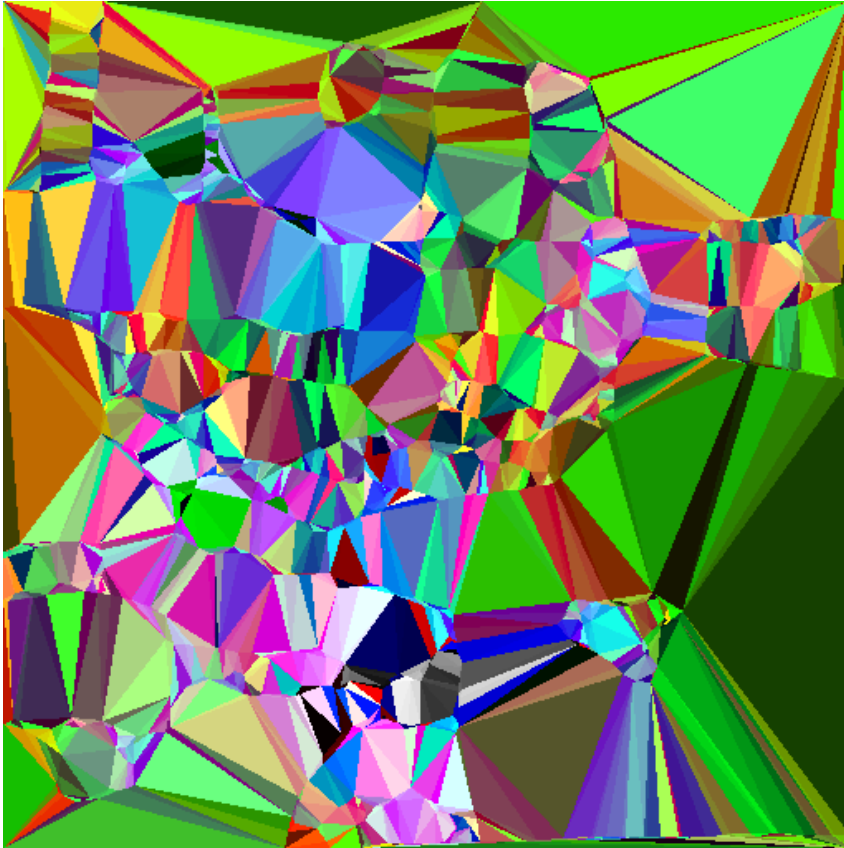
Image – „Stream&Bridge“



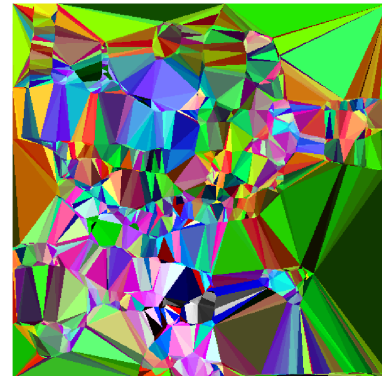
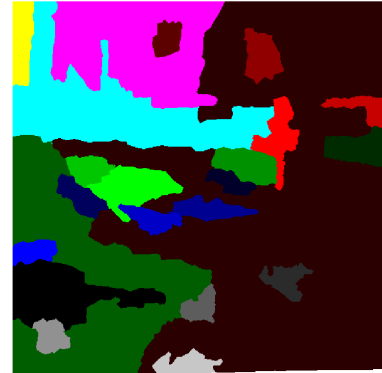
Segmentation – Segmentation Map



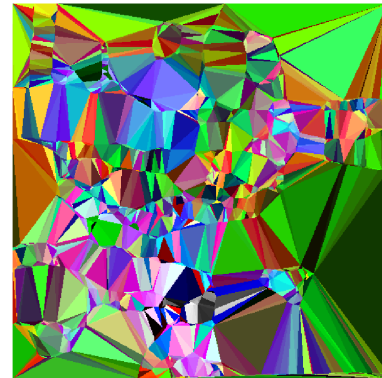
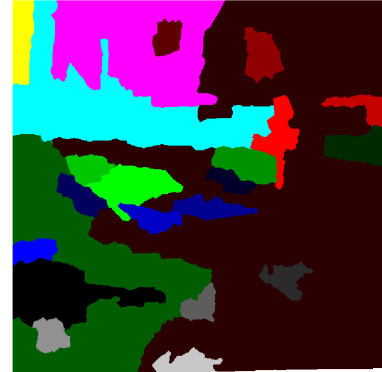
Triangulation



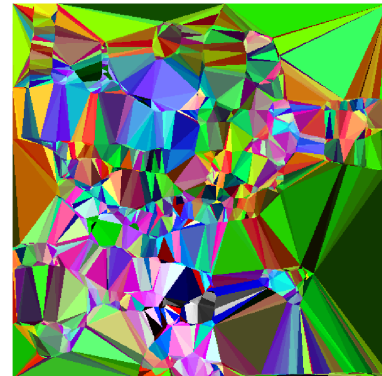
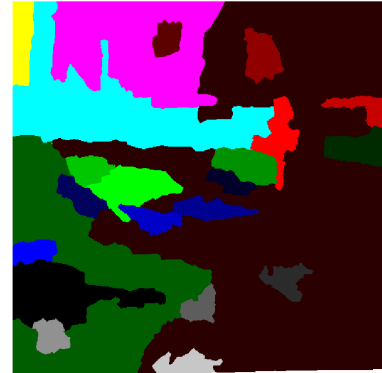
Map of Segments and Triangles



Masking – Damaged Image



KLT – $D=2$, 3 iterations



KLT vs. Bertalmio



KLT vs. TV



KLT vs. CDD



KLT vs. Oliveira



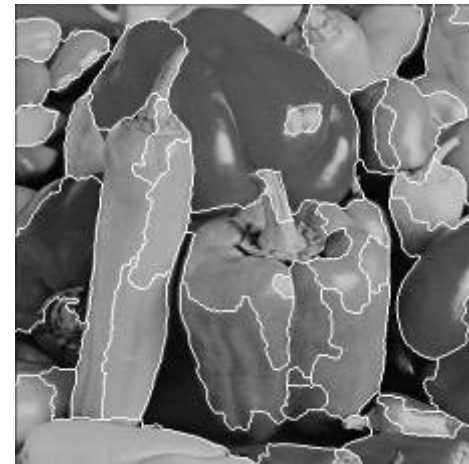
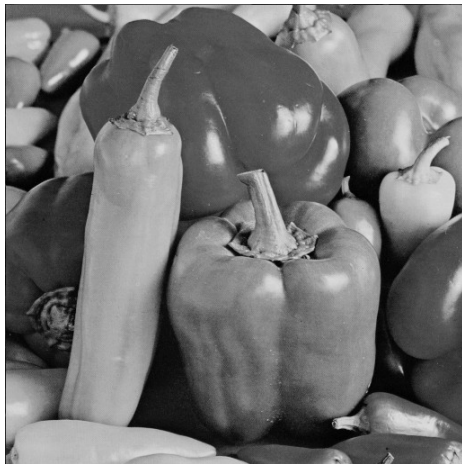
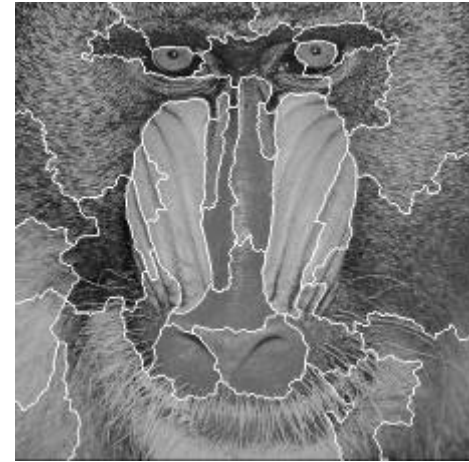
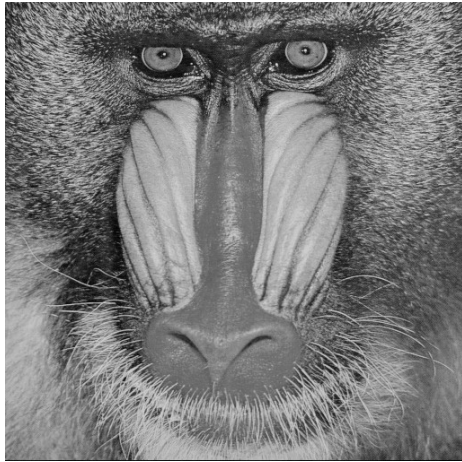
KLT vs. Mean



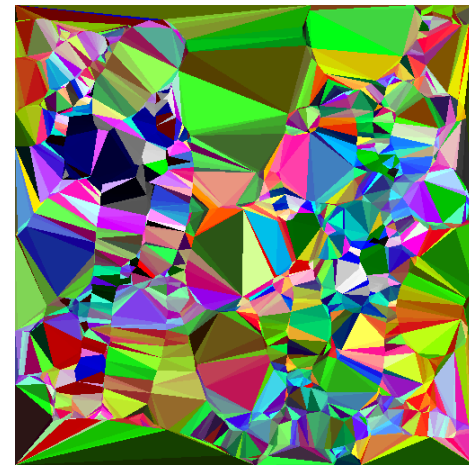
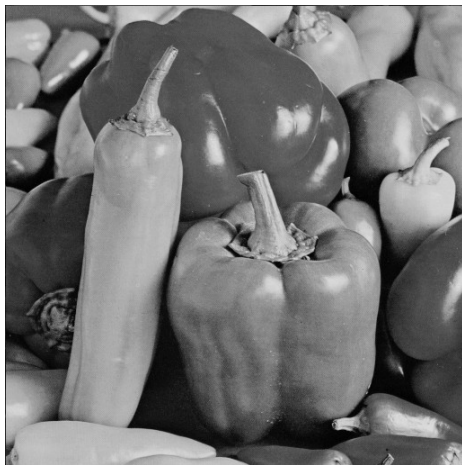
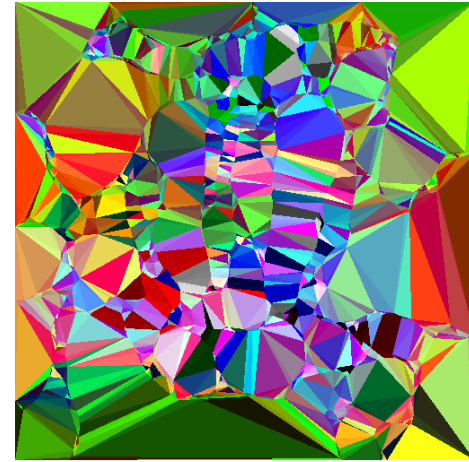
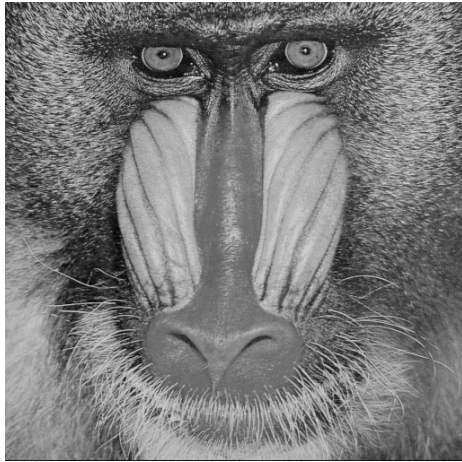
KLT vs. Resynthesizer



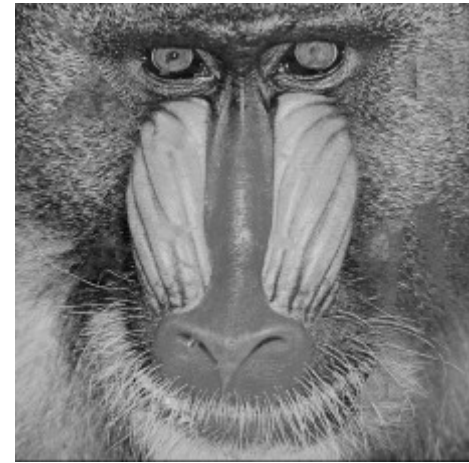
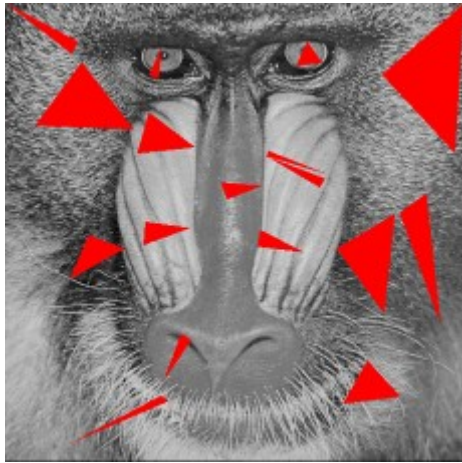
Baboon and Peppers - Segmentation



Baboon and Peppers - Triangulation



Baboon and Peppers – Restoration – KLT ($D=2$, 1 iteration)



Tables

Baboon

	Bertalmio	TV	CDD	Oliveira	Mean	Resynthesizer	KLT (D=2 iter=1)
PSNR [dB]	39.9215	44.3659	49.5500	39.7296	48.3711	48.0540	48.0446
CPU time	18 min 13 s	1 min 53 s	2 min 19 s	1.8 s	250 ms	42 min	18 s

Stream and Bridge

	Bertalmio	TV	CDD	Oliveira	Mean	Resynthesizer	KLT (D=2 iter=3)
PSNR [dB]	42.5476	41.0333	49.7810	41.8134	48.7467	47.1177	48.4396
CPU time	19 min 34 s	2 min 5 s	2 min 34 s	2 s	280 ms	17 min	25 s

Peppers

	Bertalmio	TV	CDD	Oliveira	Mean	Resynthesizer	KLT (D=2 iter=1)
PSNR [dB]	47.7050	45.7515	56.4806	47.2177	56.2860	57.3806	53.2132
CPU time	17 min 1 s	1 min 7 s	1 min 19 s	1 s	171 ms	7 min	16 s

Conclusion

- Comparable results with existing methods
- Faster algorithm than texture synthesis, we are working with segments, not whole image
- Two eigenvectors are enough for approximation
- Appropriate output of segmentation process is required
- Sometimes there are missing spatial information, average value cannot be estimated